



Liquid Crystals defects

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Liquid Crystal Physics

Observed two melting points when heating up Cholesteryl Benzoate.



Friedrich Reinitzer (1888)



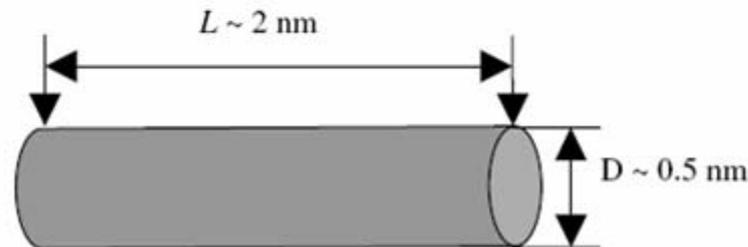
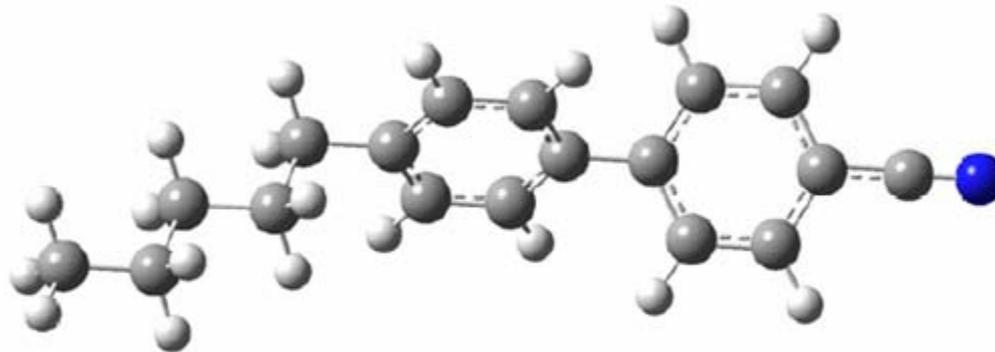
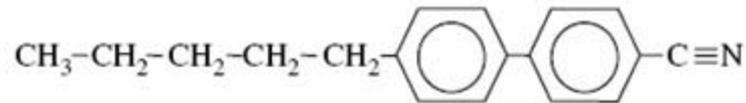
Lehmann (1900)

Established the term *liquid crystal*

Liquid Crystals (rod like)

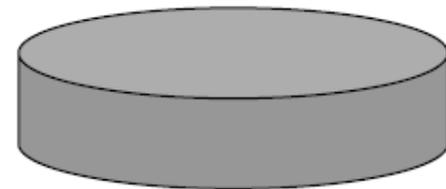
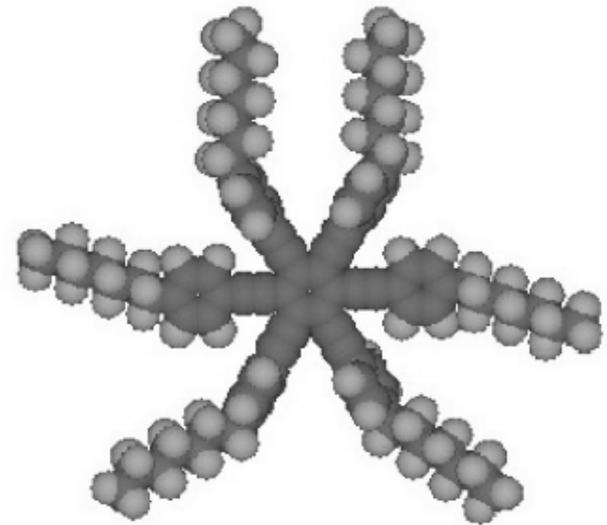
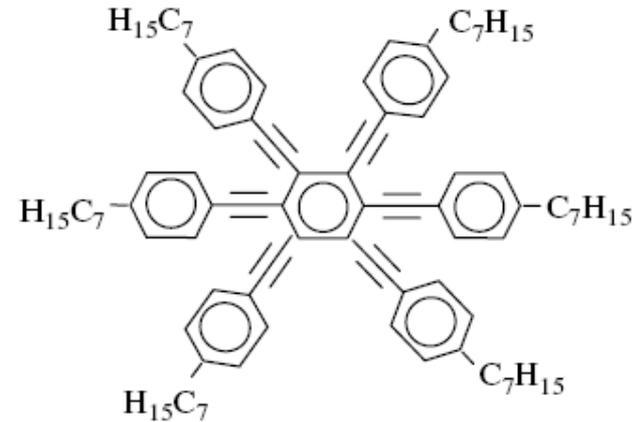
Liquid crystal materials generally have several common characteristics. Among these are a rod-like molecular structure, rigidity of the long axis, and strong dipoles and/or easily polarizable substituents.

4'-n-pentyl-4-cyano-biphenyl

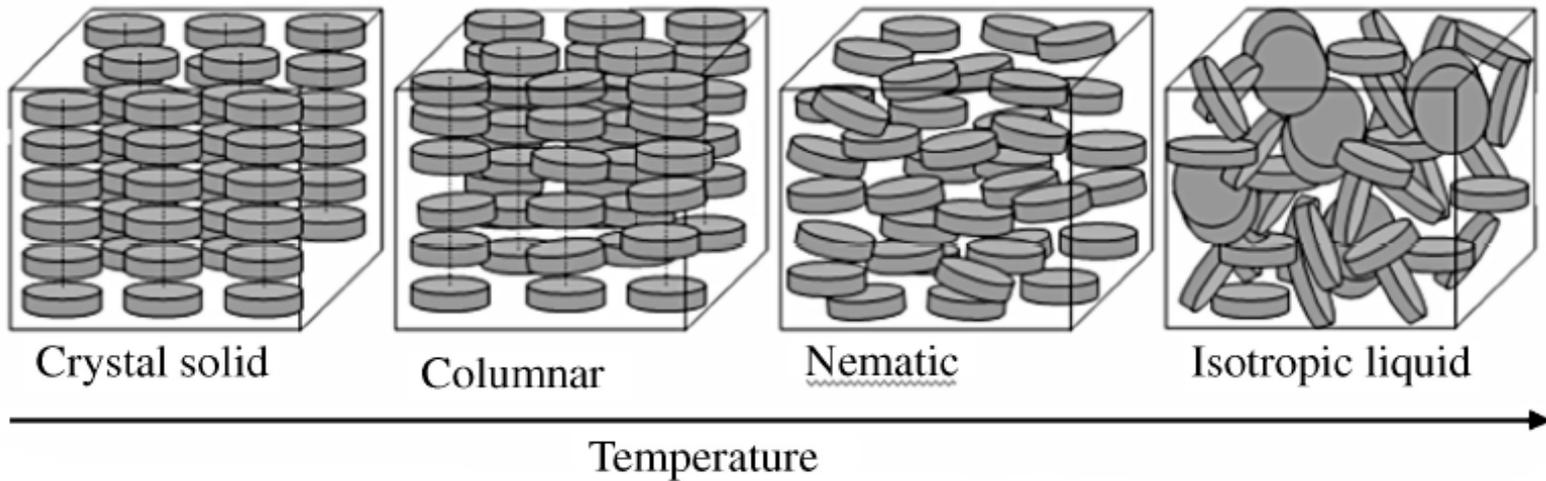
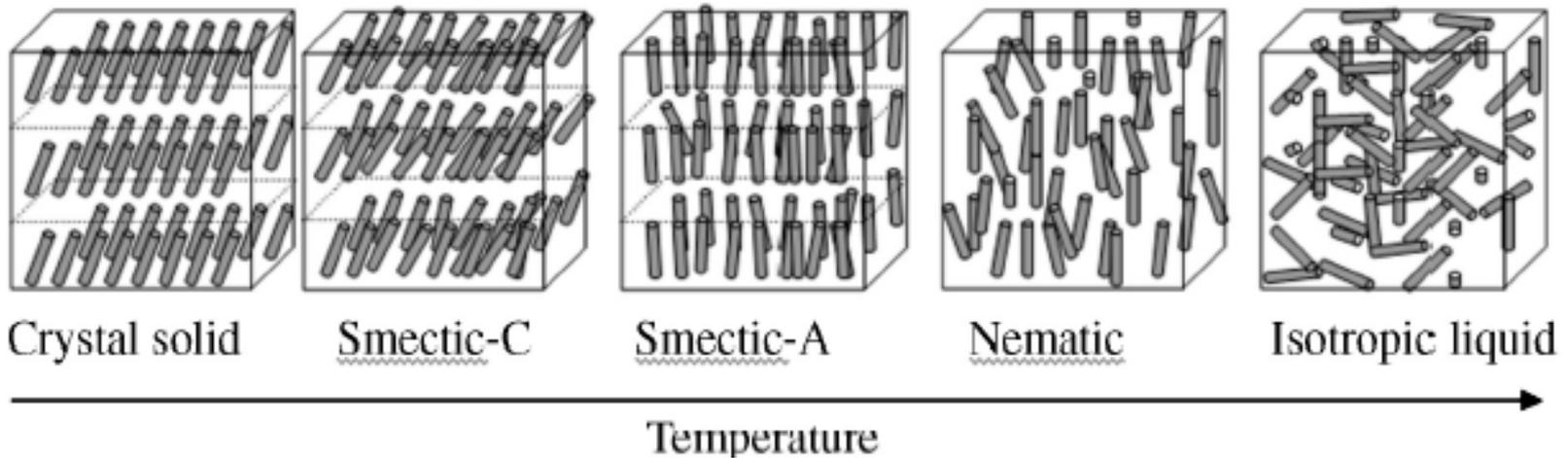


Liquid Crystals (disk like)

- Rigid core and flexible tails.
- The branches are approximately on one plane.
- There is no permanent dipole moment perpendicular to the plane of the molecule



Liquid Crystal Physics



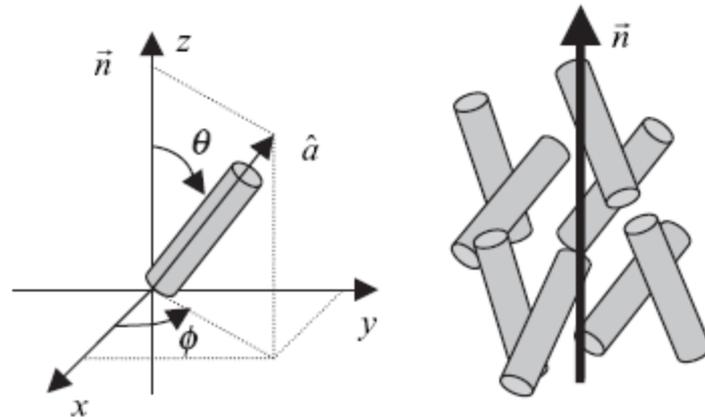
Orientational Order

The average directions of the molecular axes are along a common direction: namely, the liquid crystal **director**, \hat{n} .

The orientation of individual molecules, \hat{a} , is specified by the polar angle ϕ and the azimuthal angle θ where the z axis is chosen parallel to \hat{n} .

In general the orientational order of \hat{a} is specified by an orientational distribution function: $g(\theta, \phi)$

$g(\theta, \phi)d\Omega$ probability that \hat{a} is oriented along the direction specified by θ and ϕ within the solid angle $d\Omega$.

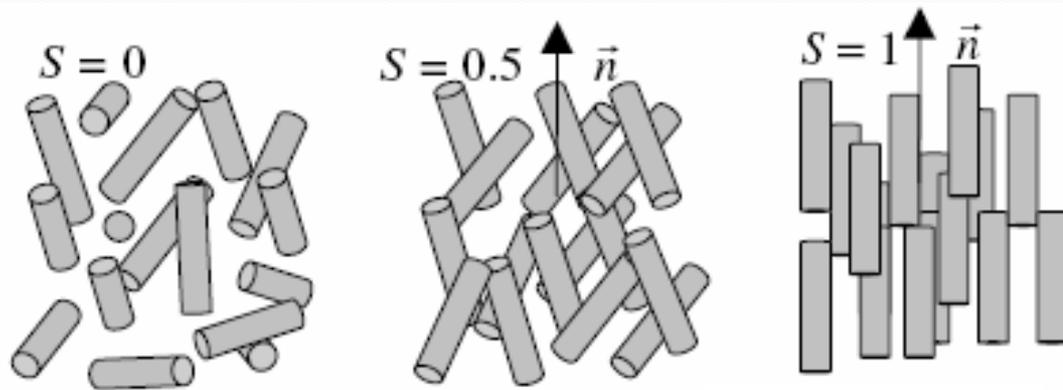


Order Parameter

- Definition of the order parameter: $S = \langle P_2(\cos\theta) \rangle = \left\langle \frac{3 \cos^2 \theta - 1}{2} \right\rangle$

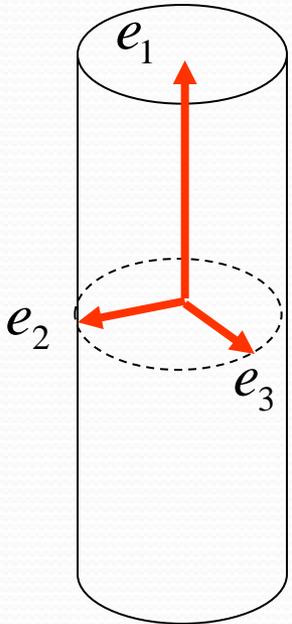
- Order parameter tensor is defined as follows: $Q_{ij} = \left\langle \frac{3n_i n_j - \delta_{ij}}{2} \right\rangle$

The largest eigenvalue of Q gives S and the corresponding eigenvector determines the director.



Orientalational Order

Uniaxial ordering

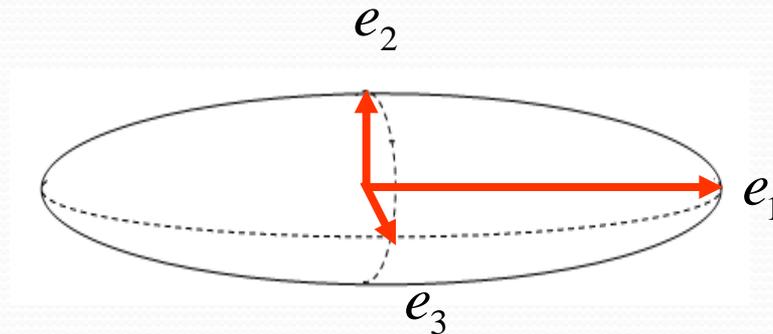


$$\lambda_1 = \frac{2}{3}S \quad , \quad \lambda_2 = -\frac{1}{3}S \quad , \quad \lambda_3 = -\frac{1}{3}S$$

Nematics are uniaxial in the bulk.
The wetting layer may exhibit *biaxiality* due to the lower symmetry near the surface.

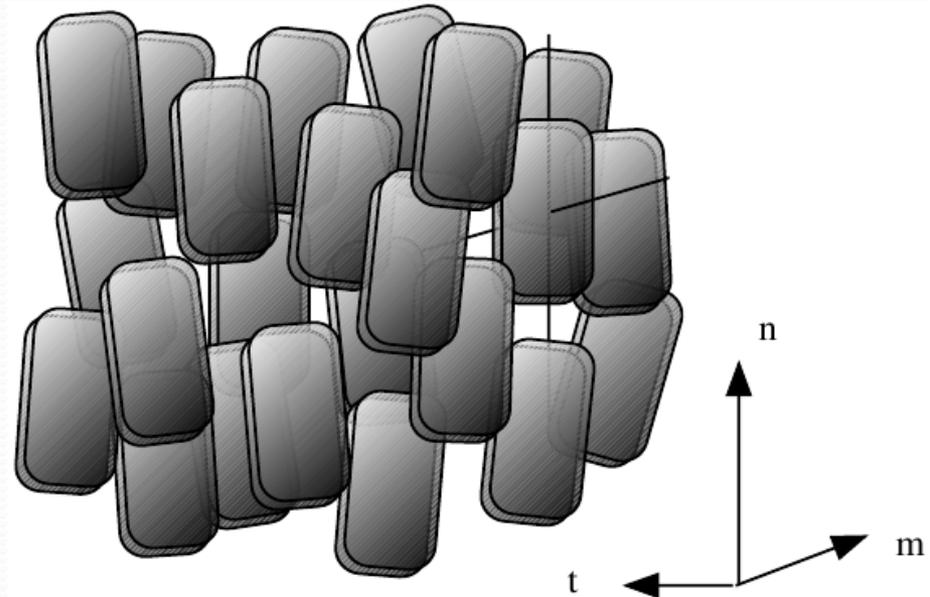
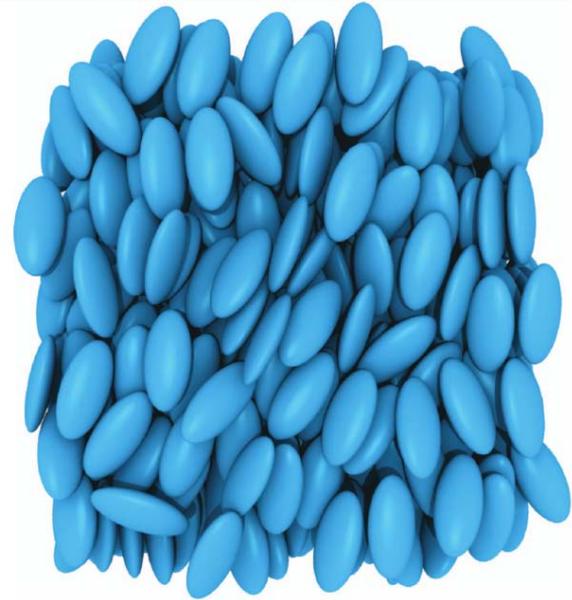
T. J. Sluckin and A. Poniewierski, *Phys. Rev. Lett.*, **55** 2907(1985).

Biaxial ordering



$$\lambda_1 = \frac{2}{3}S \quad , \quad \lambda_2 = -\frac{1}{3}S(1+B) \quad , \quad \lambda_3 = -\frac{1}{3}S(1-B) \quad , \quad 0 \leq B \leq 1$$

Biaxial nematic phase



R. Berardi, J. S. Linturuori, M. R. Wilson, C. Zannoni, J. Chem. Phys. (2011)
M. Kleman, O. Lavrentovich, Soft Matter Physics An Introduction (2003)

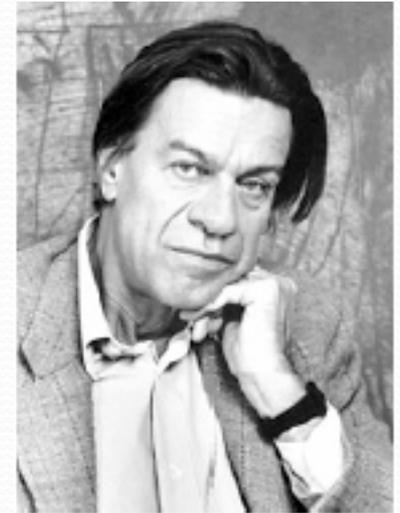
Isotropic – Nematic transition

Landau-de Gennes theory

- De Gennes extended Landau's theory to the isotropic–nematic transition because it is a weak first-order transition.
- The free energy density f of the material can be expressed in terms of the order parameter S as

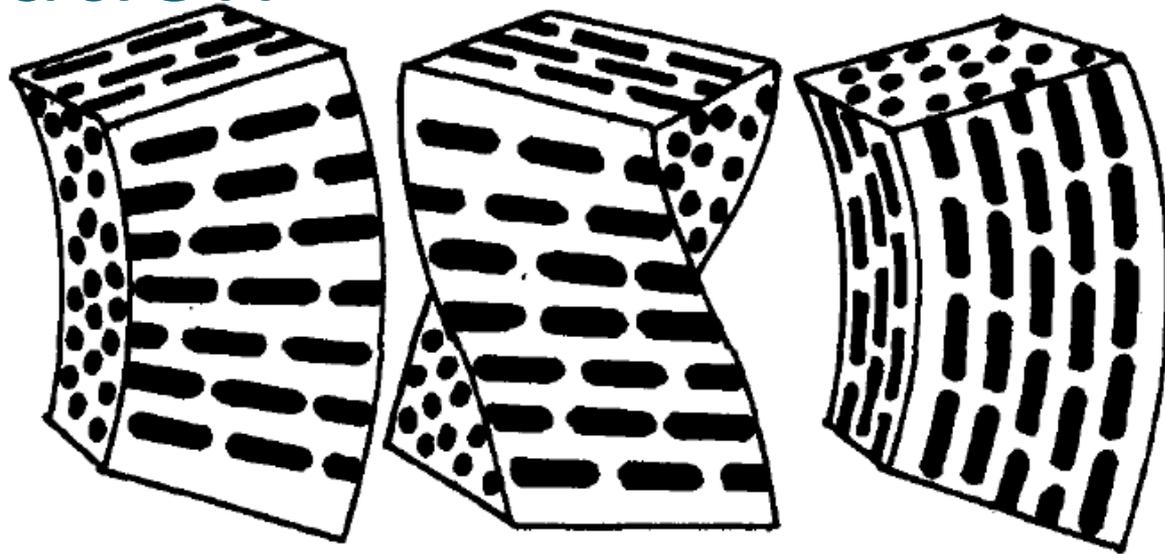
$$f = \frac{1}{2}a(T - T^*)S^2 - \frac{1}{3}bS^3 + \frac{1}{4}cS^4$$

$$F_{LdG}[Q] = \int_{\Omega} \left\{ \frac{1}{2}a(T - T^*)\text{Tr}[Q \cdot Q] - \frac{1}{3}B\text{Tr}[Q \cdot Q \cdot Q] + \frac{1}{4}C(\text{Tr}[Q \cdot Q])^2 \right\} dV$$



De Gennes

Deformation

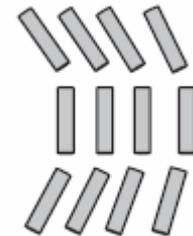
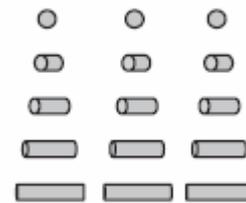
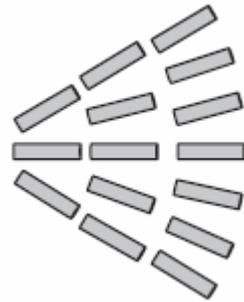


splay

twist

bend

Elasticity



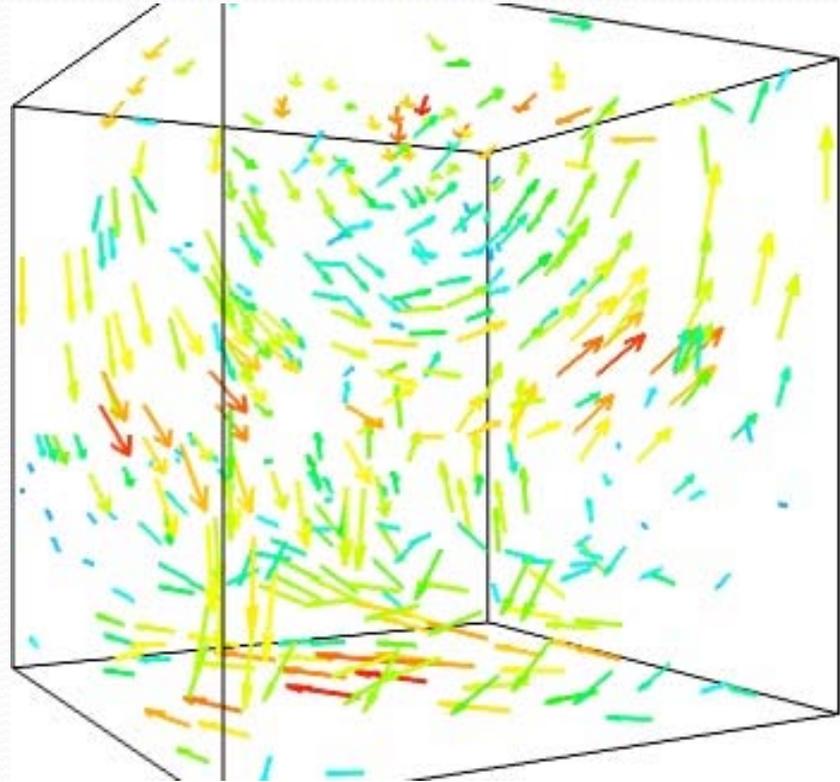
Elastic Energy

$$f_{Elastic} = \frac{1}{2} K_{splay} (\vec{\nabla} \cdot \hat{n})^2 + \frac{1}{2} K_{twist} (\hat{n} \cdot \vec{\nabla} \times \hat{n})^2 + \frac{1}{2} K_{bend} (\hat{n} \times \vec{\nabla} \times \hat{n})^2$$

P.G. de Gennes and J. Prost, *The Physics of Liquid Crystals*, 2nd ed. (Oxford University Press, Oxford, 1993).

Boundary condition effect

Defects



Defects

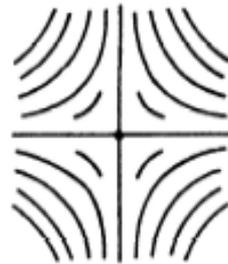
$$\theta(x, y) = s \tan^{-1}\left(\frac{y}{x}\right) + c$$



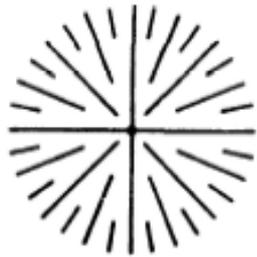
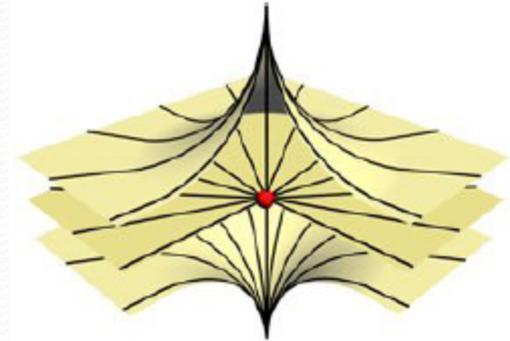
$s = \frac{1}{2}$



$s = -\frac{1}{2}$



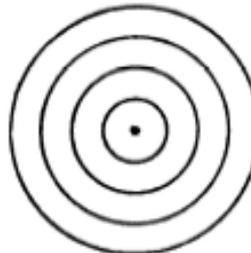
$s = -1$



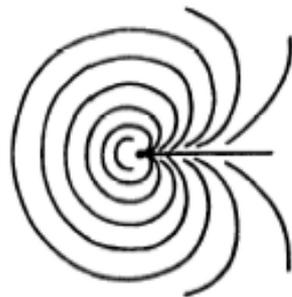
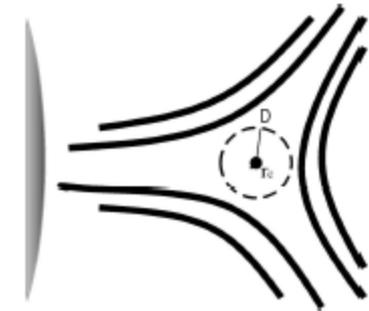
$s = 1, c = 0$



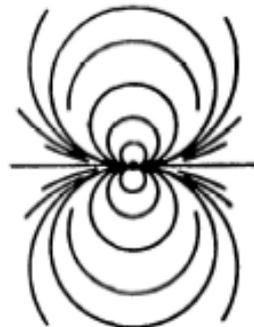
$s = 1, c = \pi/4$



$s = 1, c = \pi/2$



$s = 3/2$



$s = 2$

$$\theta_1(x, y) = s_1 \tan^{-1}\left(\frac{y}{x}\right) + c_1$$

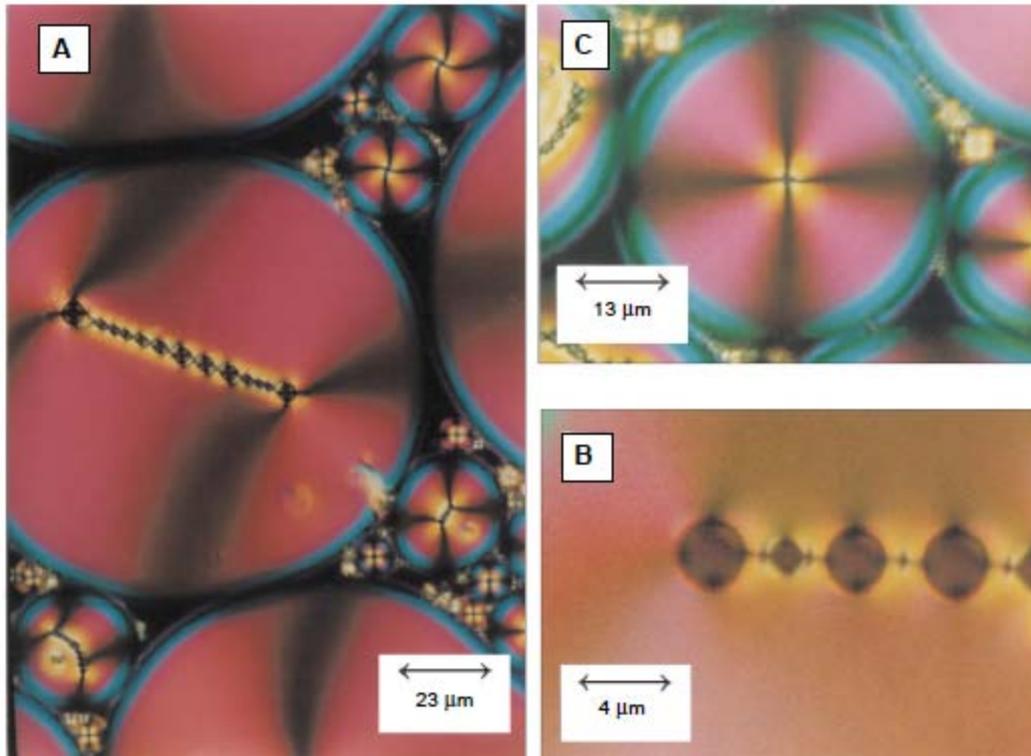
$$\theta_2(x, y) = s_2 \tan^{-1}\left(\frac{y}{x}\right) + c_2$$

$$\theta = \theta_1 + \theta_2$$

Defects

The control of the anchoring is achieved experimentally by using various amphiphilic compounds which are adsorbed at the water-liquid-crystal interface. Molecular **surfactants** are used to induce strong normal anchoring, while a **polymer** is used to induce strong planar anchoring.

P. Poulin, and D. A. Weitz, *Phys. Rev. E* 57, 626 (1998).



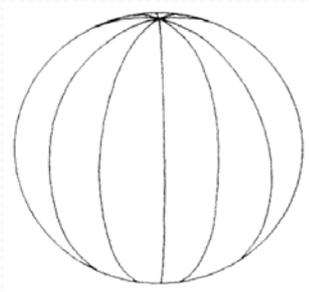
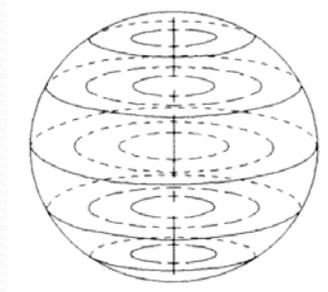
Philippe Poulin, Holger Stark,
T. C. Lubensky, D. A. Weitz,
Science 75, 1770 (1997)

Colloidal droplets in nematic medium

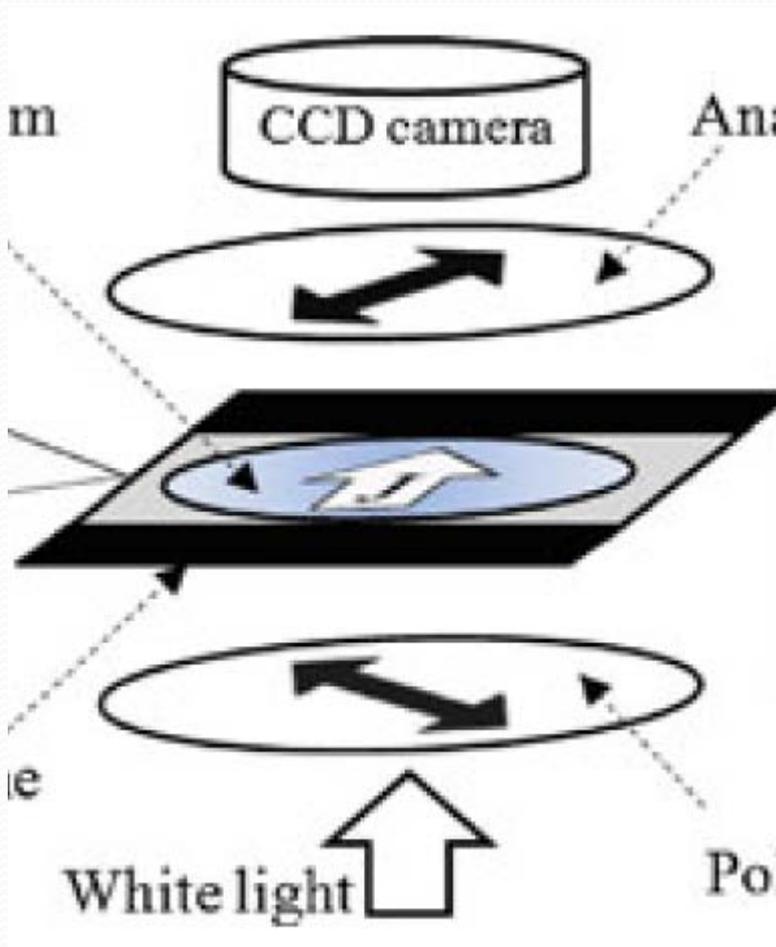
The alignment of a nematic liquid crystal by a **bounding interface** is of considerable interest both for fundamental and technological reasons.

- **homeotropic** anchoring, where the preferred, or “easy”, average orientation corresponds to \mathbf{n} normal to the interface.
- **planar** anchoring, where the preferred average orientation corresponds to \mathbf{n} lying in one particular direction parallel to the interface
- **planar degenerate** anchoring, where all the planar orientations for \mathbf{n} are equivalent easy directions.

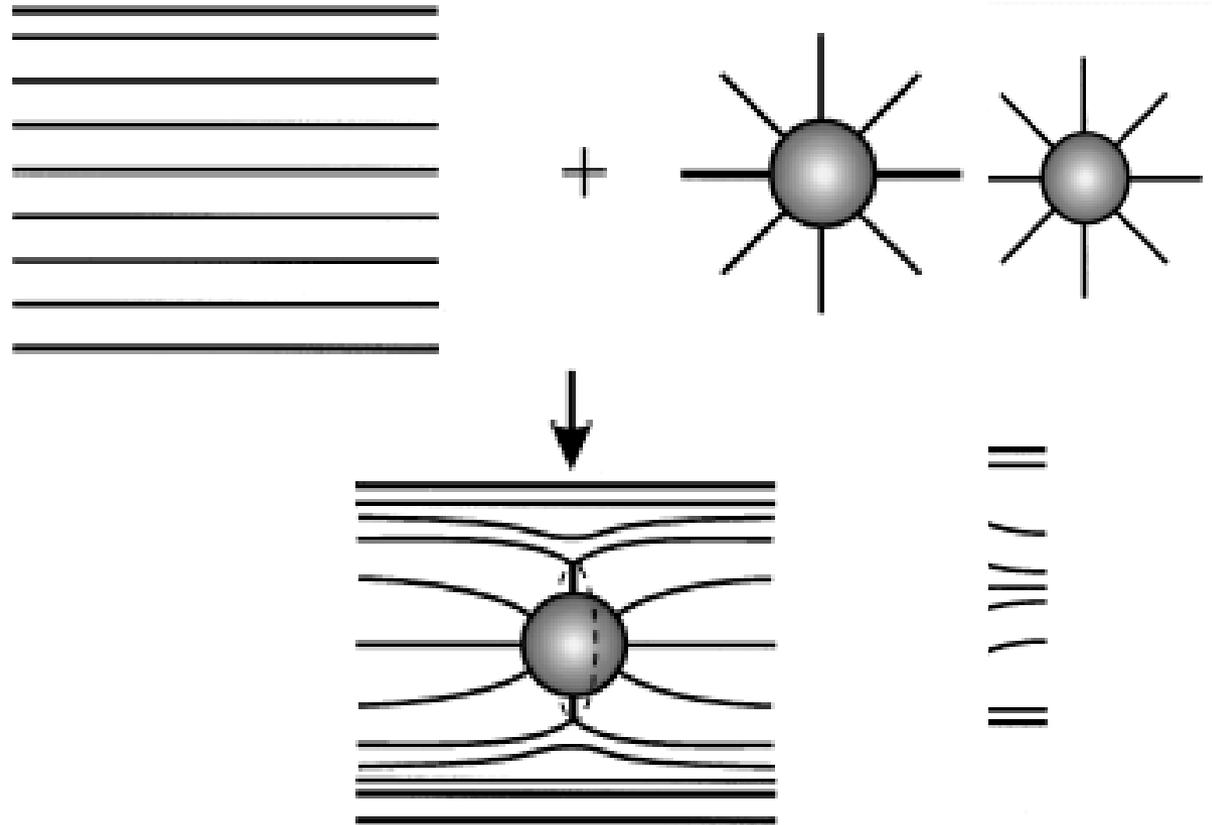
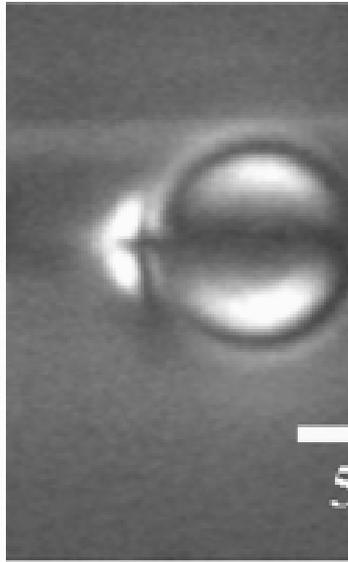
Planar anchoring on sphere



How to observe

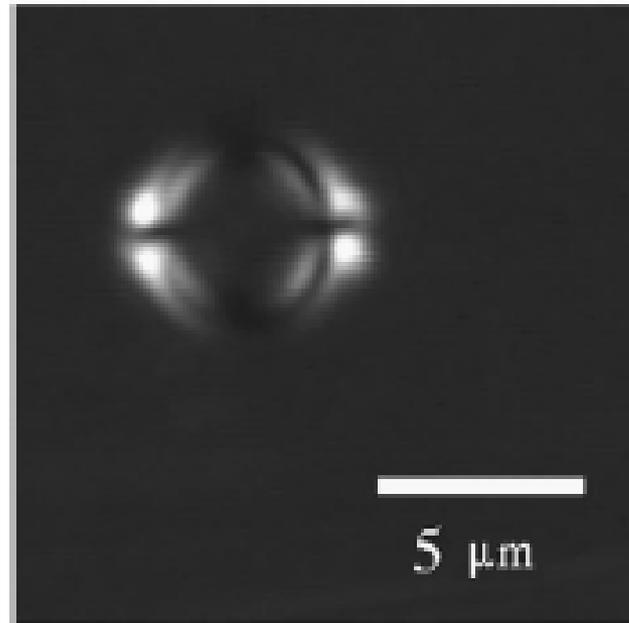
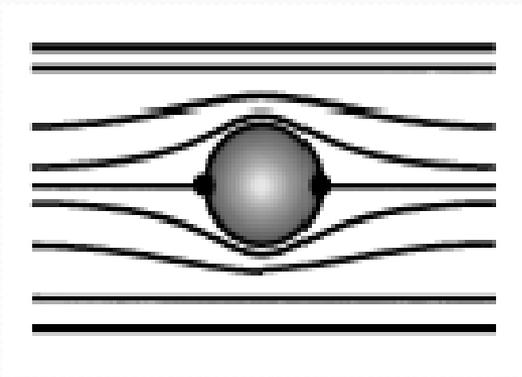


Colloids in Nematic



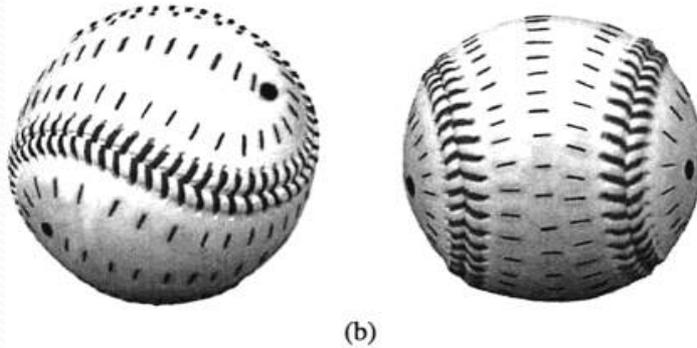
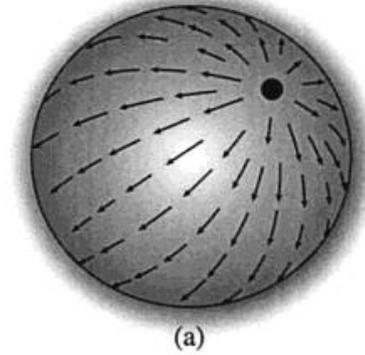
Poulin & Weitz, PRE 1998

Colloids in Nematic



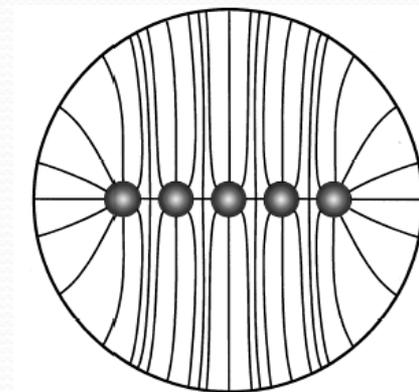
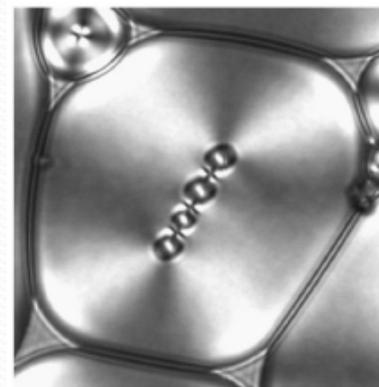
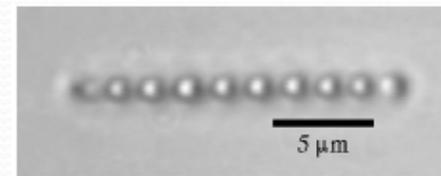
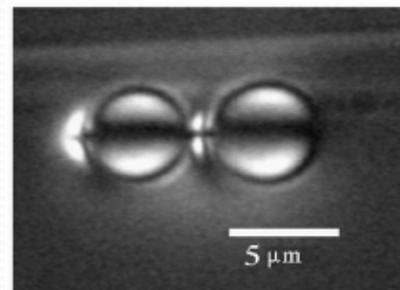
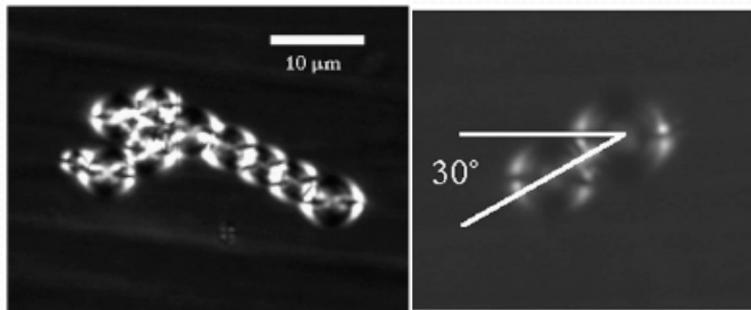
Poulin & Weitz, PRE 1998

Quadrapolar configurations

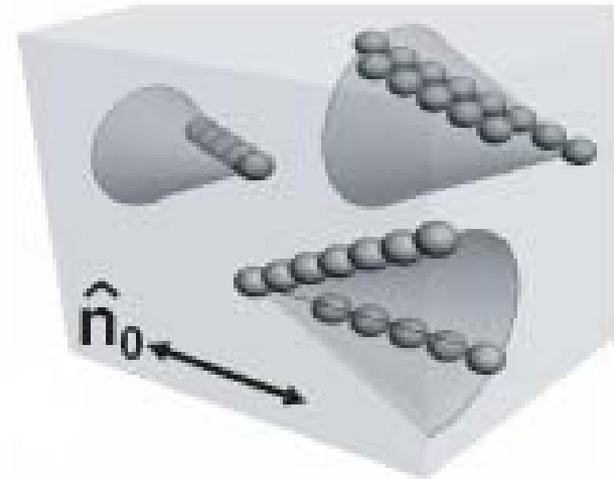
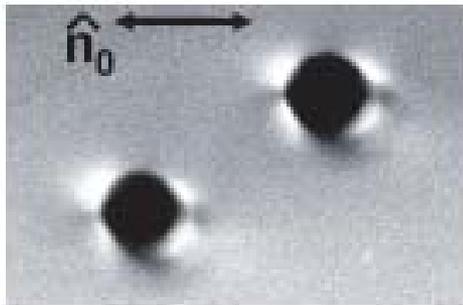
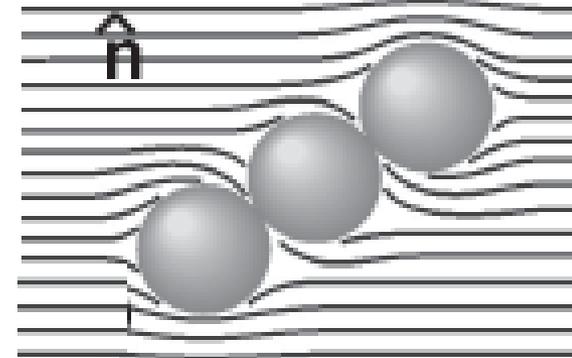
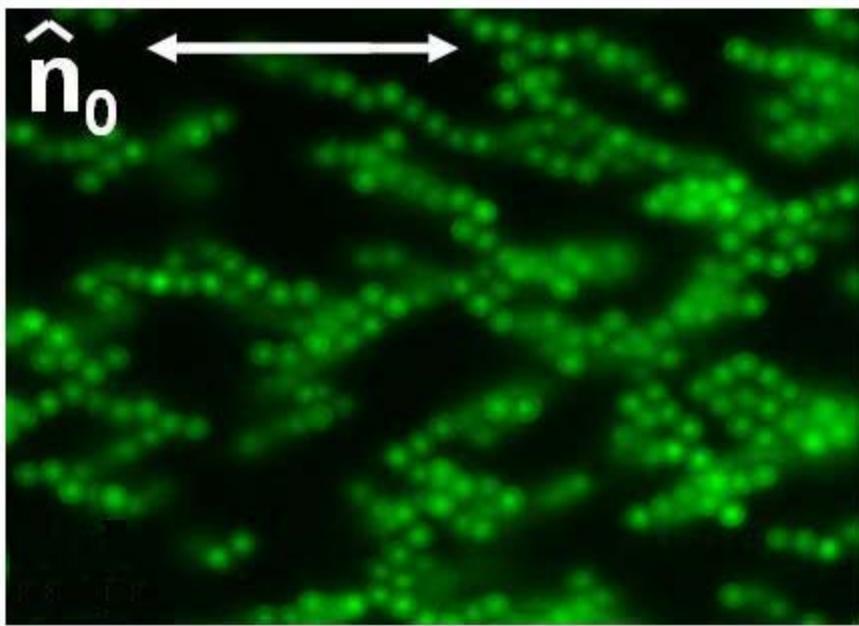


Nano Letters, Vol.2, No.10 ,1125-1129 (2002)

Aggregations



Poulin & Weitz, PRE 1998



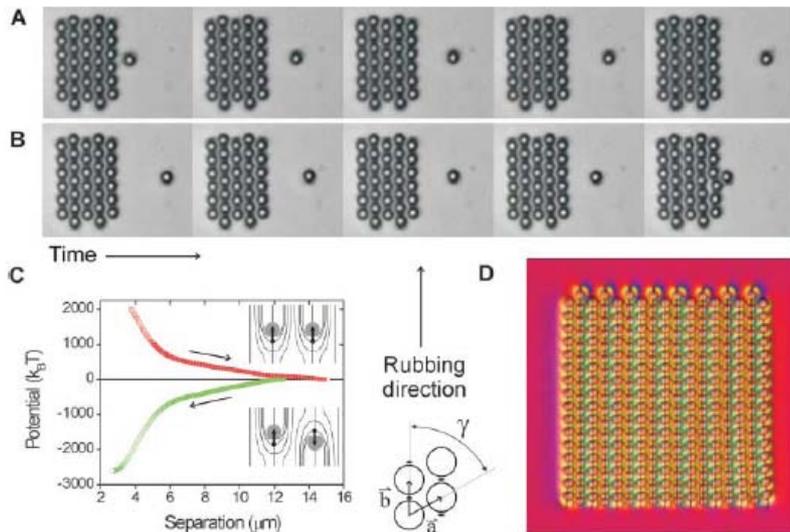
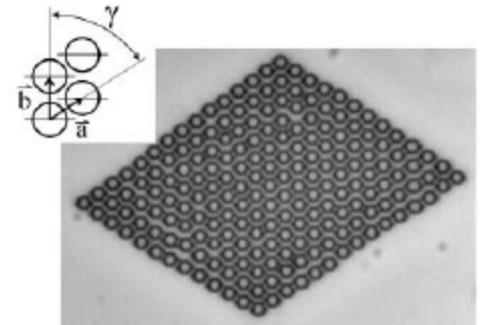
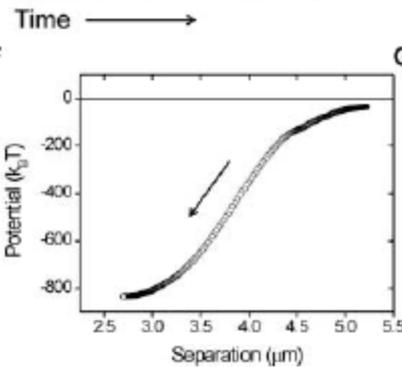
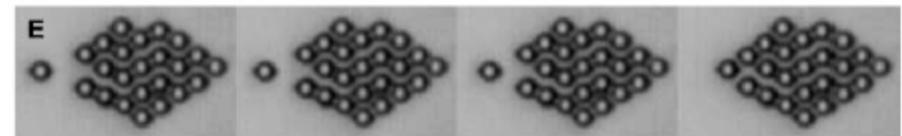
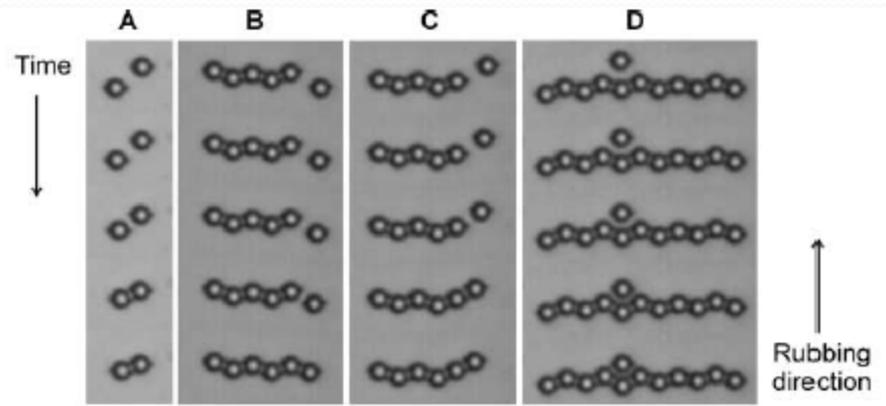
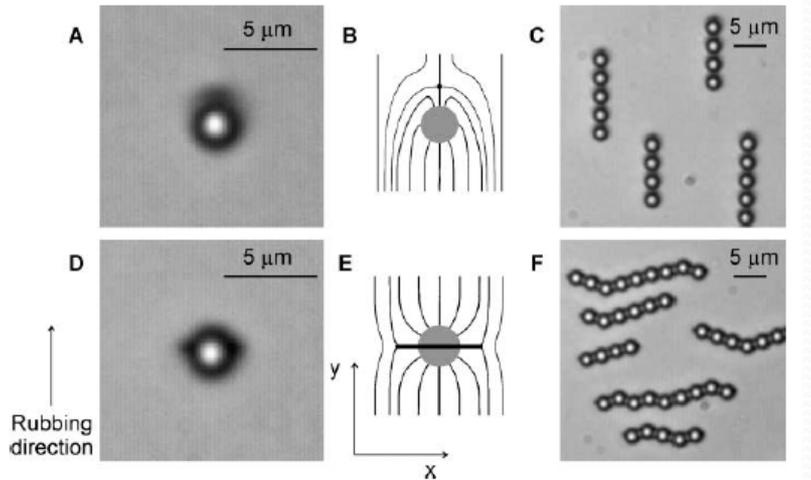
fluorescence confocal polarizing microscopy (FCPM)
to characterize the director distortions around the
particles and *optical trapping with laser tweezers*
to measure the pair interaction force

I. I. Smalyukh, *et al.*,
PRL 95, 157801 (2005)



Two-Dimensional Nematic Colloidal Crystals Self-Assembled by Topological Defects

Igor Musevic, *et al.*
Science 313, 954 (2006);
 DOI: 10.1126/science.1129660



2D Interactions and Binary Crystals of Dipolar and Quadrupolar Nematic Colloids

U. Ognysta, A. Nych, and V. Nazarenko

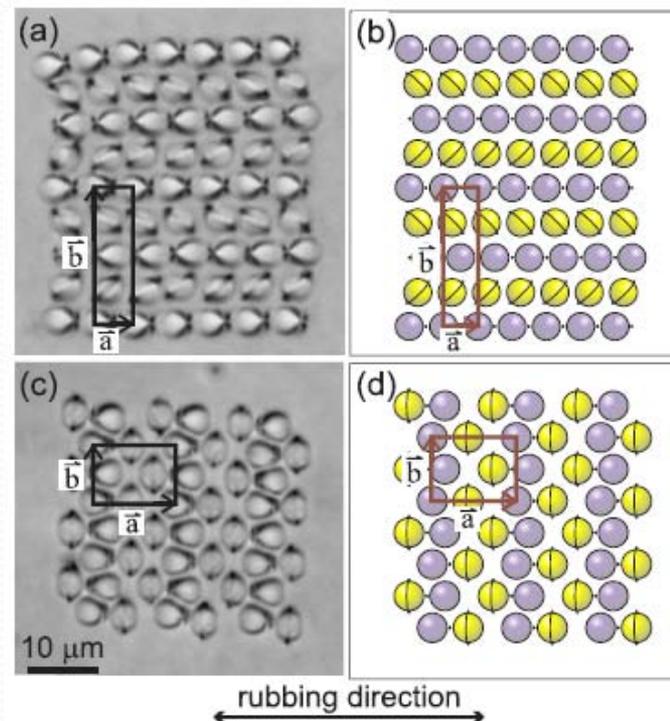
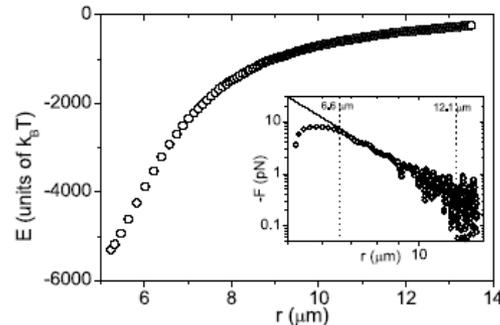
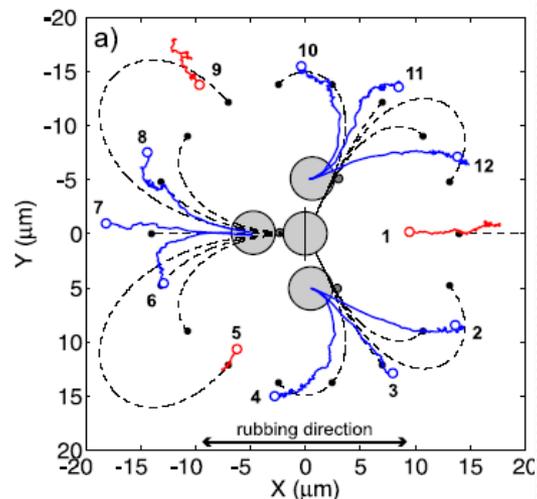
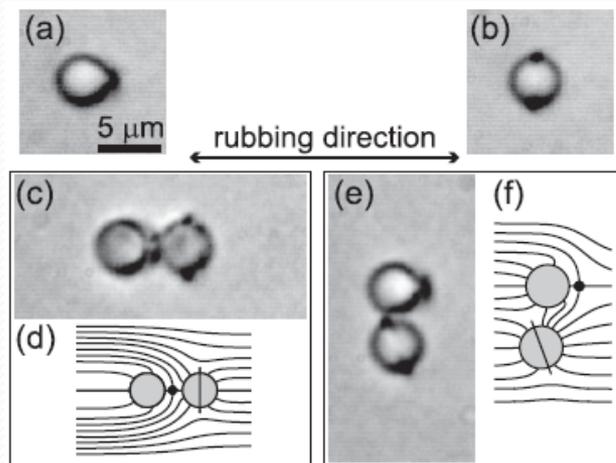
Institute of Physics, 46 Nauky avenue, Kyiv 680028, Ukraine

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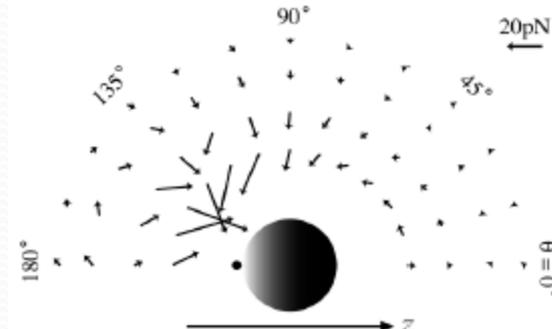
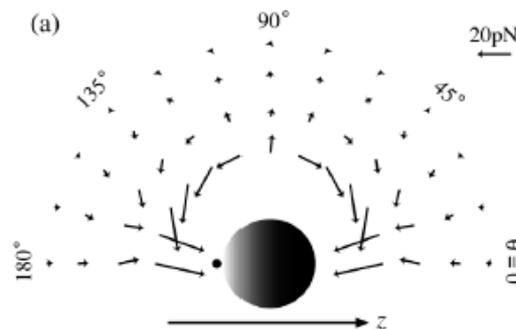
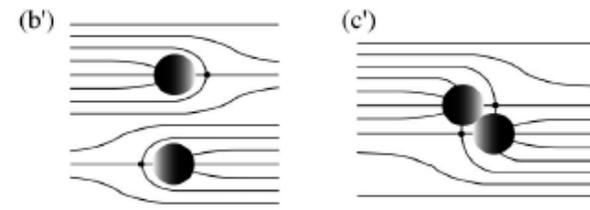
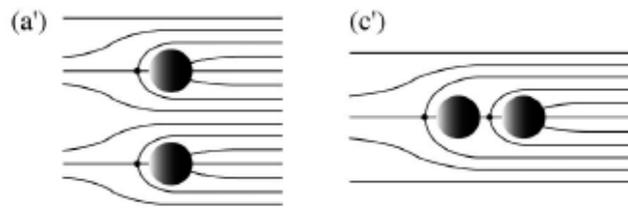
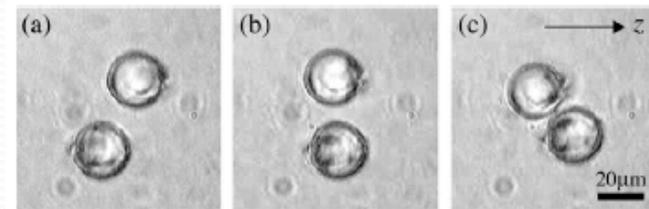
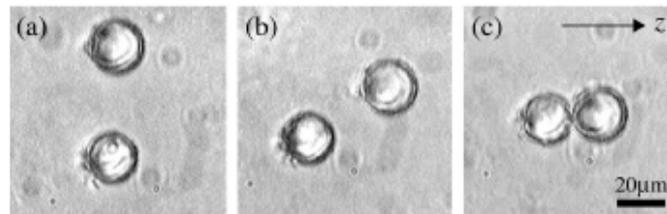
Direct Observation of Anisotropic Interparticle Forces in Nematic Colloids with Optical Tweezers

Makoto Yada,^{1,*} Jun Yamamoto,¹ and Hiroshi Yokoyama^{1,2}

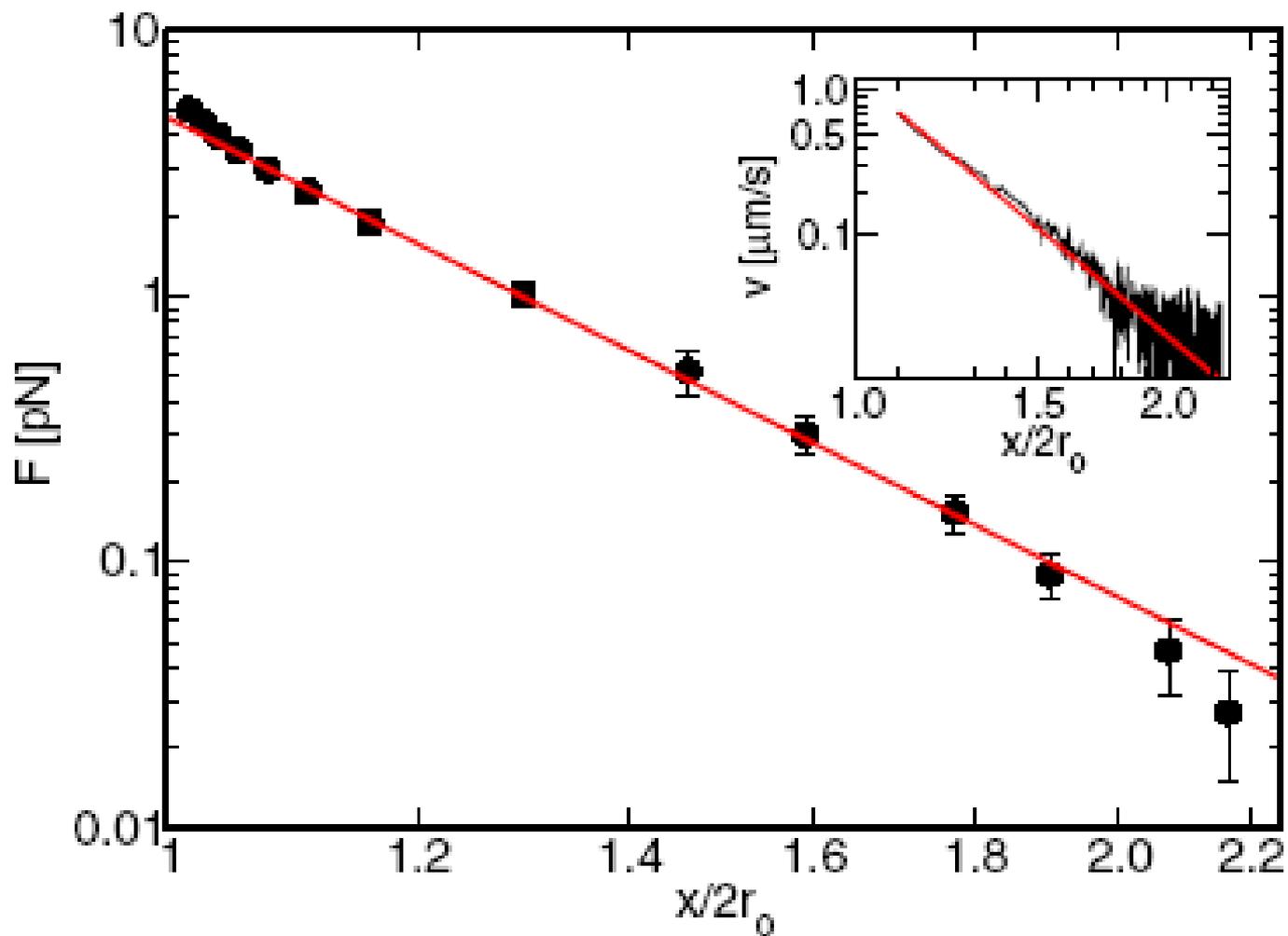
¹*Yokoyama Nano-structured Liquid Crystal Project, ERATO, Japan Science and Technology Corporation, 5-9-9 Tokodai, Tsukuba, Ibaraki, 300-2635, Japan*

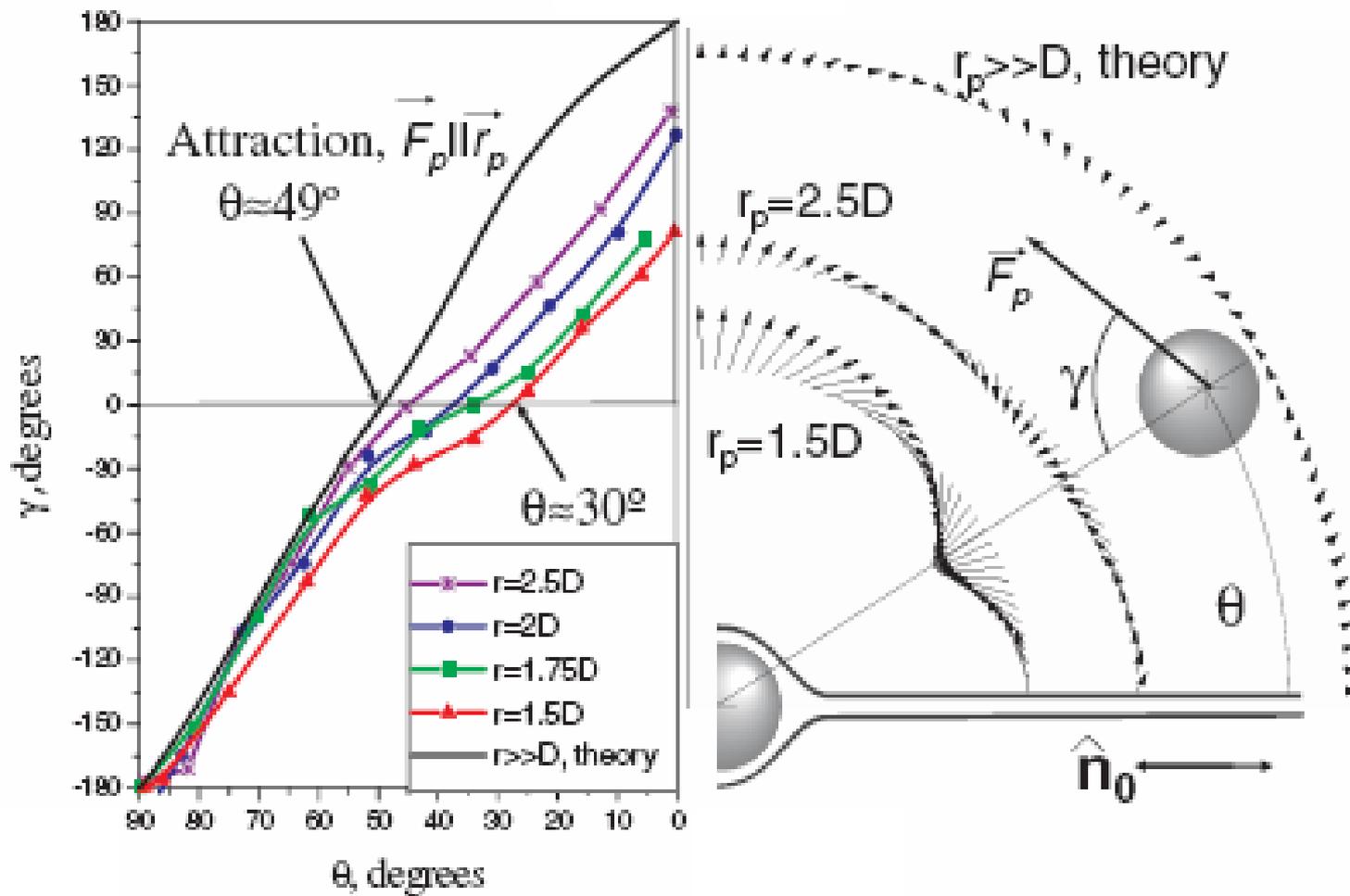
²*Nanotechnology Research Institute, National Institute of Advanced Industrial Science and Technology, 1-1-1 Umezono, Tsukuba, Ibaraki, 305-8568, Japan*

(Received 23 November 2003; published 3 May 2004)



Interparticle Potential and Drag Coefficient in Nematic Colloids

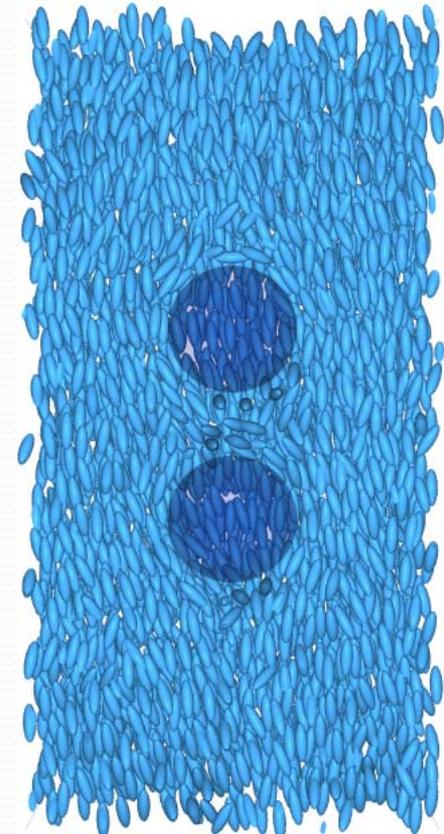
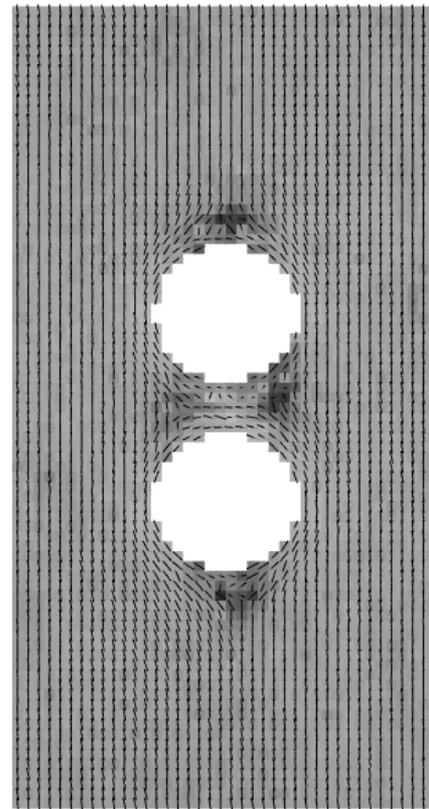




I. I. Smalyukh, *et al.*,
PRL 95, 157801 (2005)

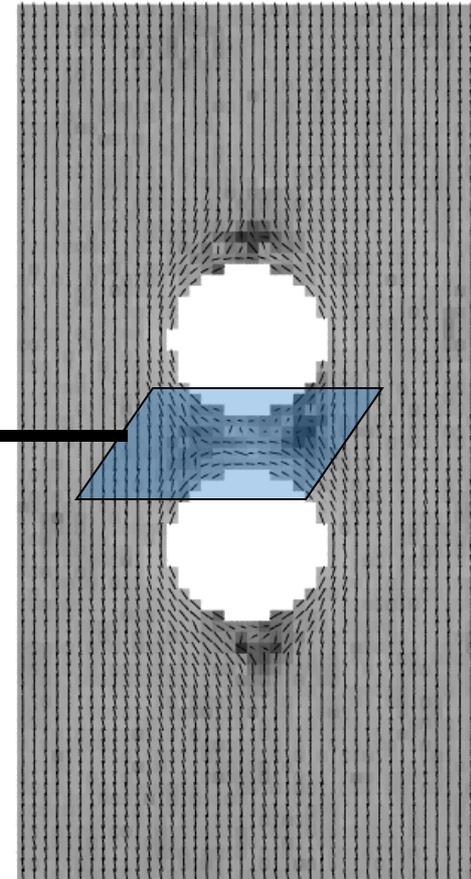
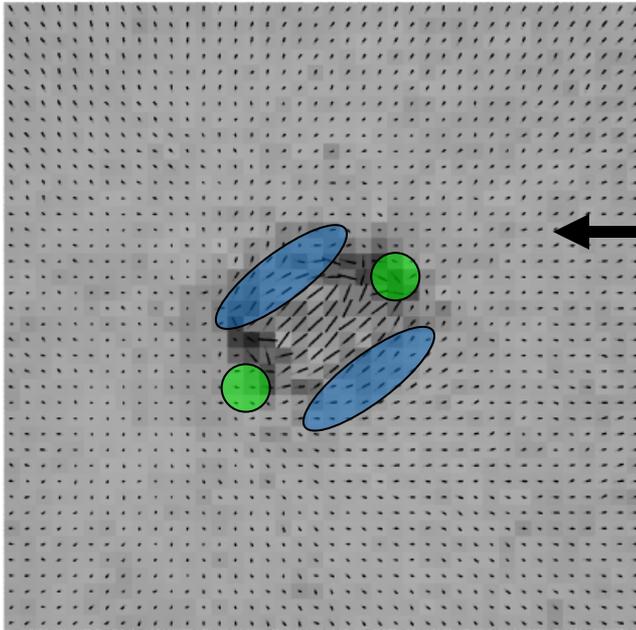
Two colloidal droplets in nematic medium (Parallel)

- Mean force exerted to the droplets along their connecting line is $1.9 \pm 0.3 [\epsilon/\sigma]$
- A spontaneous symmetry breaking mechanism positions the mesogens between the droplets in an orthogonal configuration
- Two boojums appear on the northern pole of the upper and southern pole of the lower droplet
- The nematic director tends to tilt



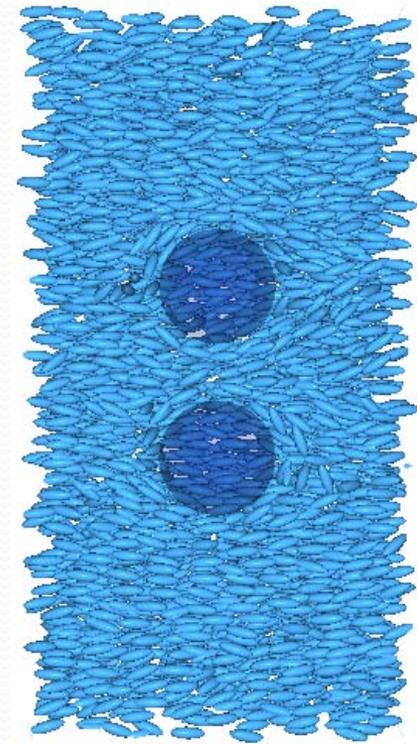
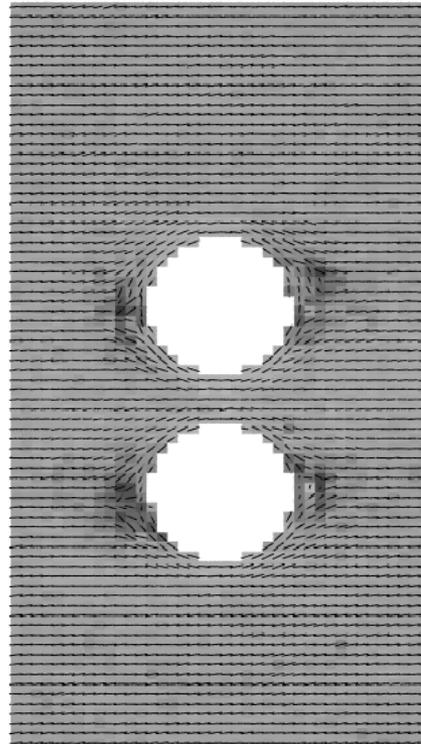
Two colloidal droplets in nematic medium (Parallel)

- In the plane between the droplets, two topological defects and two regions of nematic twist is noticed



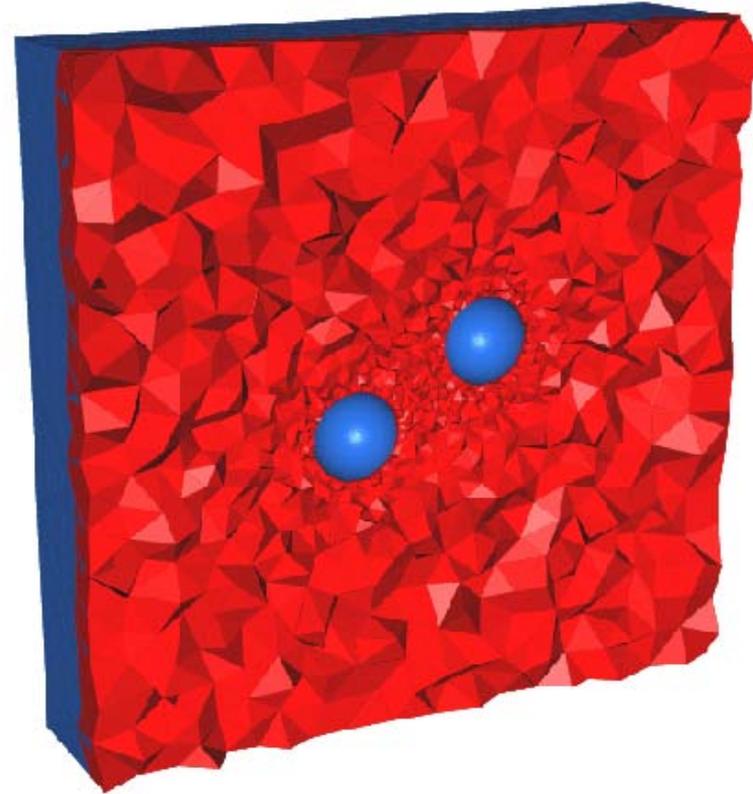
Two colloidal droplets in nematic medium (Perp.)

- Mean force exerted to the droplets along their connecting line was in the order of measurement error
- A boojum appears on each pole of the droplets along the nematic director
- The nematic director tends to tilt



Finite element method

$$\begin{aligned}\hat{F} &= (\hat{F}_{LdG} - f_o V) + \hat{F}_{Elastic} + \hat{F}_{Surface} \\ \hat{F}[q] &= \int_{\Omega} \left\{ \frac{\tau}{2} Tr[q.q] - \frac{\sqrt{6}}{4} Tr[q.q.q] + \frac{1}{4} (Tr[q.q])^2 - f_o \right\} d\hat{V} \\ &+ \frac{1}{2} \left(\frac{\xi}{R} \right)^2 \int_{\Omega} (\hat{\partial}_k q_{ij} \hat{\partial}_k q_{ij}) d\hat{V} \\ &+ \left(\frac{\hat{W}}{R} \right) \int_{\partial\Omega} (\tilde{q}_{ij} - \tilde{q}_{ij}^{\perp})(\tilde{q}_{ij} - \tilde{q}_{ij}^{\perp}) d\hat{S}\end{aligned}$$

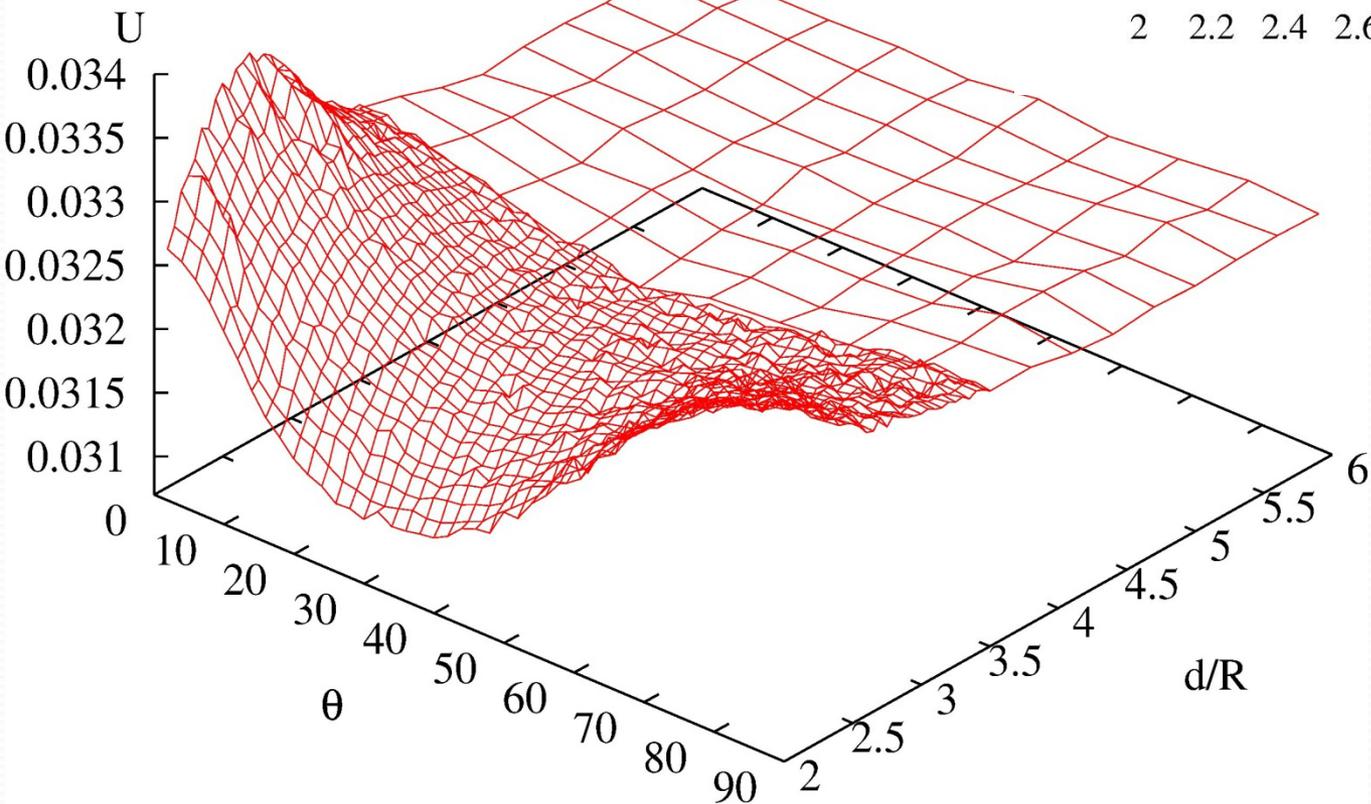
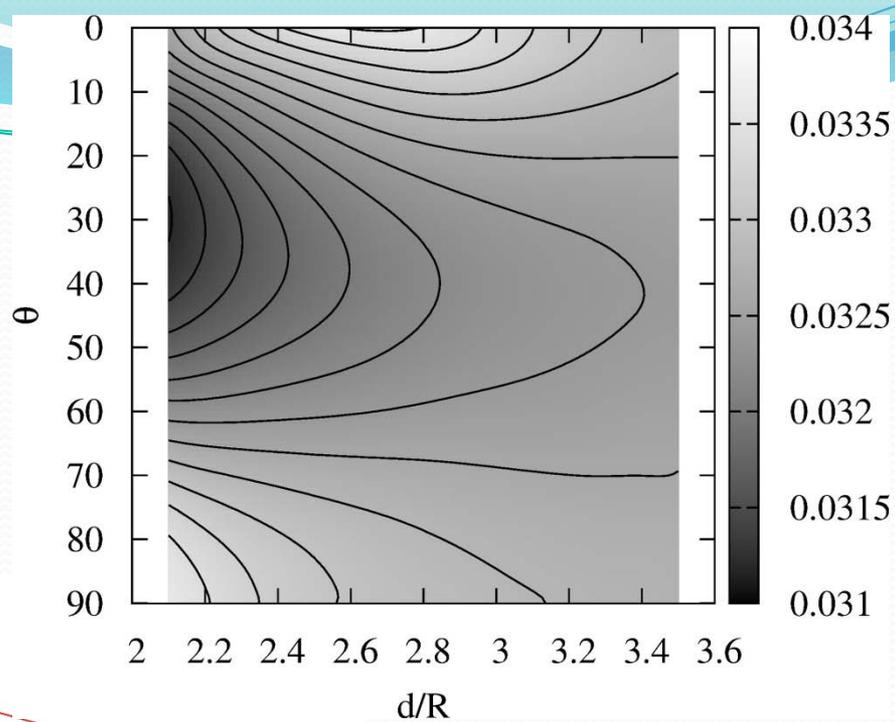


Gmsh mesh generator

Conjugate Gradient minimizing method

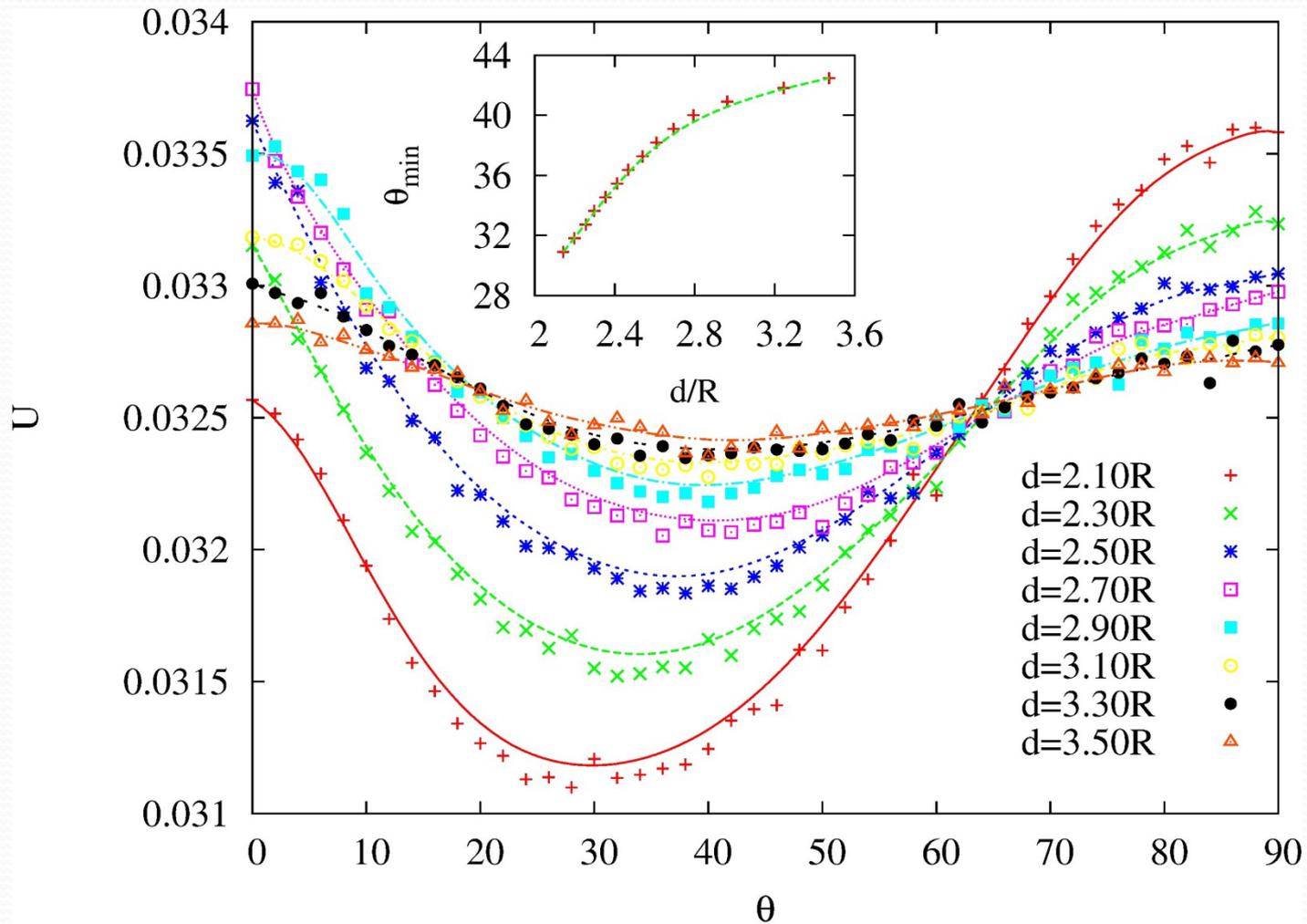
3D calculations

Planar anchoring



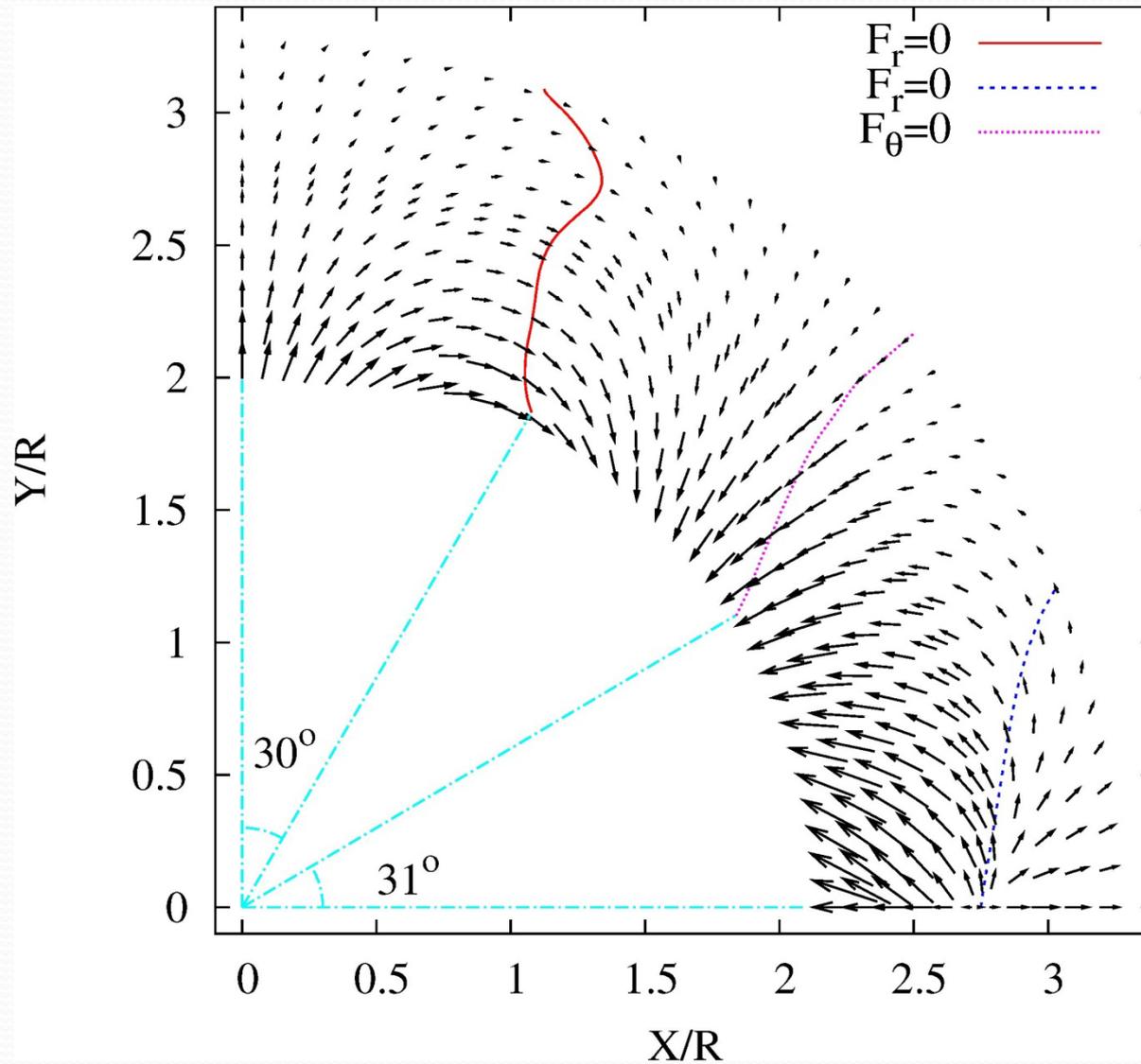
3D calculations

Planar anchoring



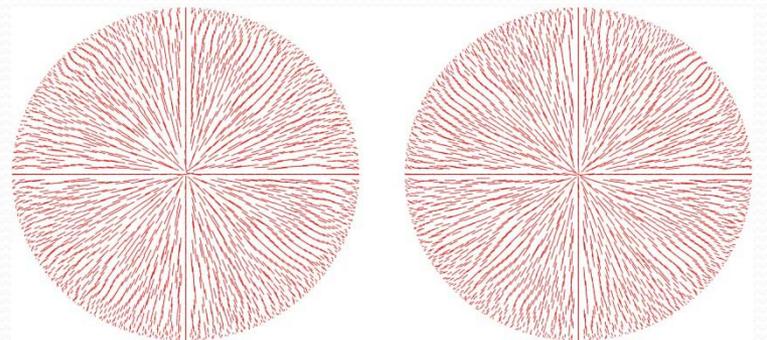
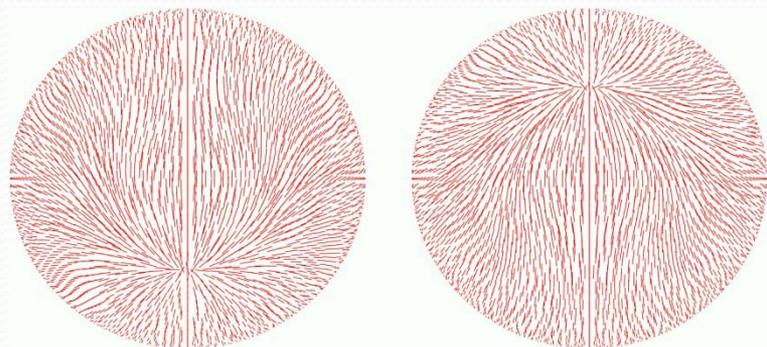
3D calculations

Planar anchoring

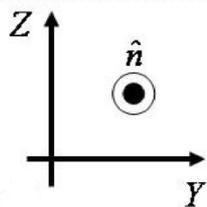


3D calculations

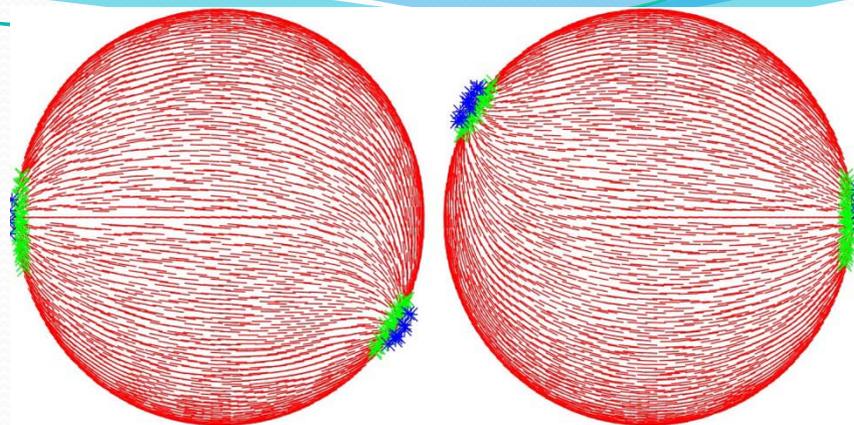
Planar anchoring



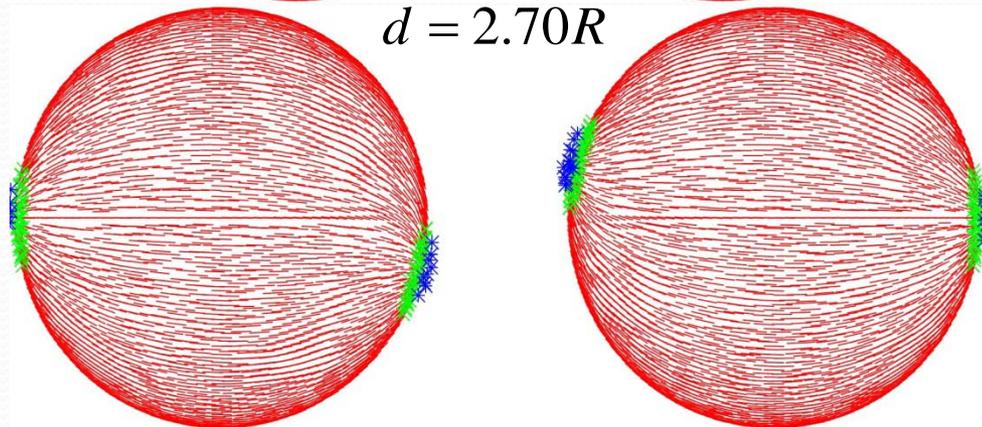
$d = 2.10R, \theta = 0^\circ$



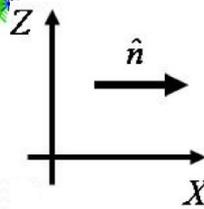
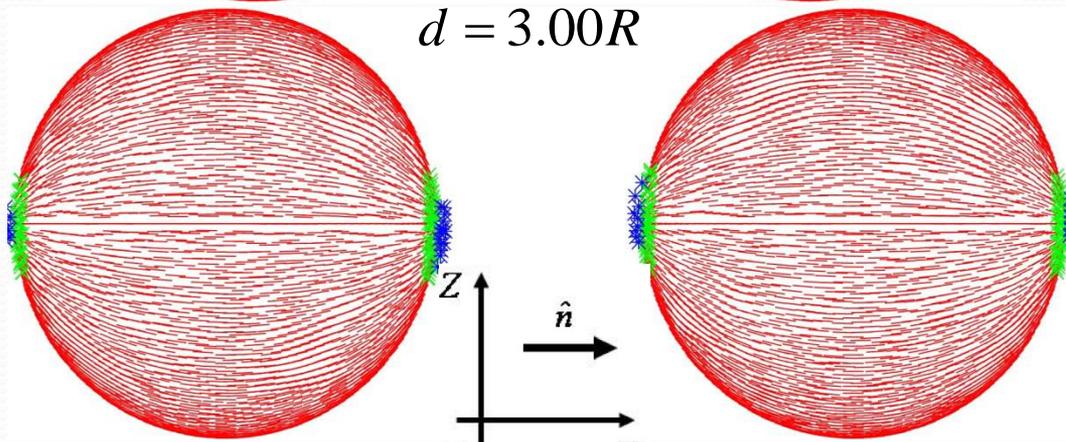
$d = 2.10R$



$d = 2.70R$



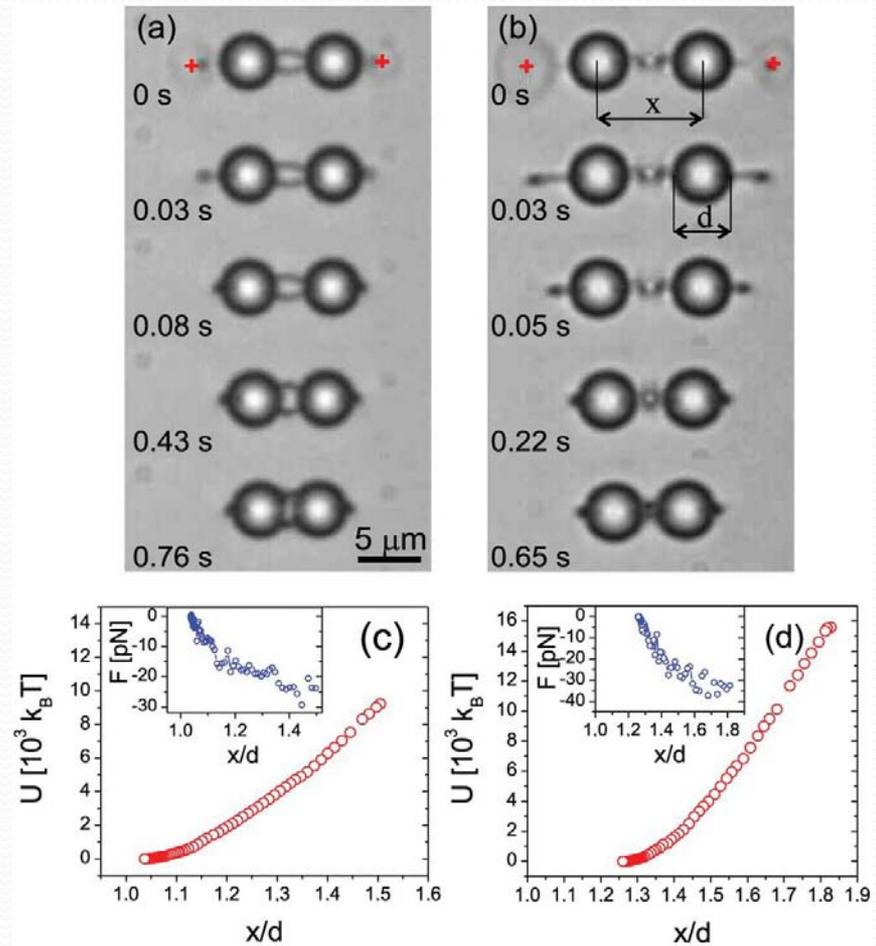
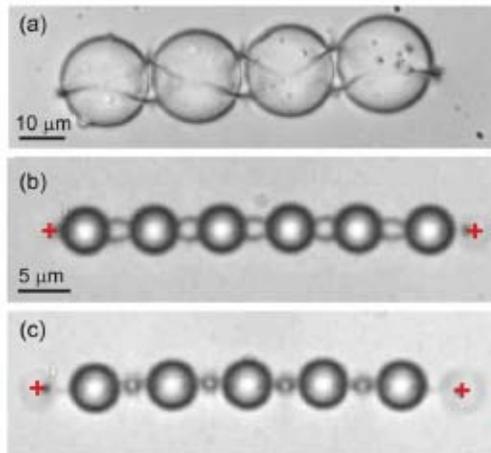
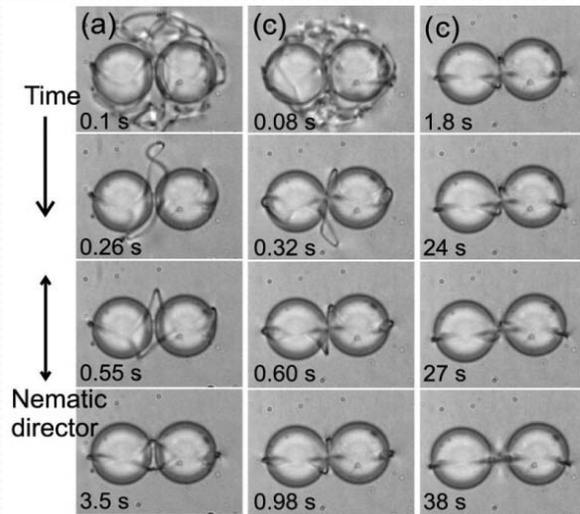
$d = 3.00R$



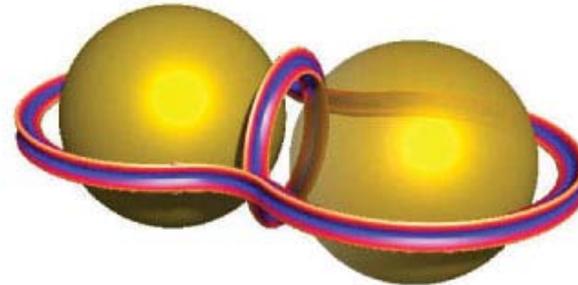
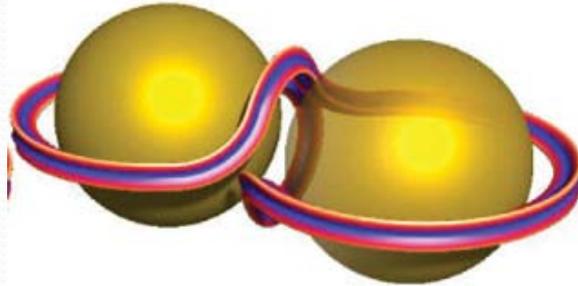


Entangled Nematic Colloidal Dimers and Wires

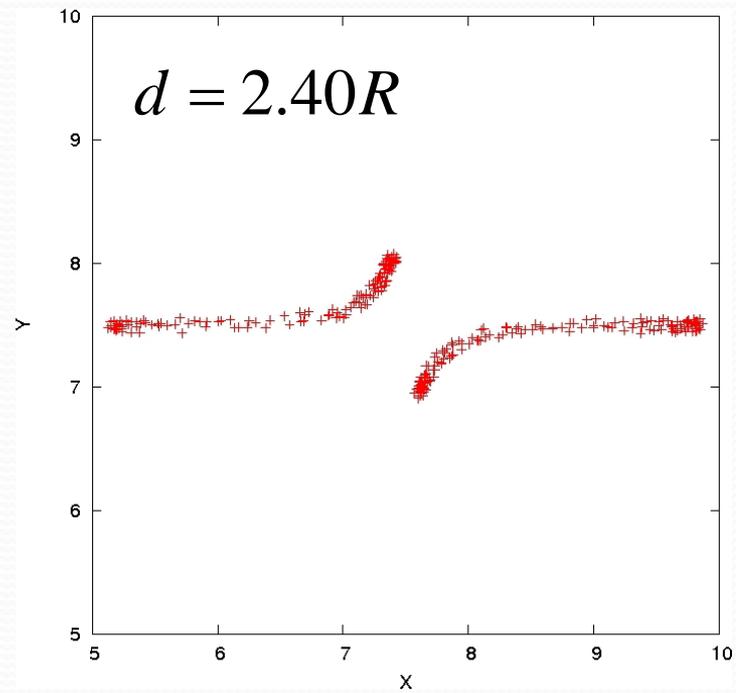
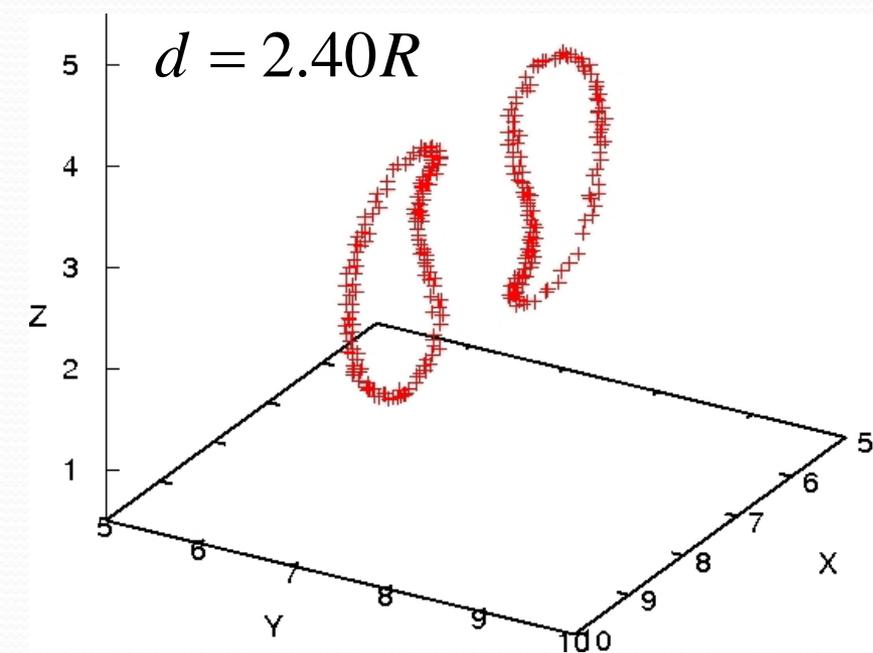
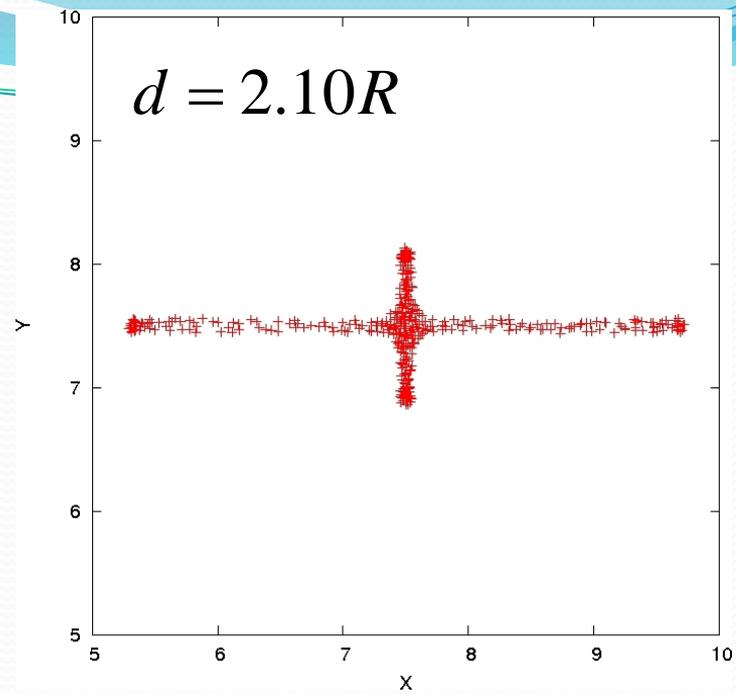
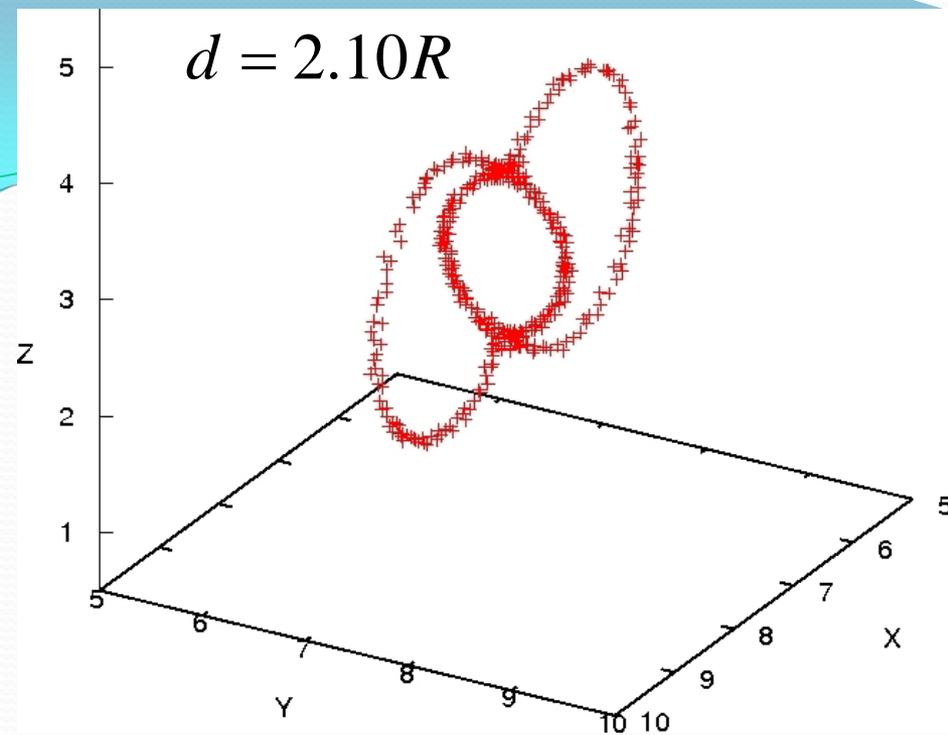
M. Ravnik,¹ M. Škarabot,² S. Žumer,^{1,2} U. Tkalec,² I. Poberaj,¹ D. Babič,¹ N. Osterman,¹ and I. Muševič^{1,2,*}



More Complicated geometries of defects



PRL 106, 177801 (2011)



Science

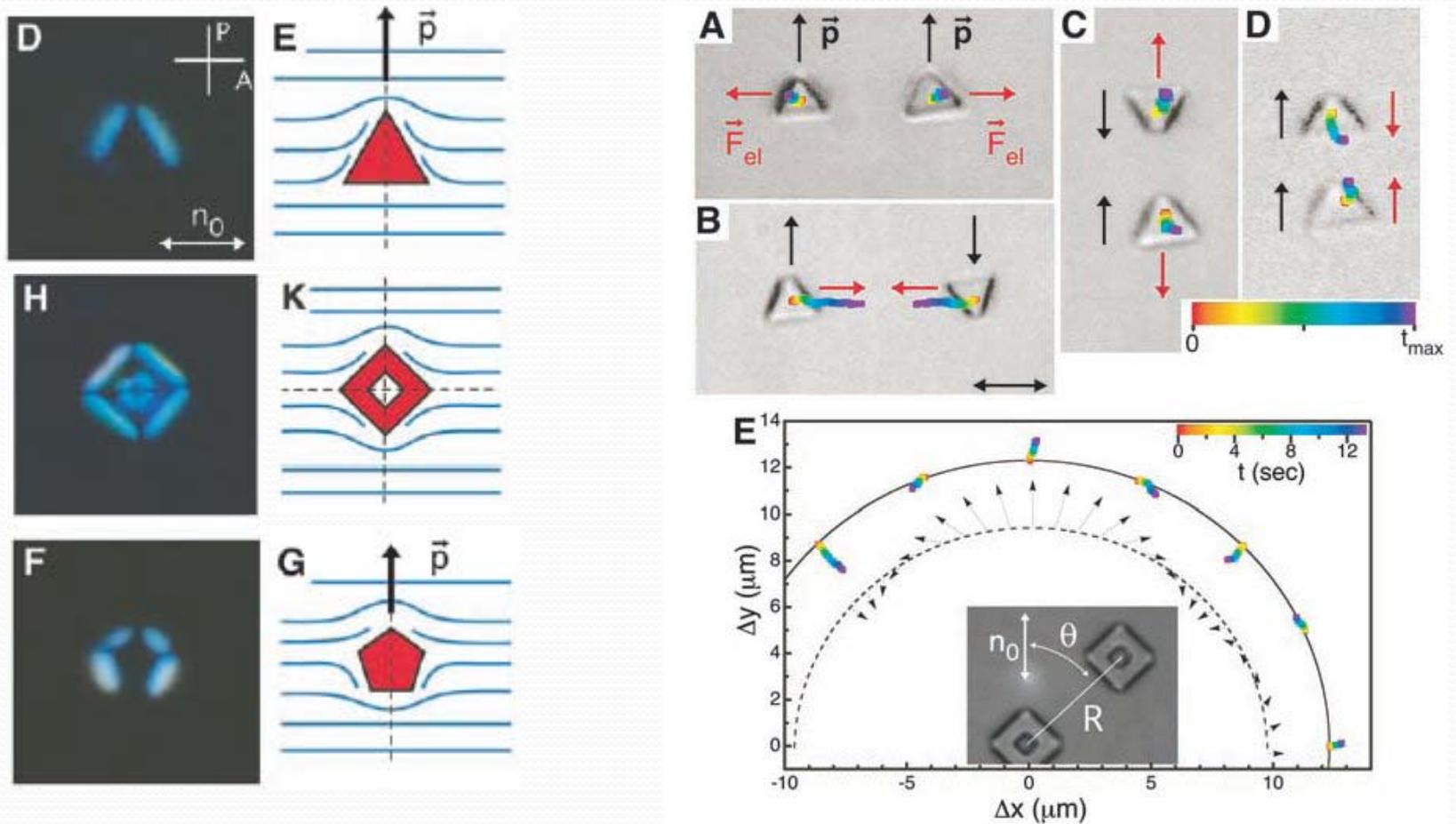
AAAS

Shape-Controlled Colloidal Interactions in Nematic Liquid Crystals

Clayton P. Lapointe, *et al.*

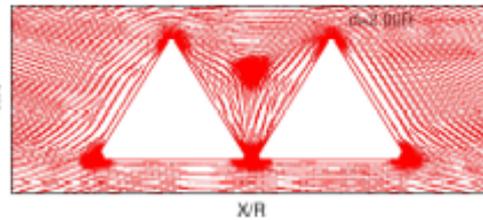
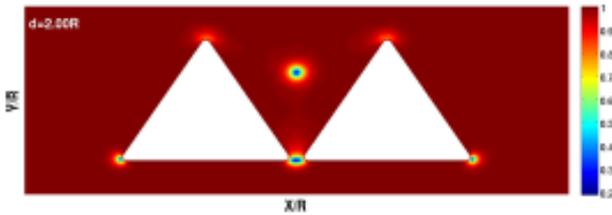
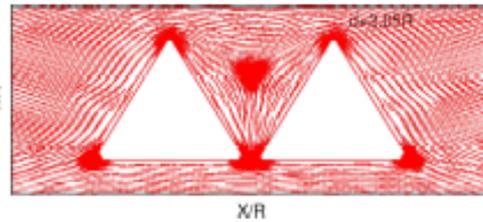
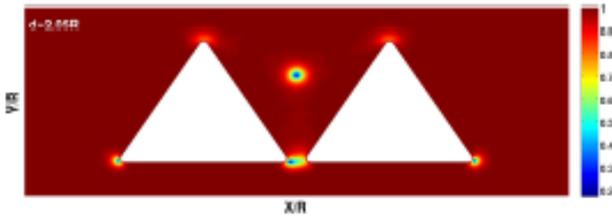
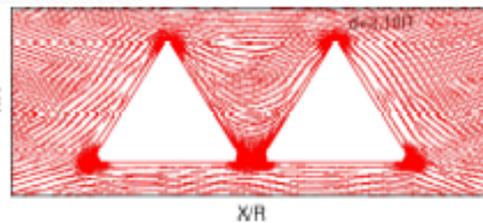
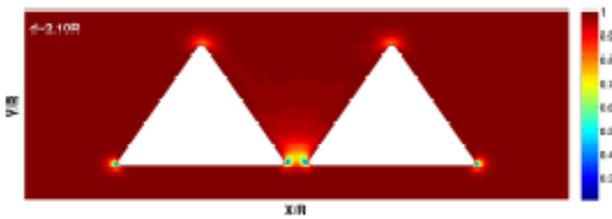
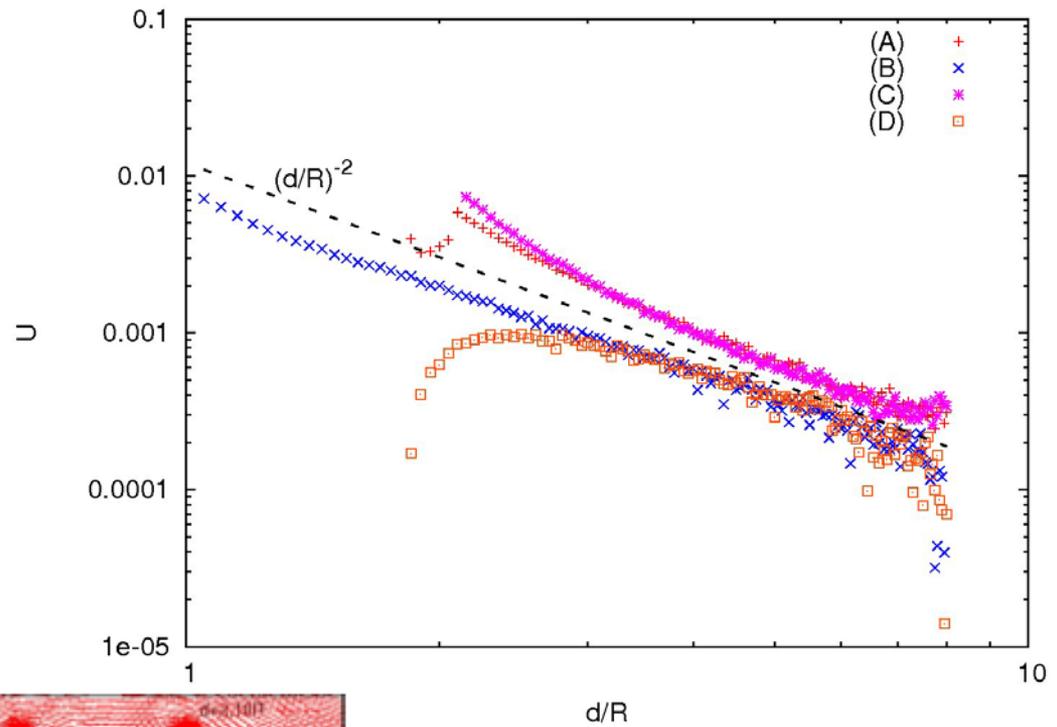
Science 326, 1083 (2009);

DOI: 10.1126/science.1176587



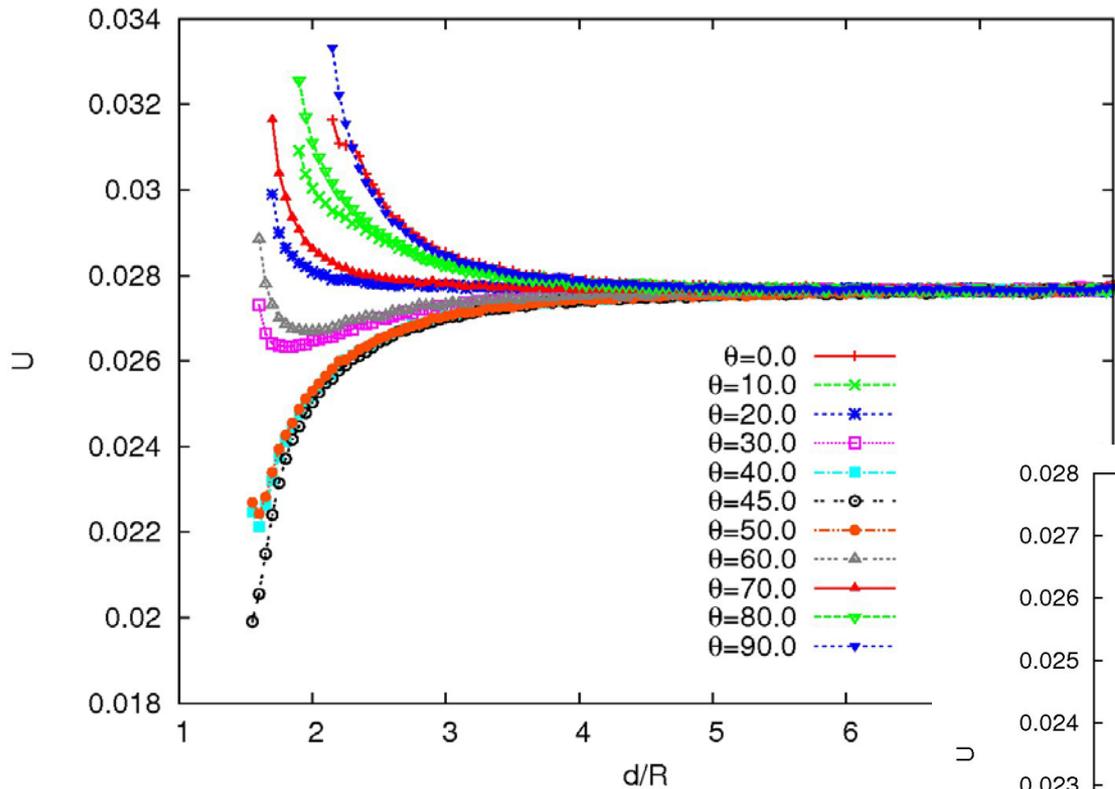
2D calculations

Planar anchoring



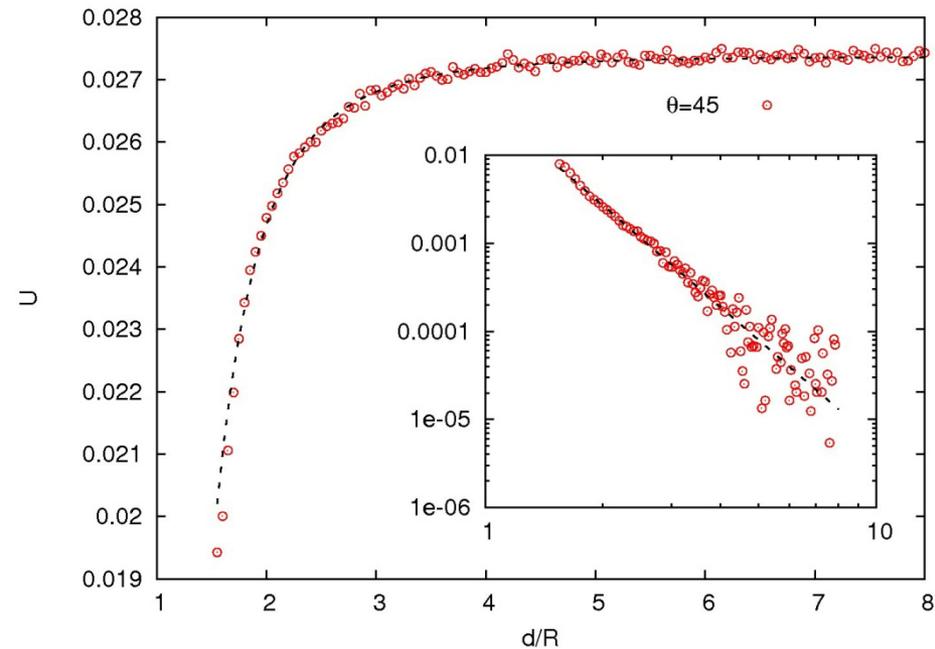
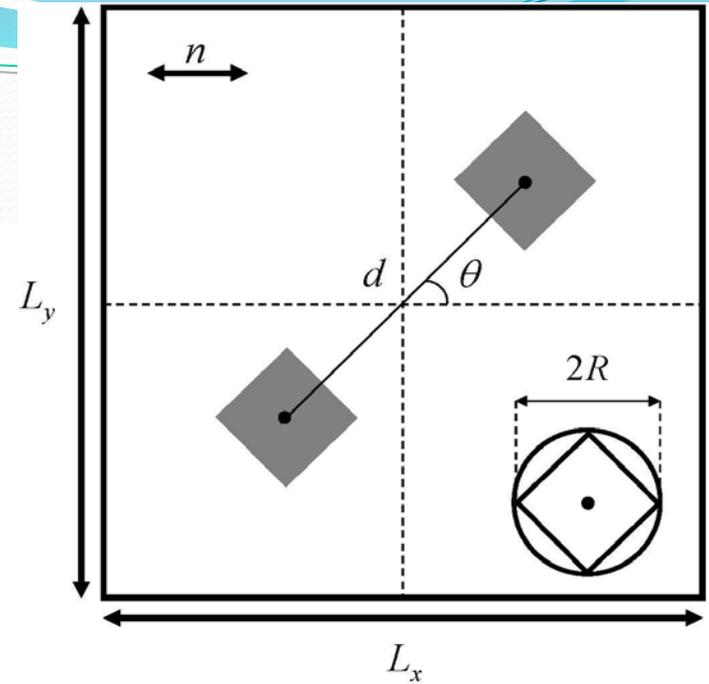
2D calculations

Planar anchoring

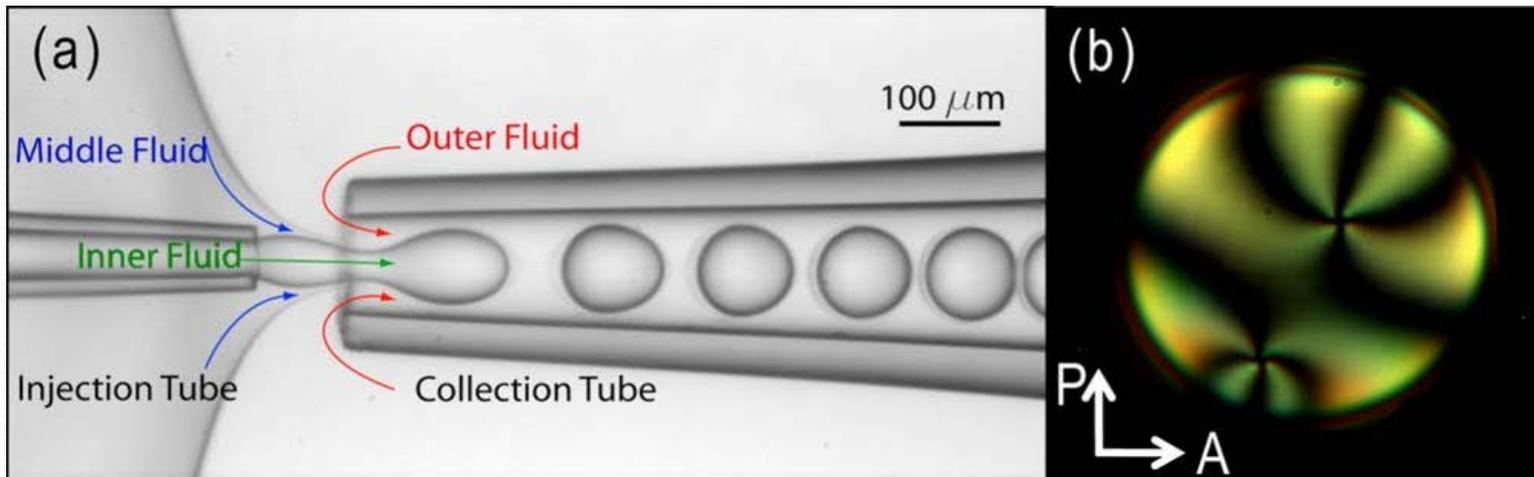


$$U(d) = a + \left(\frac{b}{d}\right)^c$$

$$c = 3.78 \pm 0.06$$

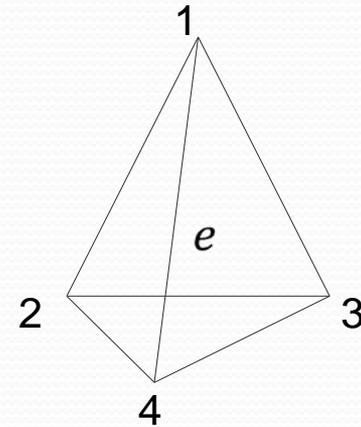
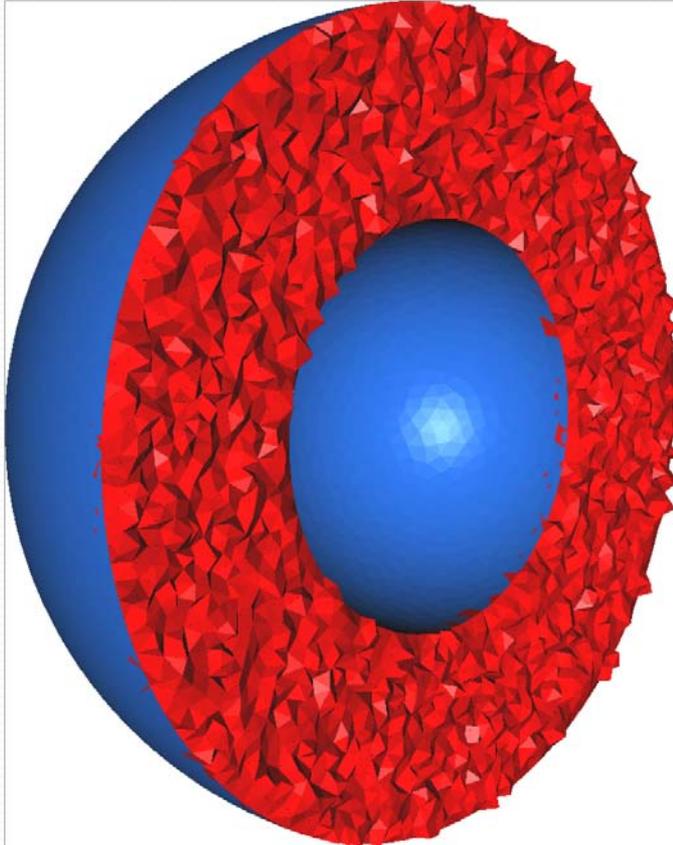


- Experimental observations



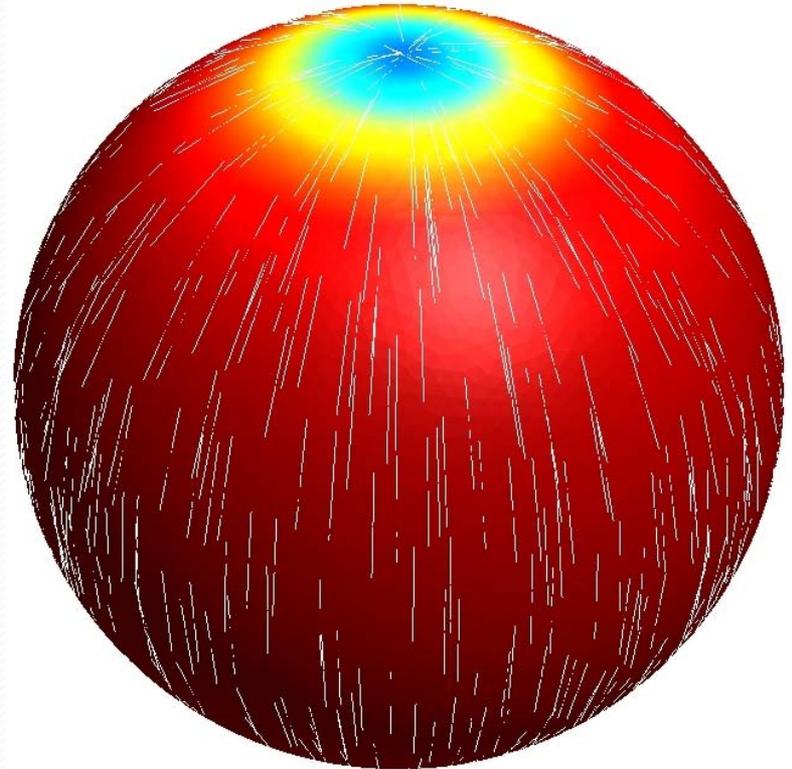
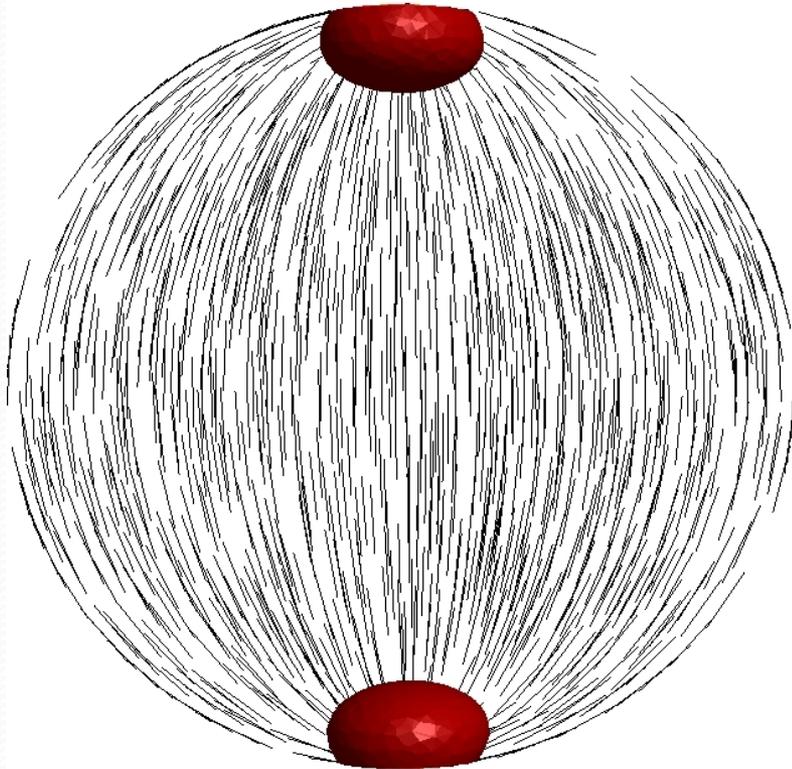
Phys Rev. E 79, 021707 (2009)

- FEM method

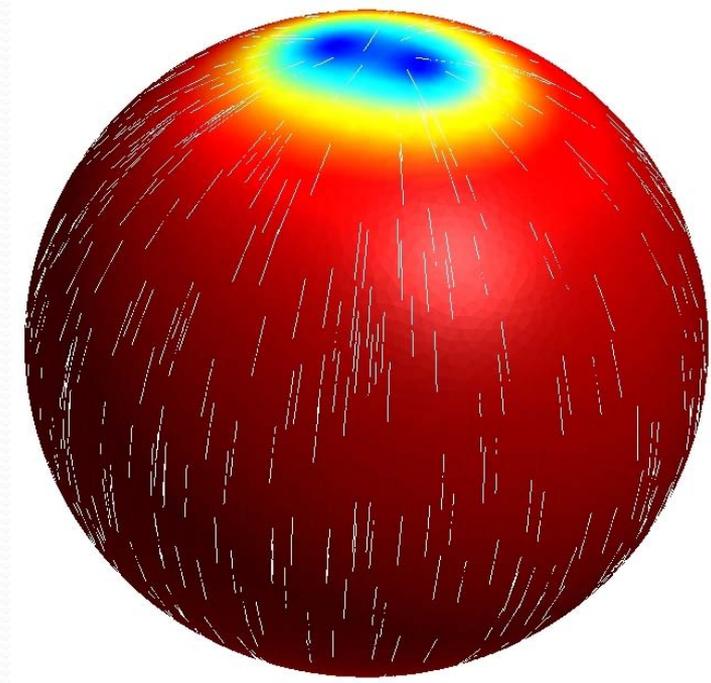
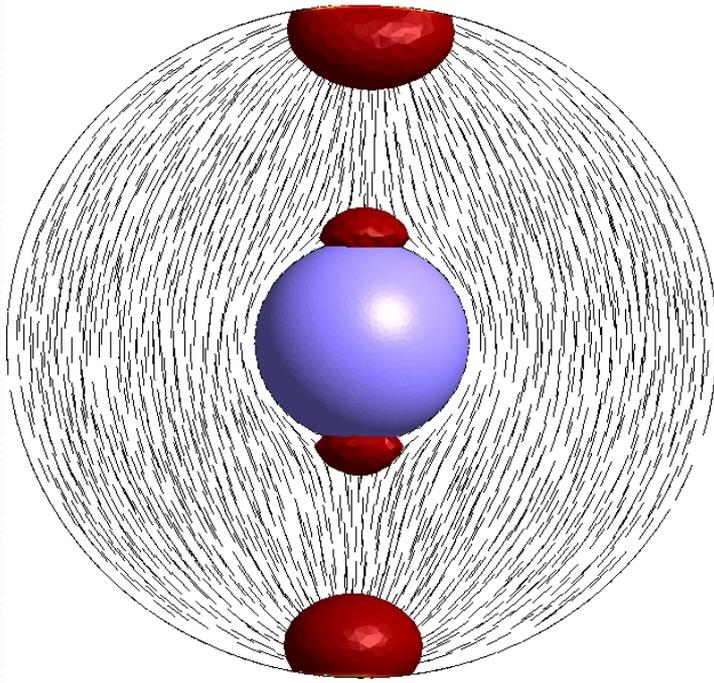


$$\varphi^e = a^e x + b^e y + c^e z + d^e$$

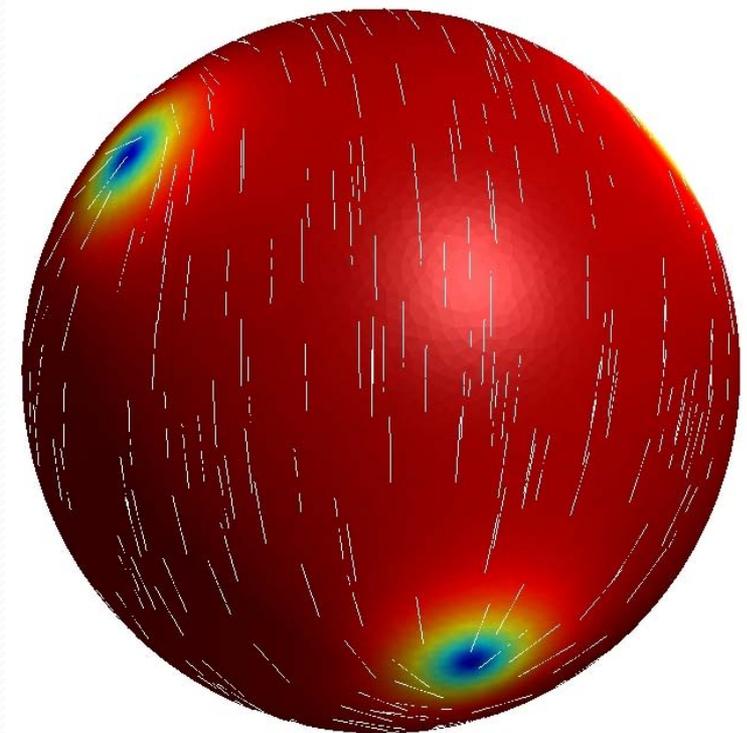
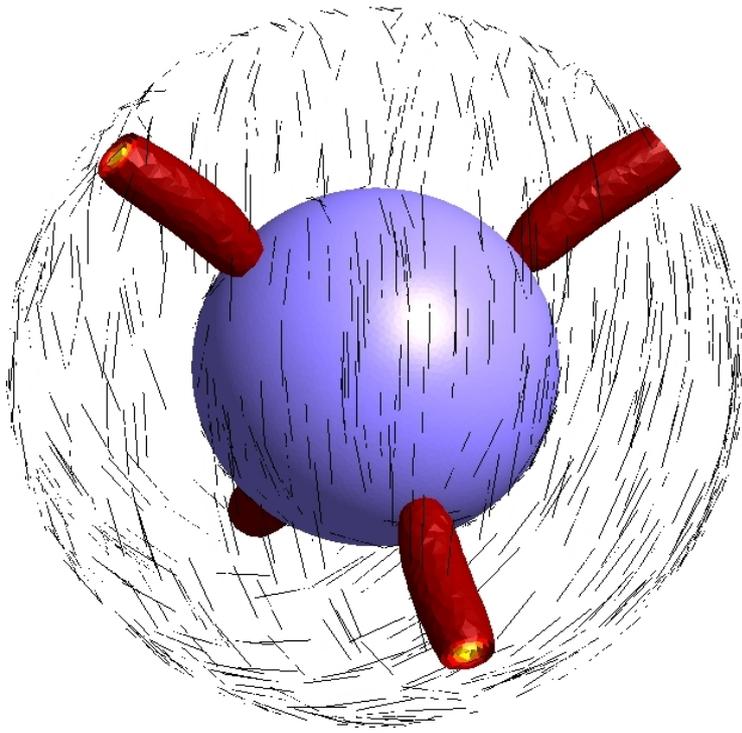
- Spherical droplet



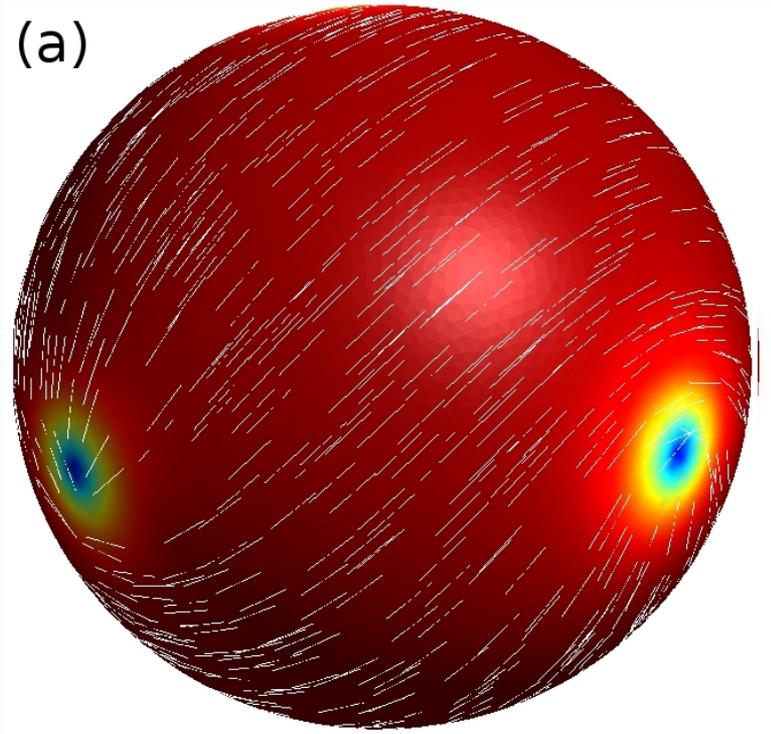
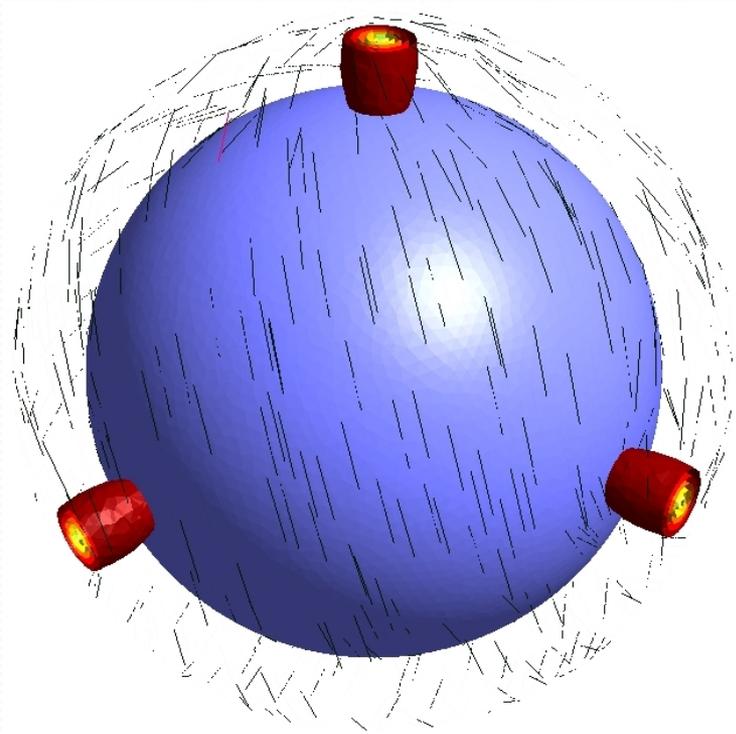
- Thick shells

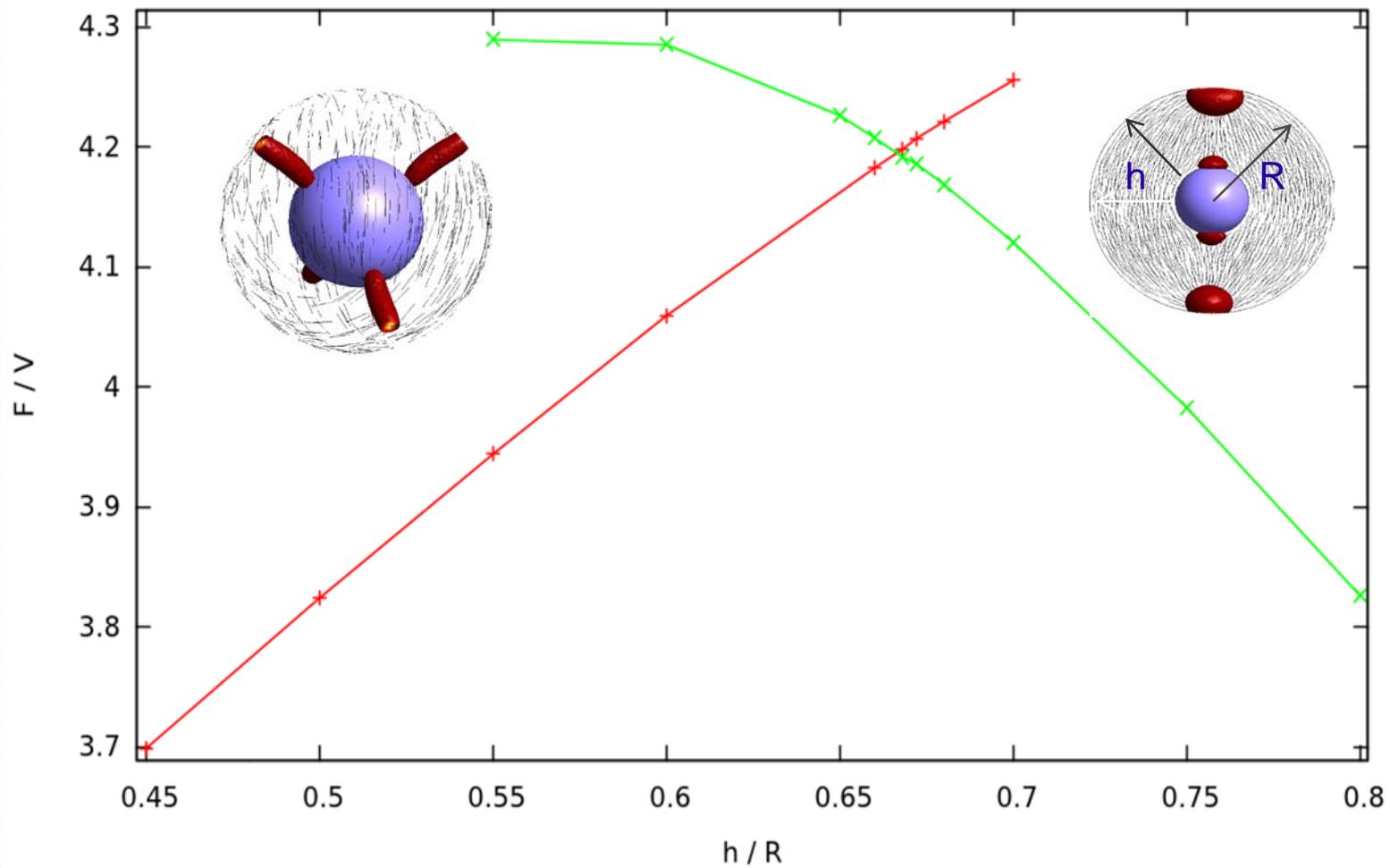


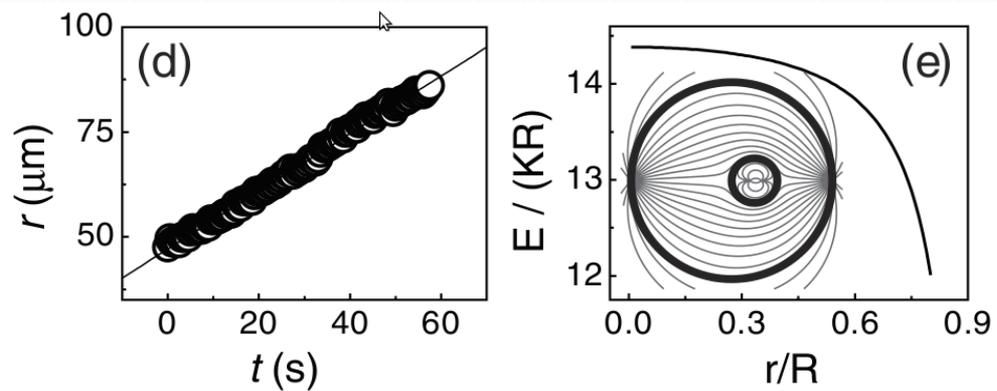
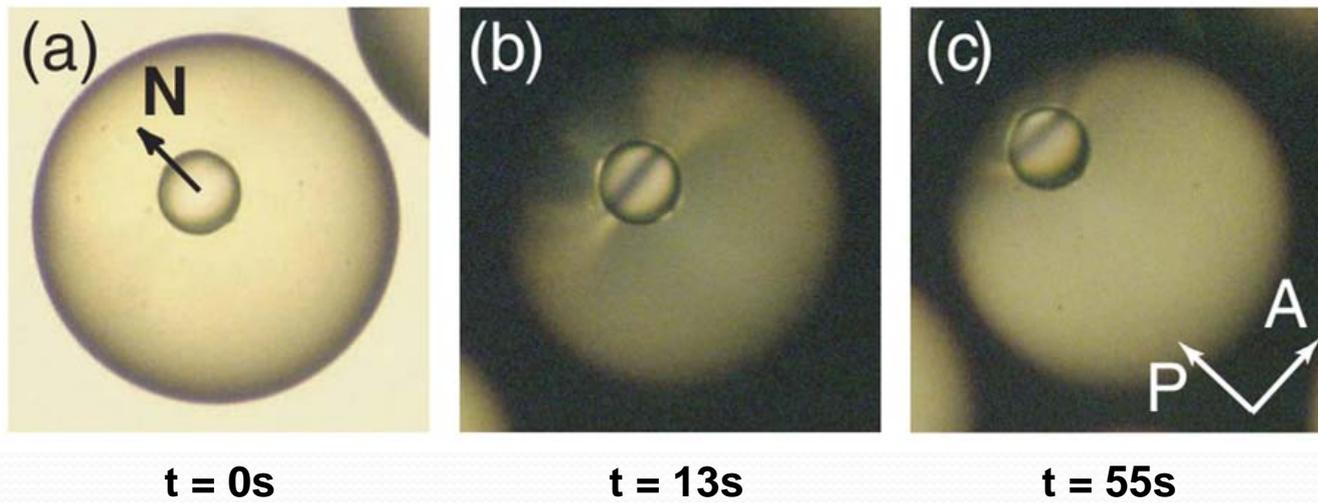
- Thin shells



- Thin shells

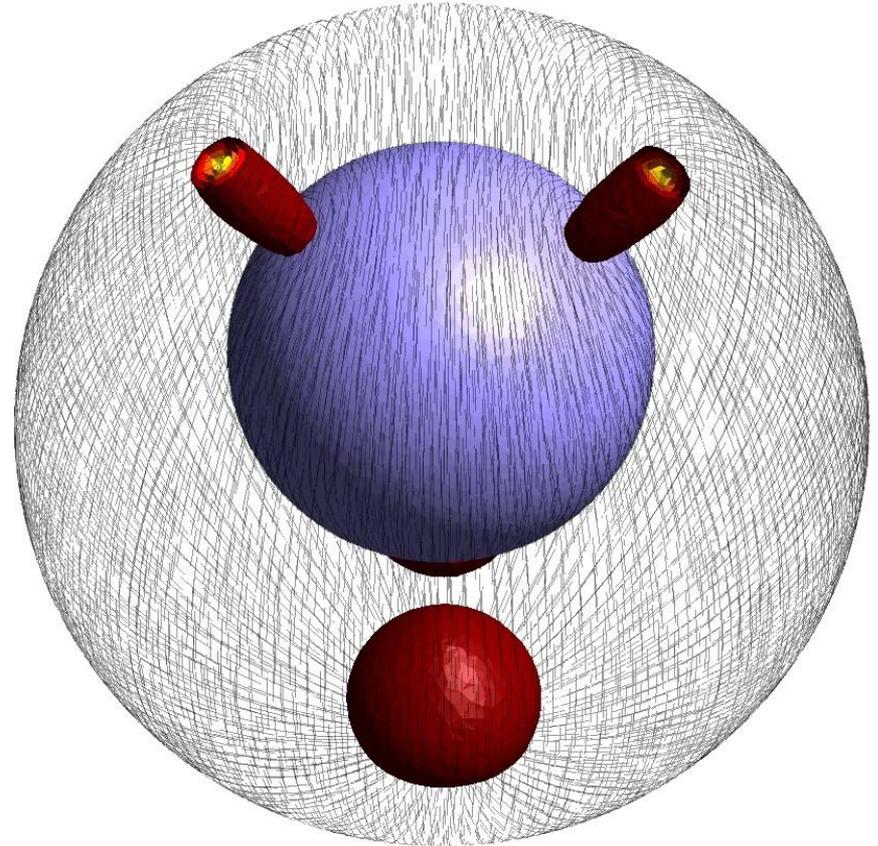
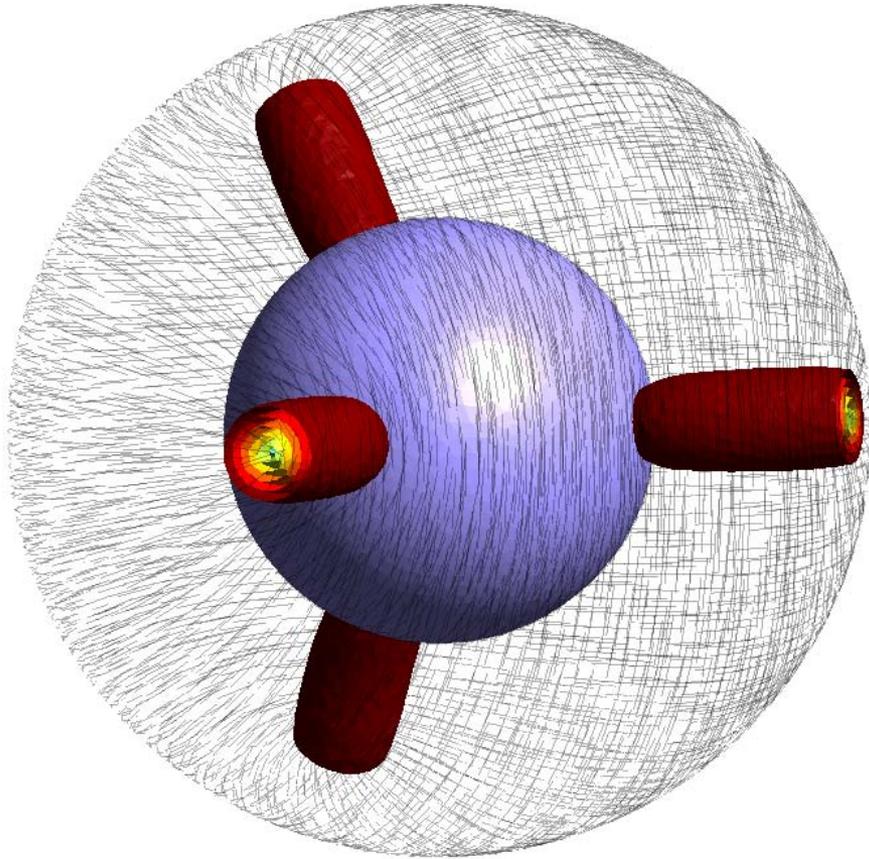






PRL 99, 157801 (2007)

- Off center spheres in thick shell



- Off center spheres in thin shell

