

Testing the Standard Model with the lepton g-2

Massimo Passera
INFN Padova

IPM International School & Workshop
on Particle Physics (IPP13)
May 5th 2013
School of Physics - IPM, Tehran, Iran

Preamble: today's values

$$a_e = 1159652180.73 (28) \times 10^{-12}$$

0.24 parts per billion !! (Hanneke et al., PRL100 (2008) 120801)

$$a_\mu = 116592089 (63) \times 10^{-11}$$

0.5 parts per million !! (E821 – Final Report: PRD73 (2006) 072003)

$$a_\tau = -0.018 (17)$$

Well, not much yet.... (PDG 2012)

Outline

- ➊ 1. Lepton magnetic moments: the basics
- ➋ 2. μ : The muon g-2: a quick update
- ➌ 3. e : Testing new physics with the electron g-2
- ➍ 4. τ : The tau g-2: opportunities & challenges (fantasies?)

1. Lepton magnetic moments: the basics

The beginning: g=2

- Uhlenbeck and Goudsmit in 1926 proposed:

$$\vec{\mu} = g \frac{e}{2mc} \vec{s}$$
$$g = \underline{2} \quad (\text{not } 1!)$$

- Dirac 1928:

$$(i\partial_\mu - eA_\mu) \gamma^\mu \psi = m\psi$$

- A Pauli term in Dirac's eq would give a deviation...

$$a \frac{e}{2m} \sigma_{\mu\nu} F^{\mu\nu} \psi \rightarrow g = 2(1 + a)$$

...but there was no need for it! g=2 stood for ~20 yrs.

Theory of the g-2: Quantum Field Theory

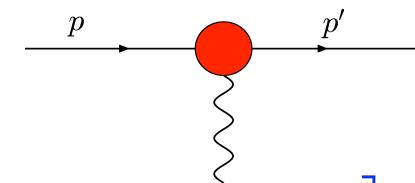
- Kusch and Foley 1948:

$$\mu_e^{\text{exp}} = \frac{e\hbar}{2mc} (1.00119 \pm 0.00005)$$

- Schwinger 1948 (triumph of QED!):

$$\mu_e^{\text{th}} = \frac{e\hbar}{2mc} \left(1 + \frac{\alpha}{2\pi}\right) = \frac{e\hbar}{2mc} \times 1.00116$$

- Keep studying the lepton- γ vertex:



$$\bar{u}(p')\Gamma_\mu u(p) = \bar{u}(p') \left[\gamma_\mu F_1(q^2) + \frac{i\sigma_{\mu\nu}q^\nu}{2m} F_2(q^2) + \dots \right] u(p)$$

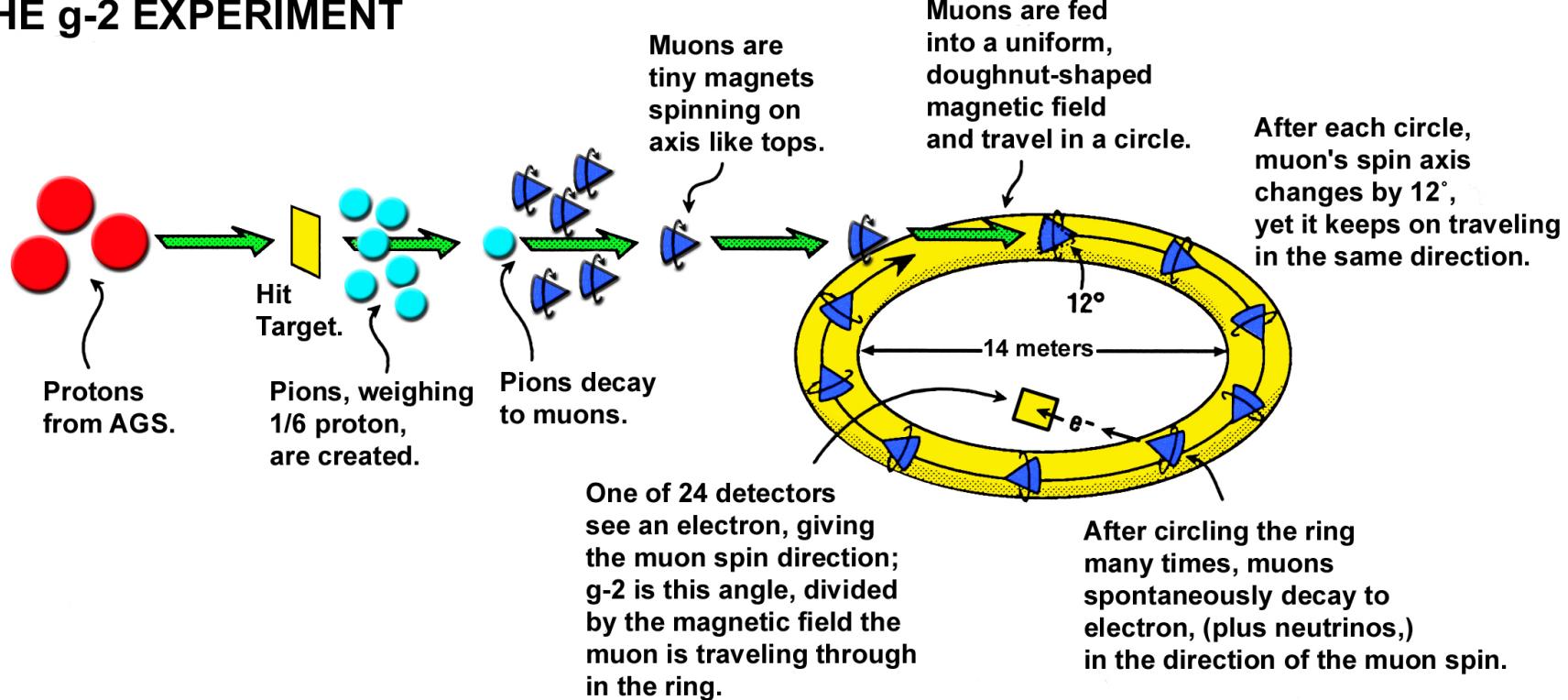
$$F_1(0) = 1 \quad F_2(0) = a_l$$

A pure “quantum correction” effect!

2. The muon g-2: a quick update

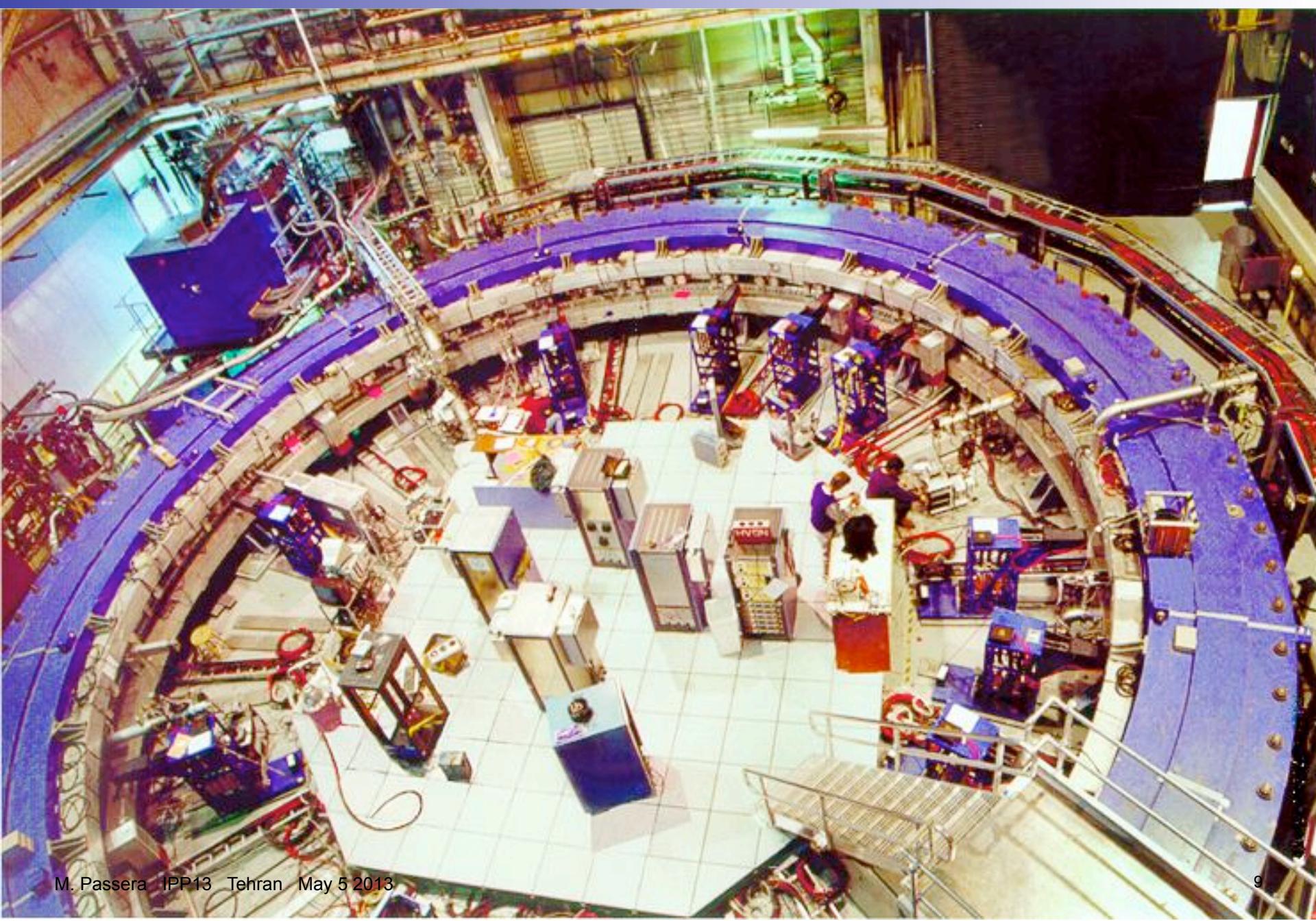
The experiment E821

LIFE OF A MUON: THE g-2 EXPERIMENT

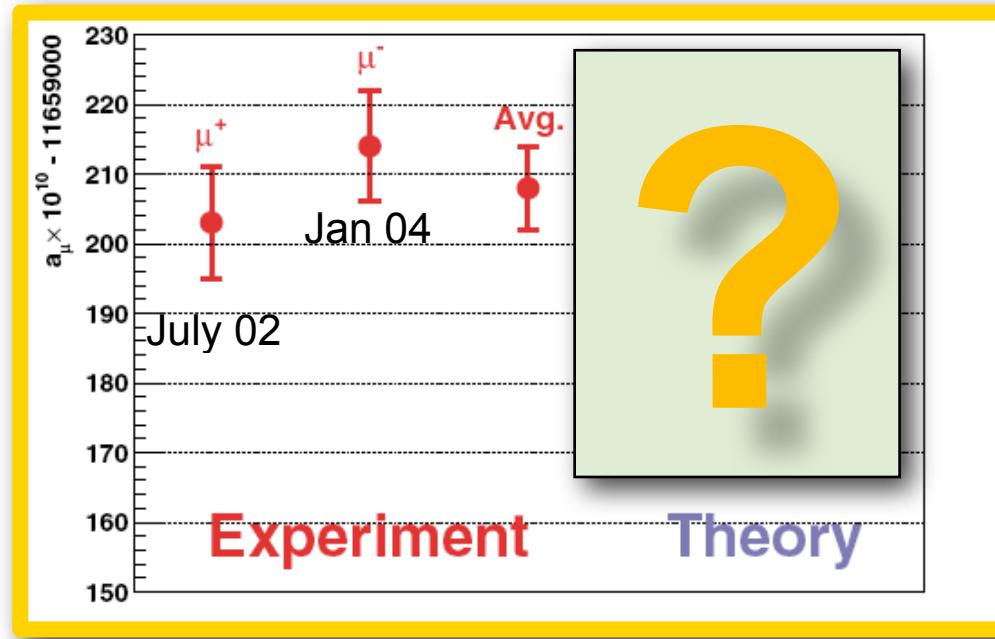


E821 @ BNL

The experiment E821 (II)



The muon g-2: the experimental result



- Today: $a_\mu^{\text{EXP}} = (116592089 \pm 54_{\text{stat}} \pm 33_{\text{sys}}) \times 10^{-11}$ [0.5 ppm].
- Future: new muon g-2 experiments proposed at:
 - Fermilab (E989), aiming at 0.14 ppm → Sep 2012: CD0 approval!
Data in 2017?
 - J-PARC aiming at 0.1 ppm
- See B.Lee Roberts & T. Mibe @ Tau2012, September 2012
- Are theorists ready for this (amazing) precision? No(t yet)

The muon g-2: the QED contribution

$$a_\mu^{\text{QED}} = (1/2)(\alpha/\pi)$$

Schwinger 1948

$$+ 0.765857425 (17) (\alpha/\pi)^2$$

Sommerfield; Petermann; Suura & Wichmann '57; Elend '66; MP '04

$$+ 24.05050996 (32) (\alpha/\pi)^3$$

Remiddi, Laporta, Barbieri ... ; Czarnecki, Skrzypek; MP '04;
Friot, Greynat & de Rafael '05, Mohr, Taylor & Newell '08

$$+ 130.8796 (63) (\alpha/\pi)^4$$

Kinoshita & Lindquist '81, ... , Kinoshita & Nio '04, '05;
Aoyama, Hayakawa, Kinoshita & Nio, 2007, Kinoshita et al. 2012

$$+ 753.29 (1.04) (\alpha/\pi)^5 \text{ COMPLETED!}$$

Kinoshita et al. '90, Yelkhovsky, Milstein, Starshenko, Laporta,
Karshenboim, ..., Kataev, Kinoshita & Nio '06, Kinoshita et al. 2012

Adding up, we get:

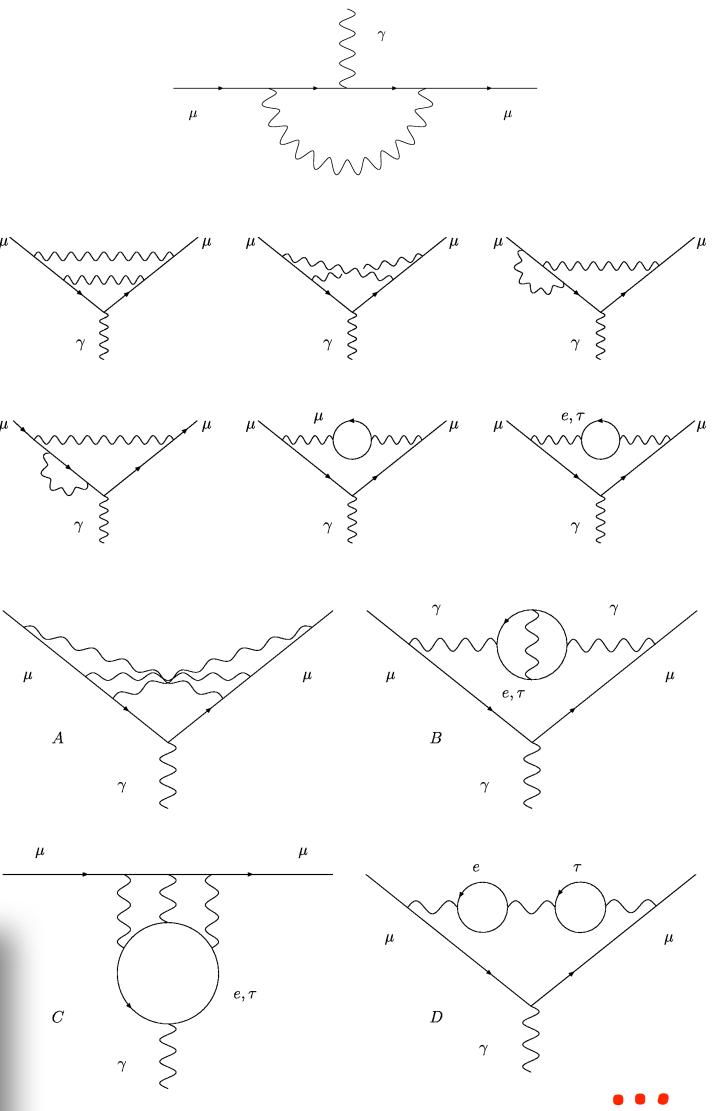
$$a_\mu^{\text{QED}} = 116584718.951 (22)(77) \times 10^{-11}$$

from coeffs, mainly from 4-loop unc



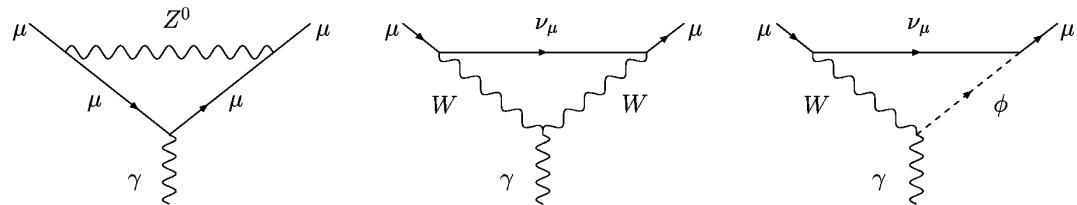
from $\delta\alpha(Rb)$

$$\text{with } \alpha=1/137.035999049(90) [0.66 \text{ ppb}]$$



The muon g-2: the electroweak contribution

- One-loop term:



$$a_\mu^{\text{EW}}(\text{1-loop}) = \frac{5G_\mu m_\mu^2}{24\sqrt{2}\pi^2} \left[1 + \frac{1}{5} (1 - 4 \sin^2 \theta_W)^2 + O\left(\frac{m_\mu^2}{M_{Z,W,H}^2}\right) \right] \approx 195 \times 10^{-11}$$

1972: Jackiw, Weinberg; Bars, Yoshimura; Altarelli, Cabibbo, Maiani; Bardeen, Gastmans, Lautrup; Fujikawa, Lee, Sanda;
Studenikin et al. '80s

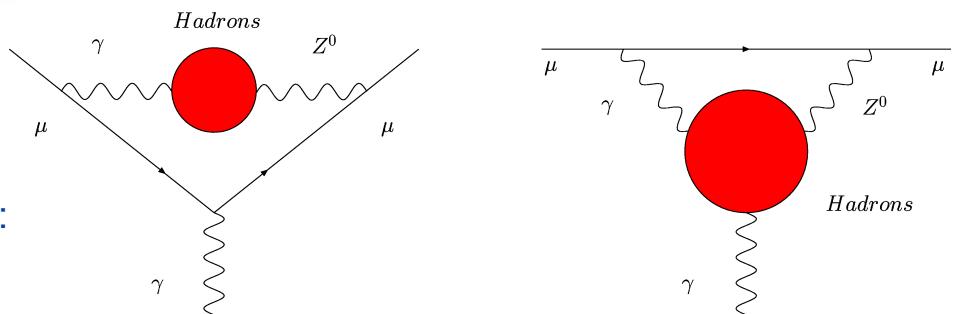
- One-loop plus higher-order terms:

$$a_\mu^{\text{EW}} = 154 (2) (1) \times 10^{-11}$$

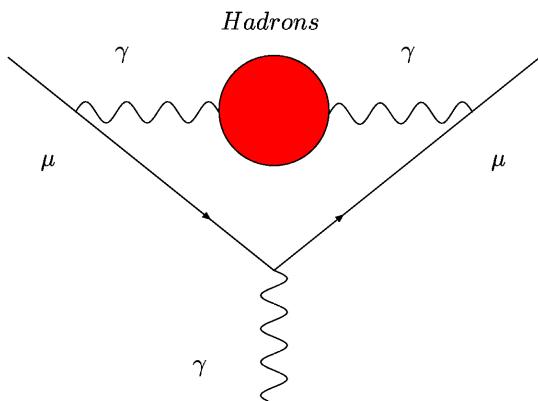
(Higgs mass variation,) M_{top} error,
3-loop nonleading logs

Hadronic loop uncertainties:

Kukhto et al. '92; Czarnecki, Krause, Marciano '95; Knecht, Peris, Perrottet, de Rafael '02; Czarnecki, Marciano, Vainshtein '02; Degrassi, Giudice '98; Heinemeyer, Stockinger, Weiglein '04; Gribouk, Czarnecki '05; Vainshtein '03.



The muon g-2: the hadronic LO contribution (HLO)



$$K(s) = \int_0^1 dx \frac{x^2(1-x)}{x^2 + (1-x)s/m_\mu^2}$$

$$a_\mu^{\text{HLO}} = \frac{1}{4\pi^3} \int_{4m_\pi^2}^\infty ds K(s) \sigma^{(0)}(s) = \frac{\alpha^2}{3\pi^2} \int_{4m_\pi^2}^\infty \frac{ds}{s} K(s) R(s)$$

$$a_\mu^{\text{HLO}} = 6903 (53)_{\text{tot}} \times 10^{-11}$$

F. Jegerlehner, A. Nyffeler, Phys. Rept. 477 (2009) 1

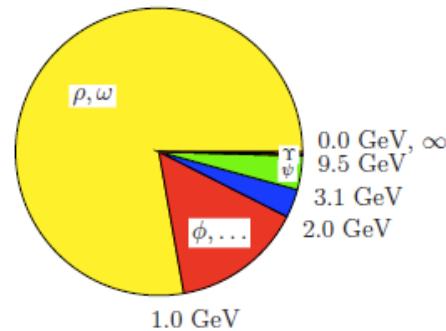
$$= 6923 (42)_{\text{tot}} \times 10^{-11}$$

Davier et al, EPJ C71 (2011) 1515 (incl. BaBar & KLOE10 2π)

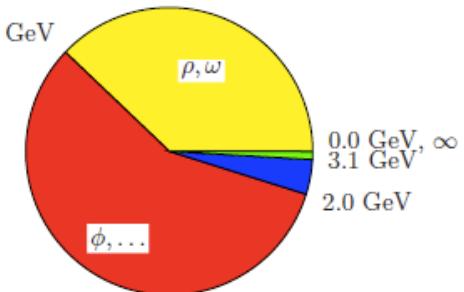
$$= 6949 (37)_{\text{exp}} (21)_{\text{rad}} \times 10^{-11}$$

Hagiwara et al, JPG 38 (2011) 085003

Central values



Errors²



F. Jegerlehner and A. Nyffeler, Phys. Rept. 477 (2009) 1



The muon g-2: the HLO contribution from e^+e^- data

- ➊ The overall agreement of all e^+e^- data looks reasonably good, some discrepancies exist.
- ➋ **Energy scan:** Agreement between the CMD2 & SND $\pi^+\pi^-$ data at VEPP-2M. Prelim results presented in Sep 2012 by CMD3 & SND at the new VEPP-2000 collider in Novosibirsk. See Shwartz @ Tau2012
- ➌ **Initial State Radiation Method (ISR):** Collider operates at fixed energy but s_π can vary continuously. Important independent method made possible by strong th & exp interplay.
- ➍ **KLOE:** The “small angle” (2008) and “large angle” (2010) $\pi^+\pi^-$ ISR analyses agree. Sep 2012: new measure by the $\pi\pi\gamma/\mu\mu\gamma$ ratio presented. It confirms their earlier results. See Mandaglio @ Tau2012
- ➎ Reasonable agreement between **KLOE** and **CMD2-SND** (especially below the ρ). The contributions to a_μ^{HLO} agree.
- ➏ **BaBar:** ISR $\pi^+\pi^-$ result from 0.3 to 3 GeV (2009). Discrepancy between the results of BaBar and KLOE. See Davier @ Tau2012

The muon g-2: the HLO contribution from tau-decay data

- The tau data of ALEPH, CLEO & OPAL are higher than the CMD2/SND/KLOE ones, particularly above the ρ . The 2008 $a_{\mu}^{\pi\pi}$ tau data result of Belle agrees with Aleph-Cleo-Opal (some deviations from Aleph's spectral functions).
- Revisited analysis in 2011: (Davier et al, EPJ C71 (2011) 1515)

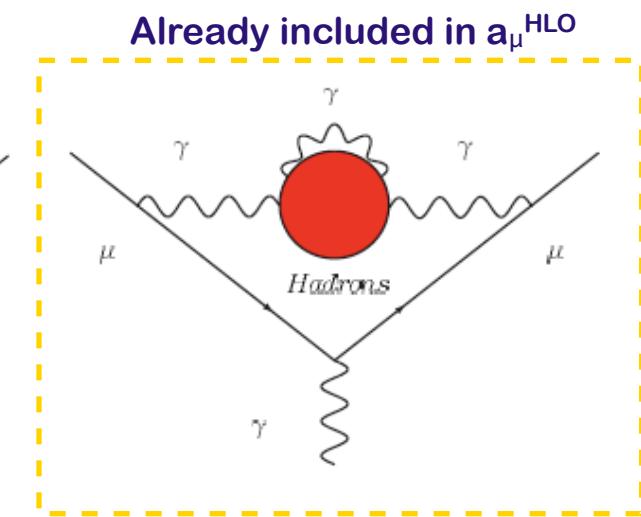
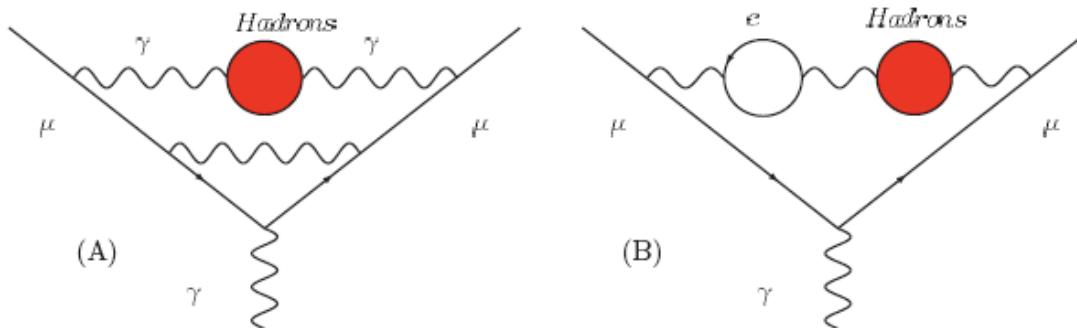
$$a_{\mu}^{\text{HLO}} = 7015 (47) \times 10^{-11}$$

Belle's data included + IB corrections revisited & updated

(Marciano & Sirlin '88; Cirigliano, Ecker, Neufeld '01-'02, Flores-Baez et al. '06&'07)

- The discrepancy with e^+e^- data decreased. Are there inconsistencies in e^+e^- or τ data? All possible isospin-breaking (IB) effects taken into account?
- Claims exist that tau data are actually consistent with e^+e^- ones after IB effects & vector meson mixings considered! (Benayoun et al., 2007, 2009 and EPJC72 (2012)1848, Jegerlehner & Szafron 2011).

- HHO: Vacuum Polarization**



$\mathcal{O}(\alpha^3)$ contributions of diagrams containing hadronic vacuum polarization insertions:

$$a_\mu^{\text{HHO(vp)}} = -98(1) \times 10^{-11}$$

Krause '96, Alemany et al. '98, Hagiwara et al. 2011

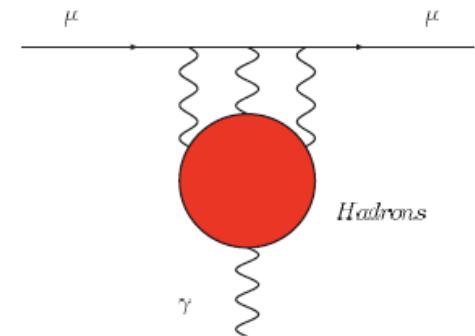
Only tiny shifts if τ data are used instead of the e^+e^- ones

Davier & Marciano '04.

- HHO: Light-by-light contribution**

Unlike the HLO term, for the hadronic l-b-l term we must rely on theoretical approaches.

This term had a troubled life! Recent values:



$$a_\mu^{\text{HHO}}(|l|) = +80(40) \times 10^{-11} \quad \text{Knecht \& Nyffeler '02}$$

$$a_\mu^{\text{HHO}}(|l|) = +136(25) \times 10^{-11} \quad \text{Melnikov \& Vainshtein '03}$$

$$a_\mu^{\text{HHO}}(|l|) = +105(26) \times 10^{-11} \quad \text{Prades, de Rafael, Vainshtein '09}$$

$$a_\mu^{\text{HHO}}(|l|) = +116(39) \times 10^{-11} \quad \text{Jegerlehner \& Nyffeler '09}$$

Results based also on Hayakawa, Kinoshita '98 & '02; Bijnens, Pallante, Prades '96 & '02

- “Bound” $a_\mu^{\text{HHO}}(|l|) < \sim 160 \times 10^{-11}$ Erler&Sanchez '06, Pivovarov '02; also Boughezal&Melnikov'11
- Lattice? Very hard... in progress.
- Large “by far not complete” calculation: 188×10^{-11} Fischer et al, PRD87(2013)034013
- Had lbl is likely to become the ultimate limitation of the SM prediction.

The muon g-2: SM vs. Experiment

Adding up all contributions, we get the following SM predictions and comparisons with the measured value:

$$a_\mu^{\text{EXP}} = 116592089 (63) \times 10^{-11}$$

E821 – Final Report: PRD73 (2006) 072
with latest value of $\lambda = \mu_\mu / \mu_p$ (CODATA'06)

$a_\mu^{\text{SM}} \times 10^{11}$	$(\Delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}}) \times 10^{11}$	σ
[1] 116 591 783 (59)	306 (86)	3.5
[2] 116 591 803 (49)	286 (80)	3.6
[3] 116 591 829 (50)	260 (80)	3.2
[4] 116 591 895 (54)	194 (83)	2.3

$$\text{with } a_\mu^{\text{HHO}}(\text{lbf}) = 105 (26) \times 10^{-11}$$

- [1] F. Jegerlehner, A. Nyffeler, Phys. Rept. 477 (2009) 1
- [2] Davier et al, EPJ C71 (2011) 1515 (includes BaBar and KLOE10 2π)
- [3] HLMNT11: Hagiwara et al, JPG38 (2011) 085003 (incl BaBar and KLOE10 2π)
- [4] Davier et al, Eur.PJ C71 (2011) 1515, τ data.

Note that the th. error is now about the same as the exp. one

How do we explain Δa_μ ? Is it New Physics?

- Δa_μ can be explained in many ways: errors in LBL, QED, EW, HHO-VP, g-2 EXP, HLO; or, we hope, New Physics!
- Can Δa_μ be due to hypothetical mistakes in the hadronic $\sigma(s)$?
- An upward shift of $\sigma(s)$ also induces an increase of $\Delta\alpha_{\text{had}}^{(5)}(M_Z)$.
- Consider:

$$\begin{aligned} a_\mu^{\text{HLO}} \rightarrow & \quad a = \int_{4m_\pi^2}^{s_u} ds f(s) \sigma(s), \quad f(s) = \frac{K(s)}{4\pi^3}, \quad s_u < M_Z^2, \\ \Delta\alpha_{\text{had}}^{(5)} \rightarrow & \quad b = \int_{4m_\pi^2}^{s_u} ds g(s) \sigma(s), \quad g(s) = \frac{M_Z^2}{(M_Z^2 - s)(4\alpha\pi^2)}, \end{aligned}$$

and the increase

$$\Delta\sigma(s) = \epsilon\sigma(s)$$

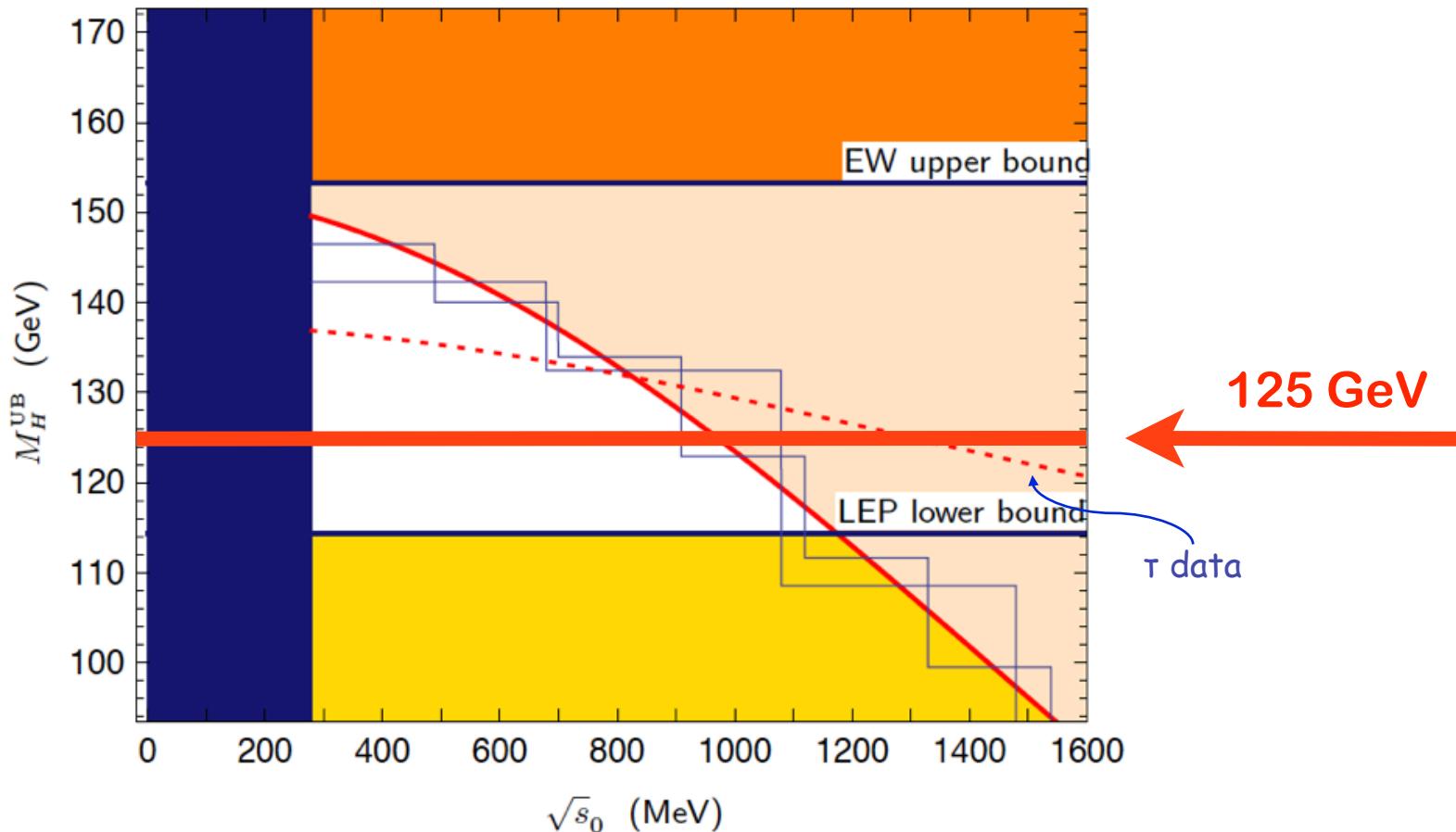
($\epsilon > 0$), in the range:

$$\sqrt{s} \in [\sqrt{s_0} - \delta/2, \sqrt{s_0} + \delta/2]$$



The muon g-2: connection with the SM Higgs mass

- How much does the M_H upper bound from the EW fit change when we shift $\sigma(s)$ by $\Delta\sigma(s)$ [and thus $\Delta\alpha_{\text{had}}^{(5)}(M_Z)$] to accommodate Δa_μ ?



W.J. Marciano, A. Sirlin, MP, 2008 & 2010

The muon g-2: connection with the SM Higgs mass (II)

- Given the quoted exp. uncertainty of $\sigma(s)$, the possibility to explain the muon g-2 with these very large shifts $\Delta\sigma(s)$ appears to be very unlikely.
- Also, given a **125 GeV SM Higgs**, these hypothetical shifts $\Delta\sigma(s)$ could only occur at very low energy (below ~ 1 GeV).
- Vice versa, assuming we now have a SM Higgs with $M_{Higgs} = 125$ GeV, if we bridge the M_{Higgs} discrepancy in the EW fit via changes in the low-energy hadronic cross section, **the muon g-2 discrepancy increases**.

W.J. Marciano, A. Sirlin, MP, 2008 & 2010

3. Testing new physics with the electron g-2

G.F. Giudice, P. Paradisi, MP

JHEP 1211 (2012) 113

The QED prediction of the electron g-2

$$a_e^{\text{QED}} = + (1/2)(\alpha/\pi) - 0.328\ 478\ 444\ 002\ 55(33) (\alpha/\pi)^2$$

Schwinger 1948

Sommerfield; Petermann; Suura&Wichmann '57; Elend '66; CODATA Mar '12

$$A_1^{(4)} = -0.328\ 478\ 965\ 579\ 193\ 78\dots$$

$$A_2^{(4)} (m_e/m_\mu) = 5.197\ 386\ 68 (26) \times 10^{-7}$$

$$A_2^{(4)} (m_e/m_\tau) = 1.837\ 98 (33) \times 10^{-9}$$

$$+ 1.181\ 234\ 016\ 816 (11) (\alpha/\pi)^3$$

Kinoshita, Barbieri, Laporta, Remiddi, ... , Li, Samuel; MP '06; GPP 2012

$$A_1^{(6)} = 1.181\ 241\ 456\ 587\dots$$

$$A_2^{(6)} (m_e/m_\mu) = -7.373\ 941\ 62 (27) \times 10^{-6}$$

$$A_2^{(6)} (m_e/m_\tau) = -6.5830 (11) \times 10^{-8}$$

$$A_3^{(6)} (m_e/m_\mu, m_e/m_\tau) = 1.909\ 82 (34) \times 10^{-13}$$

$$- 1.9097 (20) (\alpha/\pi)^4$$

Kinoshita & Lindquist '81, ... , Kinoshita & Nio '05; Aoyama, Hayakawa, Kinoshita & Nio, May 2012

$$+ 9.16 (58) (\alpha/\pi)^5 \quad (12672 \text{ mass independent diagrams!})$$

Aoyama, Hayakawa, Kinoshita, Nio, 2012

The SM prediction of the electron g-2

The SM prediction is:

$$a_e^{\text{SM}}(\alpha) = a_e^{\text{QED}}(\alpha) + a_e^{\text{EW}} + a_e^{\text{HAD}}$$

The EW (1&2 loop) term is: Czarnecki, Krause, Marciano '96 [Codata 2012]

$$a_e^{\text{EW}} = 0.2973(52) \times 10^{-13}$$

The Hadronic contribution is: Nomura & Teubner '12, Jegerlehner & Nyffeler '09; Krause '97

$$a_e^{\text{HAD}} = 16.82(16) \times 10^{-13}$$

Which value of α should we use to compute a_e^{SM} and compare it with a_e^{EXP} ?? Not the PDG/Codata one (obtained equating $a_e^{\text{SM}}(\alpha) = a_e^{\text{EXP}}$)! Use atomic-physics measurements of alpha.

The electron g-2 gives the best determination of alpha

- The 2008 measurement of the electron g-2 is:

$$a_e^{\text{EXP}} = 11596521807.3 \text{ (2.8)} \times 10^{-13} \quad \text{Hanneke et al, PRL100 (2008) 120801}$$

vs. old (factor of 15 improvement, 1.8σ difference):

$$a_e^{\text{EXP}} = 11596521883 \text{ (42)} \times 10^{-13} \quad \text{Van Dyck et al, PRL59 (1987) 26}$$

- Equate $a_e^{\text{SM}}(\alpha) = a_e^{\text{EXP}}$ → best determination of alpha (2012):

$$\alpha^{-1} = 137.035\ 999\ 173 \text{ (34)} \quad [0.25 \text{ ppb}]$$

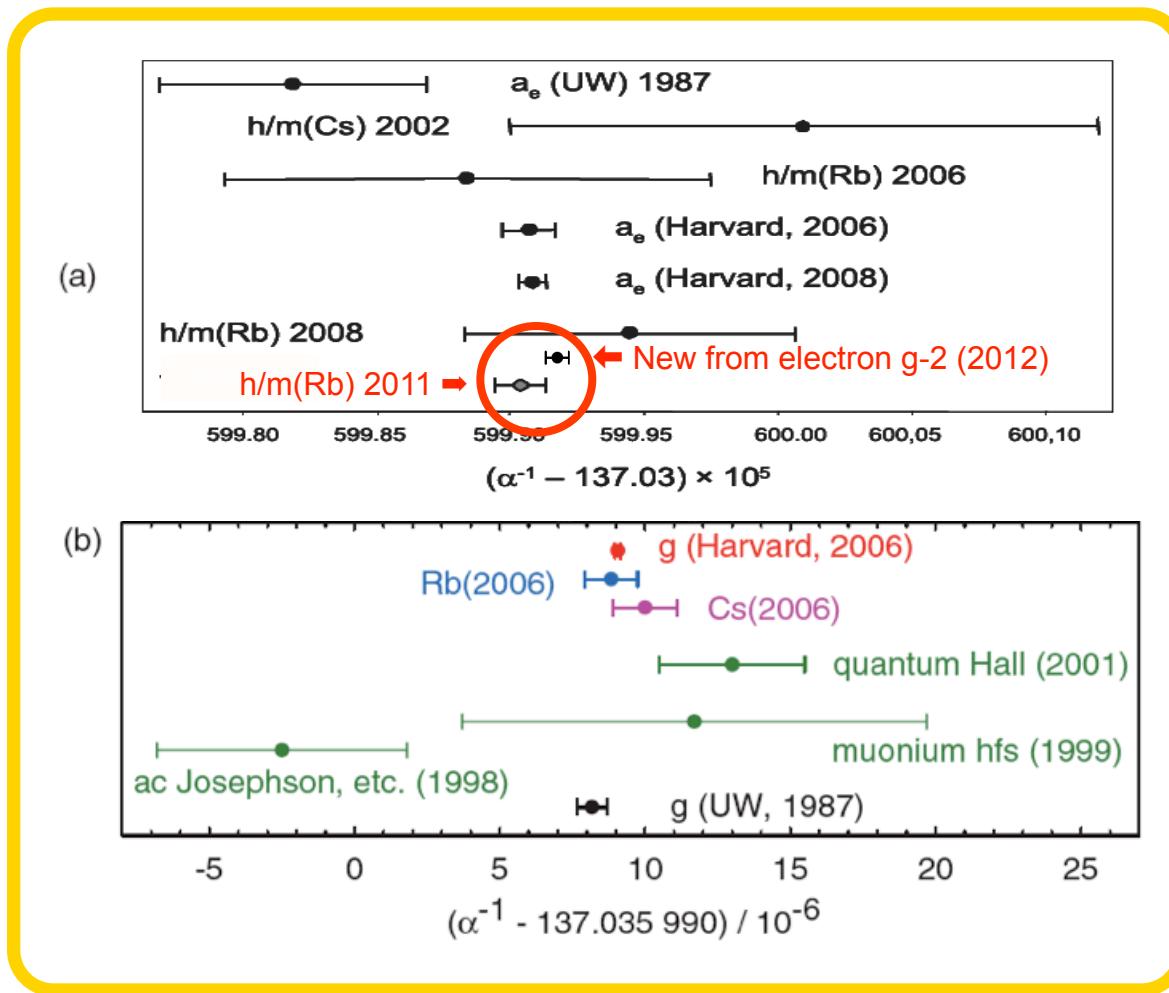
- Compare it with other determinations (independent of a_e):

$$\alpha^{-1} = 137.036\ 000\ 0 \text{ (11)} \quad [7.7 \text{ ppb}] \quad \text{PRA73 (2006) 032504 (Cs)}$$

$$\alpha^{-1} = 137.035\ 999\ 049 \text{ (90)} \quad [0.66 \text{ ppb}] \quad \text{PRL106 (2011) 080801 (Rb)}$$

Excellent agreement → beautiful test of QED at 4-loop level!

Old and new determinations of alpha



Gabrielse, Hanneke, Kinoshita, Nio & Odom, PRL99 (2007) 039902
 Hanneke, Fogwell & Gabrielse, PRL100 (2008) 120801
 Bouchendira et al, PRL106 (2011) 080801

The electron g-2: SM vs. Experiment

- Using $\alpha = 1/137.035\ 999\ 049\ (90)$ [^{87}Rb , 2011], the SM prediction for the electron g-2 is

$$a_e^{\text{SM}} = 115\ 965\ 218\ 17.8\ (0.6)\ (0.4)\ (0.2)\ (7.6) \times 10^{-13}$$

δC_4^{qed} δC_5^{qed} δa_e^{had} from $\delta \alpha$

- The EXP-SM difference is:

$$\Delta a_e = a_e^{\text{EXP}} - a_e^{\text{SM}} = -10.5\ (8.1) \times 10^{-13}$$

The SM is in very good agreement with experiment (1.3σ).

NB: The 4-loop contrib. to a_e^{QED} is $-5.56 \times 10^{-11} \sim 70 \Delta a_e$!
(the 5-loop one is 6.2×10^{-13})

The electron g-2 sensitivity and NP tests

- The present sensitivity is $\delta\Delta a_e = 8.1 \times 10^{-13}$, ie (10^{-13} units):

$$(0.6)_{\text{QED4}}, \quad (0.4)_{\text{QED5}}, \quad (0.2)_{\text{HAD}}, \quad (7.6)_{\delta\alpha}, \quad (2.8)_{\delta a_e^{\text{EXP}}}$$

$\underbrace{\qquad\qquad\qquad}_{(0.7)_{\text{TH}}} \leftarrow \text{may drop to 0.2 or 0.3}$

- The $(g-2)_e$ exp. error may soon drop below 10^{-13} and work is in progress for a significant reduction of that induced by $\delta\alpha$.
→ a sensitivity of 10^{-13} may be reached with ongoing exp work.

- In a broad class of BSM theories, contributions to a_l scale as

$$\frac{\Delta a_{\ell_i}}{\Delta a_{\ell_j}} = \left(\frac{m_{\ell_i}}{m_{\ell_j}} \right)^2 \quad \text{This Naive Scaling leads to:}$$

The electron g-2 sensitivity and NP tests (II)

$$\Delta a_e = \left(\frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.7 \times 10^{-13}; \quad \Delta a_\tau = \left(\frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.8 \times 10^{-6}$$

- The experimental sensitivity in Δa_e is not far from what is required to test whether the discrepancy in $(g-2)_\mu$ also manifests itself in $(g-2)_e$ under the naive scaling hypothesis.
- BSM scenarios exist which violate Naive Scaling leading to larger effects in Δa_e (& Δa_τ).

4. The tau g-2: opportunities & challenges

Work in progress in collaboration with
S. Eidelman, D. Epifanov, M. Fael, L. Mercolli & C. Ng
arXiv:1301.5302

The SM prediction of the tau g-2

The Standard Model prediction of the tau g-2 is:

$$\begin{aligned} a_{\tau}^{SM} = & 117324 & (2) & \times 10^{-8} & \text{QED} \\ & + 47.4 & (0.5) & \times 10^{-8} & \text{EW} \\ & + 337.5 & (3.7) & \times 10^{-8} & \text{HLO} \\ & + 7.6 & (0.2) & \times 10^{-8} & \text{HHO (vac)} \\ & + 5 & (3) & \times 10^{-8} & \text{HHO (lbi)} \end{aligned}$$

$$a_{\tau}^{SM} = 117721 (5) \times 10^{-8}$$

Eidelman & MP
2007

$(m_{\tau}/m_{\mu})^2 \sim 280$: great opportunity to look for New Physics,
and a “clean” NP test too...

	Electron	Muon	Tau
a_{EW}/a_{HAD}	1/56	1/45	1/7
$a_{EW}/\delta a_{HAD}$	1.6	3	10

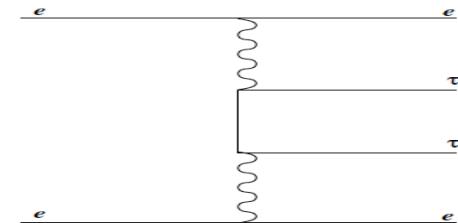
... if only we could measure it!!

The tau g-2: experimental bounds

- The very short lifetime of the tau makes it very difficult to determine a_τ measuring its spin precession in a magnetic field.
- DELPHI's result, from $e^+e^- \rightarrow e^+e^-\tau^+\tau^-$ total cross-section measurements at LEP 2 (the PDG value):

$$a_\tau = -0.018 (17)$$

PDG 2011



- With an effective Lagrangian approach, using data on tau lepton production at LEP1, SLC, and LEP2:

$$-0.004 < a_\tau^{\text{NP}} < 0.006 \quad (95\% \text{ CL})$$

Escribano & Massó 1997

$$-0.007 < a_\tau^{\text{NP}} < 0.005 \quad (95\% \text{ CL})$$

González-Sprinberg et al 2000

- Bernabéu et al, propose the measurement of $F_2(q^2=M_Y^2)$ from $e^+e^- \rightarrow \tau^+\tau^-$ production at B factories. NPB 790 (2008) 160

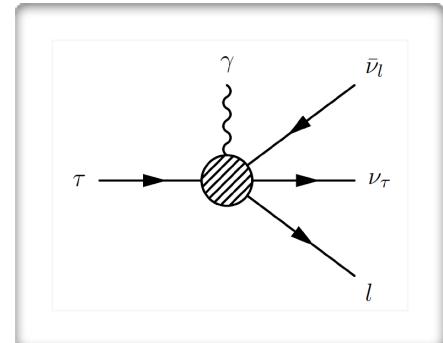
The tau g-2 via its radiative leptonic decays: a proposal

- Tau radiative leptonic decays at LO:

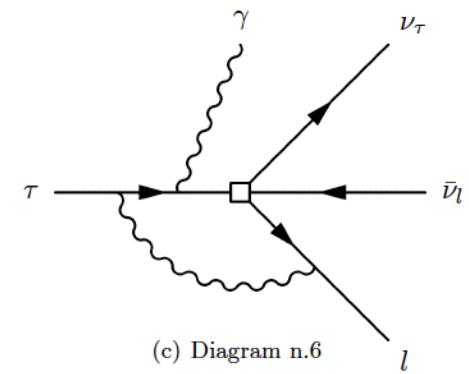
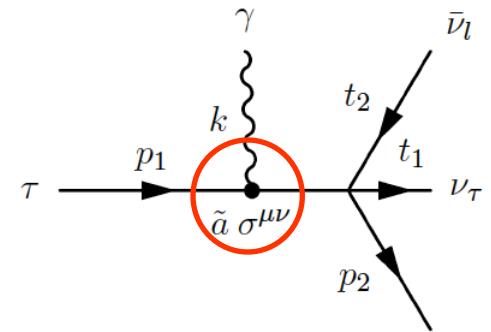
$$\frac{d^3\Gamma}{dx dy d \cos \theta} = \frac{\alpha M_\tau^5 G_F^2 y \sqrt{x^2 - 4r^2}}{2\pi(4\pi)^6} G_0(x, y, \cos \theta, r)$$

Kinoshita & Sirlin PRL2(1959)177; Kuno & Okada, RMP73(2001)151

$$\begin{aligned} \left. \frac{\Gamma(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau \gamma)}{\Gamma_{\text{total}}} \right|_{E_\gamma > 10 \text{ MeV}} &= \boxed{1.823\% \quad \text{vs} \quad 1.75(18)\% \\ \text{CLEO 2000}} \\ \left. \frac{\Gamma(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau \gamma)}{\Gamma_{\text{total}}} \right|_{E_\gamma > 10 \text{ MeV}} &= \boxed{0.364\% \quad \text{vs} \quad 0.361(38)\%} \end{aligned}$$



$$x = \frac{2E_l}{M_\tau}, \quad y = \frac{2E_\gamma}{M_\tau}, \quad r = \frac{m_l}{M_\tau}$$



$$G_0 \rightarrow G_0 + \tilde{a}_\tau G_a + \frac{\alpha}{\pi} G_{\text{RC}}$$

- Measure $d^3\Gamma$ precisely and get \tilde{a}_τ !

[see also Laursen, Samuel, Sen, PRD29 (1984) 2652]

Conclusions

- ➊ The lepton g-2 provide beautiful examples of interplay between theory and experiment.
- ➋ The discrepancy Δa_μ is $\sim 3.5\sigma$ (with e^+e^- data; 2.3σ with tau data). Is it NP? Sep 2012: CD0 approval for new g-2 exp! KLOE new measure presented: it agrees with KLOE 08 & 10! Future of LBL?
- ➌ Could Δa_μ be due to mistakes in the hadronic $\sigma(s)$? Very unlikely. Also, given a 125 GeV SM Higgs, these hypothetical shifts $\Delta\sigma(s)$ could only occur at very low energies (below $\sim 1\text{GeV}$).
- ➍ The sensitivity of the electron g-2 has improved! It may soon be possible to test whether Δa_μ manifests itself in the electron g-2. A robust and ambitious exp program is needed to improve α & a_e .
- ➎ The tau g-2 is essentially unknown: we propose to measure it at Belle II via its radiative leptonic decays.

The End