


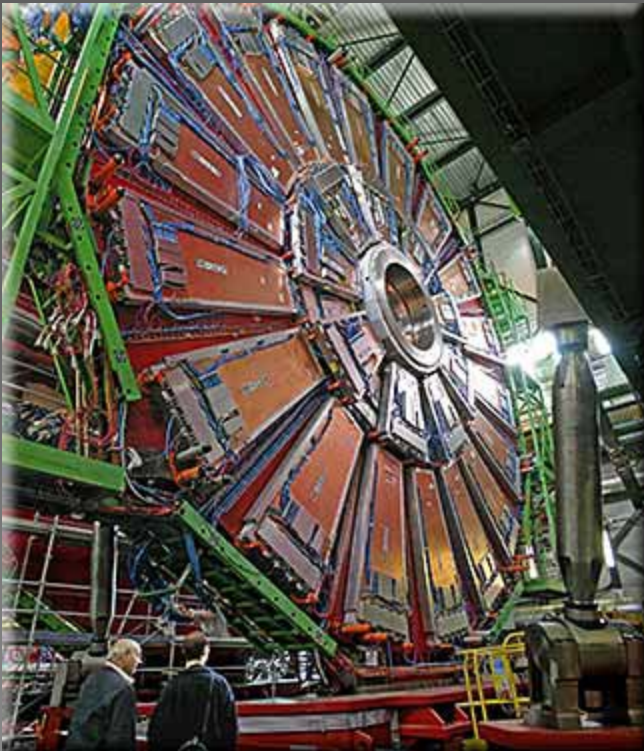
Minimal Supersymmetric Standard Model

Collider physics, constrained
MSSM, Neutrino masses

Y. Farzan

LHC

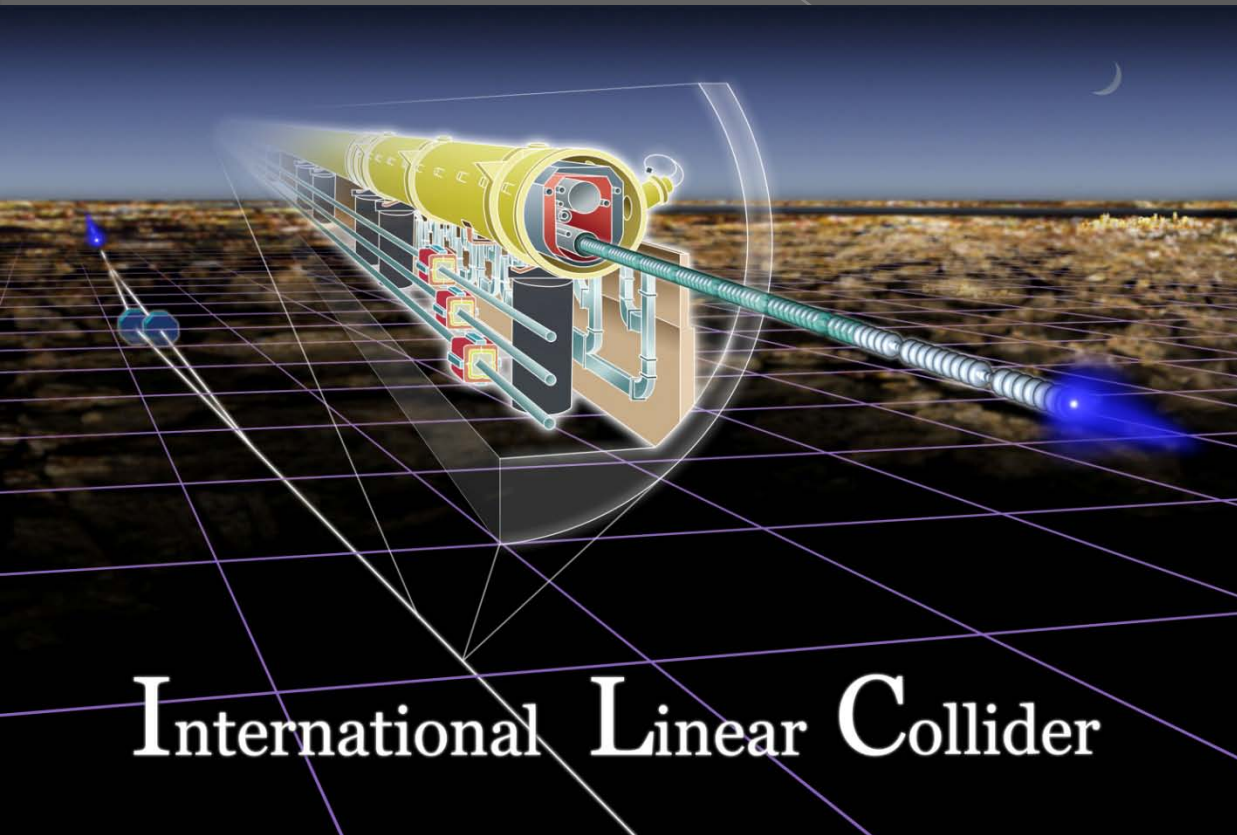
Currently running: LHC 
Large Hadron Collider 
Proton Proton collider 



ILC

Proposal level 

<http://www.linearcollider.org>



Electron positron collider

TESLA + NLC  ILC

International Linear Collider

Simple process at ILC

$$e^+ e^- \rightarrow \tilde{\mu}^+ \tilde{\mu}^-$$

What is the diagram? 

$$\frac{d\sigma}{d\cos\theta} = \frac{\pi\alpha^2}{2s} \beta^3 \sin^2\theta |f_{ab}|^2$$

$$f_{ab} = 1 + \frac{(I_e^3 + \frac{1}{2}s_w^2)(I_\mu^3 + \frac{1}{2}s_w^2)}{c_w^2 s_w^2} \frac{s}{s - m_Z^2}$$

$$I^3 = -\frac{1}{2}, 0 \text{ for } a, b = L, R$$

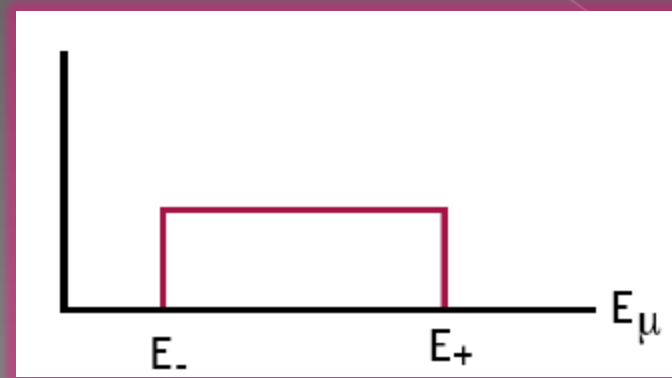
$$|f_{ab}|^2 = \begin{array}{ll} e_R^- \rightarrow \tilde{\mu}^- & : 1.69 \quad e_R^- \rightarrow \tilde{\mu}^+ & : 0.42 \\ e_L^- \rightarrow \tilde{\mu}^- & : 0.42 \quad e_L^- \rightarrow \tilde{\mu}^+ & : 1.98 \end{array}$$

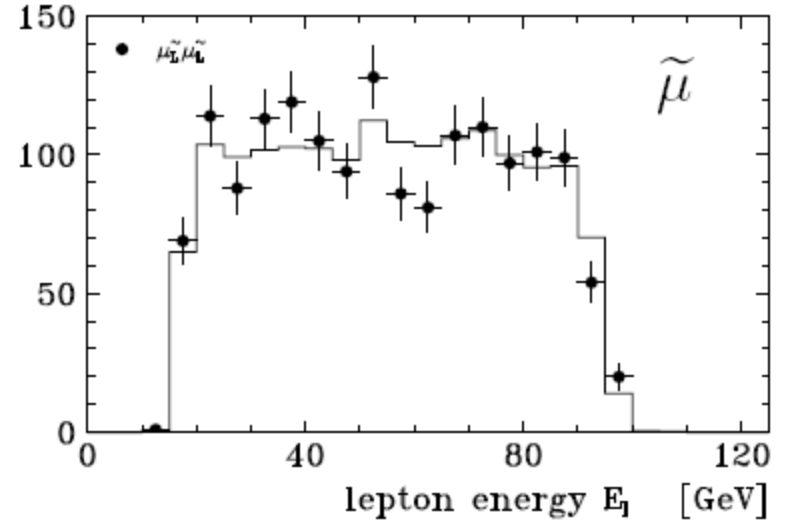
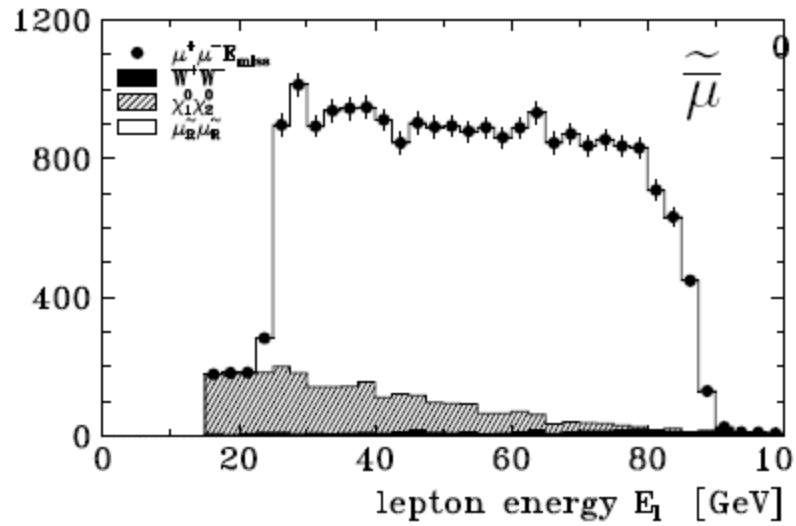
Signal

$$e^+e^- \rightarrow \tilde{\mu}^+\tilde{\mu}^-$$


$$\tilde{\mu} \rightarrow \mu N_1^0$$

$$e^+e^- \rightarrow \mu^+\mu^- + (\text{missing } E \text{ and } p)$$






Blair and Martyn

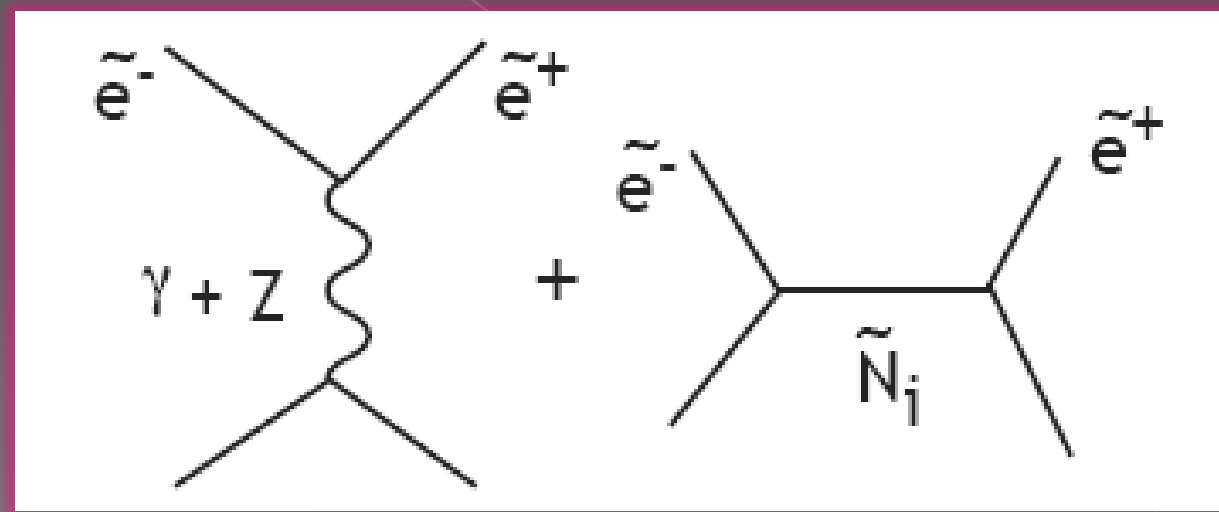
How do you guess the argument will  change?

$$e^+ e^- \rightarrow \tilde{\tau}^+ \tilde{\tau}^-$$

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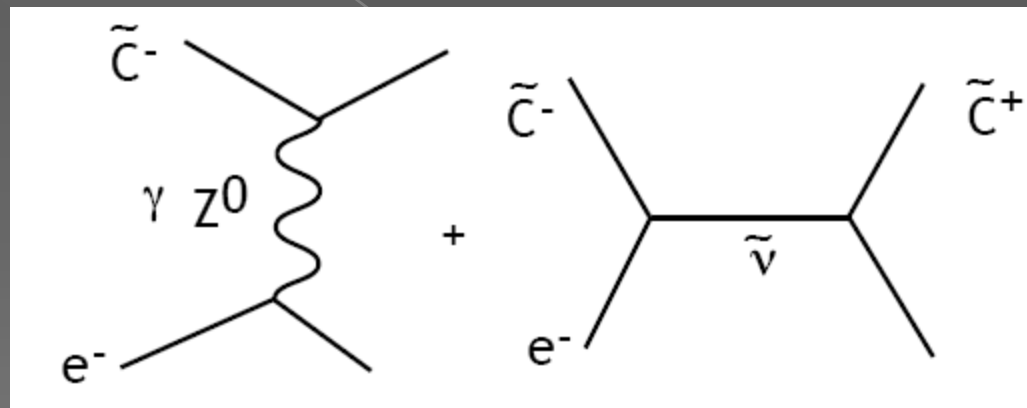
$$e^+ e^- \rightarrow \tilde{e}^- \tilde{e}^+.$$

Both s-channel and t-channel contributions



Chargino and neutralino pair production at ILC

$$e^+e^- \rightarrow C_k^+ C_\ell^- , N_i N_j$$



$$\tilde{C}^+ \rightarrow \ell^+ \nu \tilde{N}_1 \quad \tilde{C}^- \rightarrow q \bar{q} N_1$$

Supersymmetry at LHC

$$gg \rightarrow \widetilde{g}\widetilde{g}, \widetilde{q}\widetilde{q}^* \quad gq \rightarrow \widetilde{g}\widetilde{q}$$

$$\widetilde{q} \rightarrow \bar{q}N_1^0$$

$$\begin{aligned} \widetilde{q} &\rightarrow qN_2^0 \rightarrow q(\ell^+\ell^-)N_1^0 \\ \widetilde{q} &\rightarrow u\bar{d}C_1^+ \rightarrow u\bar{d}W^+N_1^0 \end{aligned}$$

Cascade decay

$$\tilde{q} \rightarrow q\tilde{\chi}_2^0 \rightarrow ql\tilde{l} \rightarrow ql\tilde{l}\tilde{\chi}_1^0$$

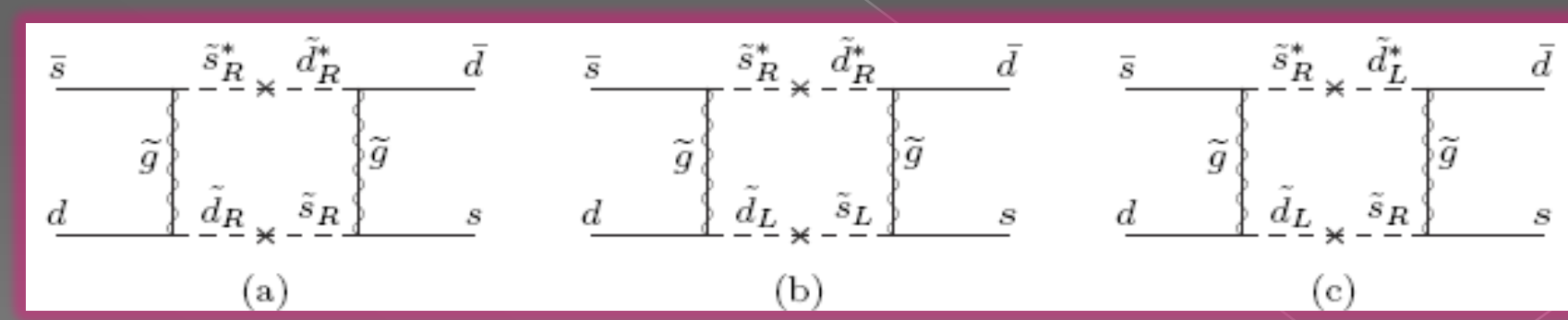
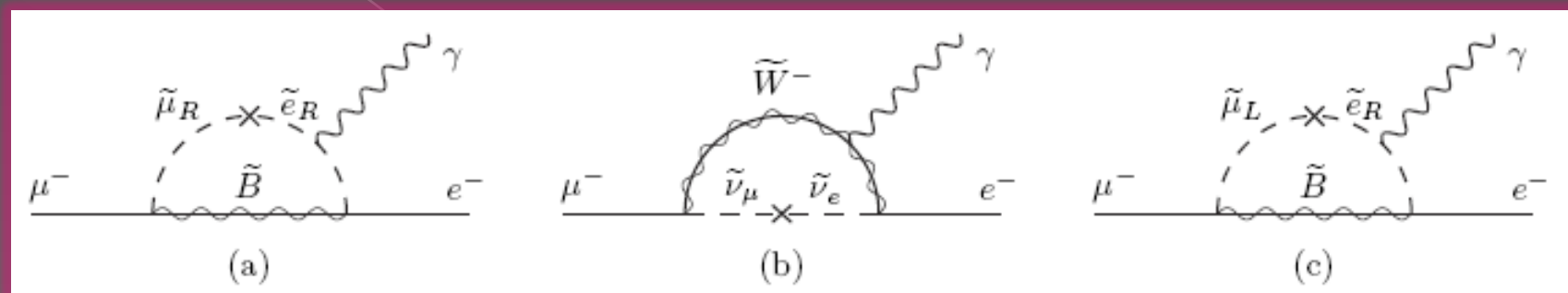
$$A \rightarrow XB \rightarrow XYC$$

$d\Gamma_A/ds$, possesses a kinematic edge located at

$$s = \frac{(m_A^2 - m_B^2)(m_B^2 - m_C^2)}{m_B^2},$$

$$s \equiv (p_X + p_Y)^2$$

Flavor violation



$$K^0 \leftrightarrow \bar{K}^0$$

Bounds

No (significant) deviation from SM 

$$b \rightarrow s\gamma$$

$$K^0 \leftrightarrow \bar{K}^0$$

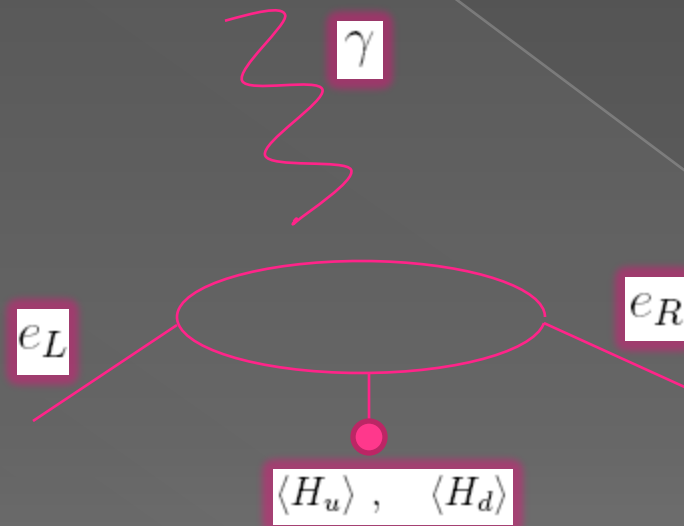
No **new** source of flavor violation

~~$$\tau \rightarrow e\gamma \quad \tau \rightarrow \mu\gamma$$~~

~~$$\mu^- \rightarrow e^- \gamma \quad \mu^- \rightarrow e^- e^+ e^-$$~~

~~$$\mu^- N \rightarrow e^- N \quad \tau^- \rightarrow e^- \gamma$$~~

Electric dipole moment of the electron



$$d_e \propto \Im[\mathcal{M}]$$

$$d_e < 1.4 \times 10^{-27} e \text{ cm}$$

$$A_e \tilde{e}_R \tilde{e}_L H_d \quad \mu \tilde{e}_R \tilde{e}_L H_u^*$$

Bounds on the phases of A_e and μ

mSUGRA or Constrained MSSM

$$m_0 \quad m_{1/2} \quad a_0 \quad \text{sgn}[\mu] \quad \tan \beta$$

$$M_1 = M_2 = M_3 = m_{1/2}$$

$$m_{\tilde{l}_R}^2 = m_{\tilde{l}_L}^2 = m_{\tilde{q}_R}^2 = m_{\tilde{q}_L}^2 = m_0^2 \mathbb{I}_{3 \times 3}$$

$$m_{H_u}^2 = m_{H_d}^2 = m_0^2$$

$$A_\ell = a_0 Y_\ell \quad A_U = a_0 Y_U \quad A_D = a_0 Y_D$$

No source of flavor violation

No new source of CP-violation

No source of LFV

How neutrino masses are supposed to be explained? ○

In the context of SUSY: ○

R-parity violation ○

Seesaw mechanism embedded in SUSY ○

R-parity violation

$$\mathcal{W}_Y = \epsilon_{\alpha\beta} \left(Y_U^{ij} \widehat{Q}_i^\alpha \widehat{u}_j^c \widehat{H}_u^\beta + Y_D^{ij} \widehat{Q}_i^\beta \widehat{d}_j^c \widehat{H}_d^\alpha + Y_l^{ij} \widehat{L}_i^\beta \widehat{l}_j^c \widehat{H}_d^\alpha \right)$$

$$\mathcal{W}_{bR_p} = \mathcal{W}_Y + \epsilon_{\alpha\beta} \left[\epsilon_i \widehat{L}_i^\alpha \widehat{H}_u^\beta - \mu \widehat{H}_d^\alpha \widehat{H}_u^\beta \right]$$

$$\mathcal{W}_{\mu\nu\text{SSM}} = \mathcal{W}_Y + \epsilon_{\alpha\beta} \left[Y_\nu^i \widehat{L}_i^\alpha \widehat{\nu}^c \widehat{H}_u^\beta - \lambda \widehat{\nu}^c \widehat{H}_d^\alpha \widehat{H}_u^\beta \right] + \frac{1}{3} \kappa \widehat{\nu}^c \widehat{\nu}^c \widehat{\nu}^c$$

Neutrino mass at tree level

$$(\psi^0)^T = (\tilde{B}^0, \tilde{W}_3^0, \tilde{H}_d^0, \tilde{H}_u^0, \nu^c, \nu_1, \nu_2, \nu_3)$$

$$\mathcal{M}_n = \begin{pmatrix} M_H & \hat{m} \\ \hat{m}^T & 0 \end{pmatrix}$$

$$M_H = \begin{pmatrix} M_1 & 0 & -\frac{1}{2}g'v_d & \frac{1}{2}g'v_u & 0 \\ 0 & M_2 & \frac{1}{2}gv_d & -\frac{1}{2}gv_u & 0 \\ -\frac{1}{2}g'v_d & \frac{1}{2}gv_d & 0 & -\mu & -\frac{1}{\sqrt{2}}\lambda v_u \\ \frac{1}{2}g'v_u & -\frac{1}{2}gv_u & -\mu & 0 & -\frac{1}{\sqrt{2}}\lambda v_d \\ 0 & 0 & -\frac{1}{\sqrt{2}}\lambda v_u & -\frac{1}{\sqrt{2}}\lambda v_d & \sqrt{2}\kappa v_c \end{pmatrix}$$

$$\hat{m}^T = \begin{pmatrix} -\frac{1}{2}g'v_1 & \frac{1}{2}gv_1 & 0 & \epsilon_1 & \epsilon_1 \frac{v_u}{v_c} \\ -\frac{1}{2}g'v_2 & \frac{1}{2}gv_2 & 0 & \epsilon_2 & \epsilon_2 \frac{v_u}{v_c} \\ -\frac{1}{2}g'v_3 & \frac{1}{2}gv_3 & 0 & \epsilon_3 & \epsilon_3 \frac{v_u}{v_c} \end{pmatrix}$$

Seesaw mechanism

Adding right-handed neutrino: N 

Superpotential:

$$W = -Y_{\nu}^{ij} \epsilon_{\alpha\beta} H_{u\alpha} N_i L_{j\beta} + \frac{M_{ij}}{2} N_i N_j$$

New terms in the soft susy breaking potential

Sneutrino mass term: $m_0^2 \tilde{N}_i^\dagger \tilde{N}_i$

Neutrino A-term: $a_0 Y_\nu^{ij} \epsilon_{\alpha\beta} H_{u\alpha} \tilde{N}_i \tilde{L}_{j\beta}$

Neutrino B-term: $\frac{B_\nu M_i}{2} \tilde{N}_i \tilde{N}_i$

One should worry about LFV again. 