The spherical sector of the classical rational Calogero model and its integrals of motion are studied using the matrix model description. A diagrammatic technique, which allows to find explicit expressions of the constants of motion is presented. The relation with valence-bond singlet states of quantum spins is discussed.