

# Baryon asymmetry of the Universe

## experiment and theory





$$(i\gamma^\mu \partial_\mu - m)\psi = 0$$

Paul Dirac



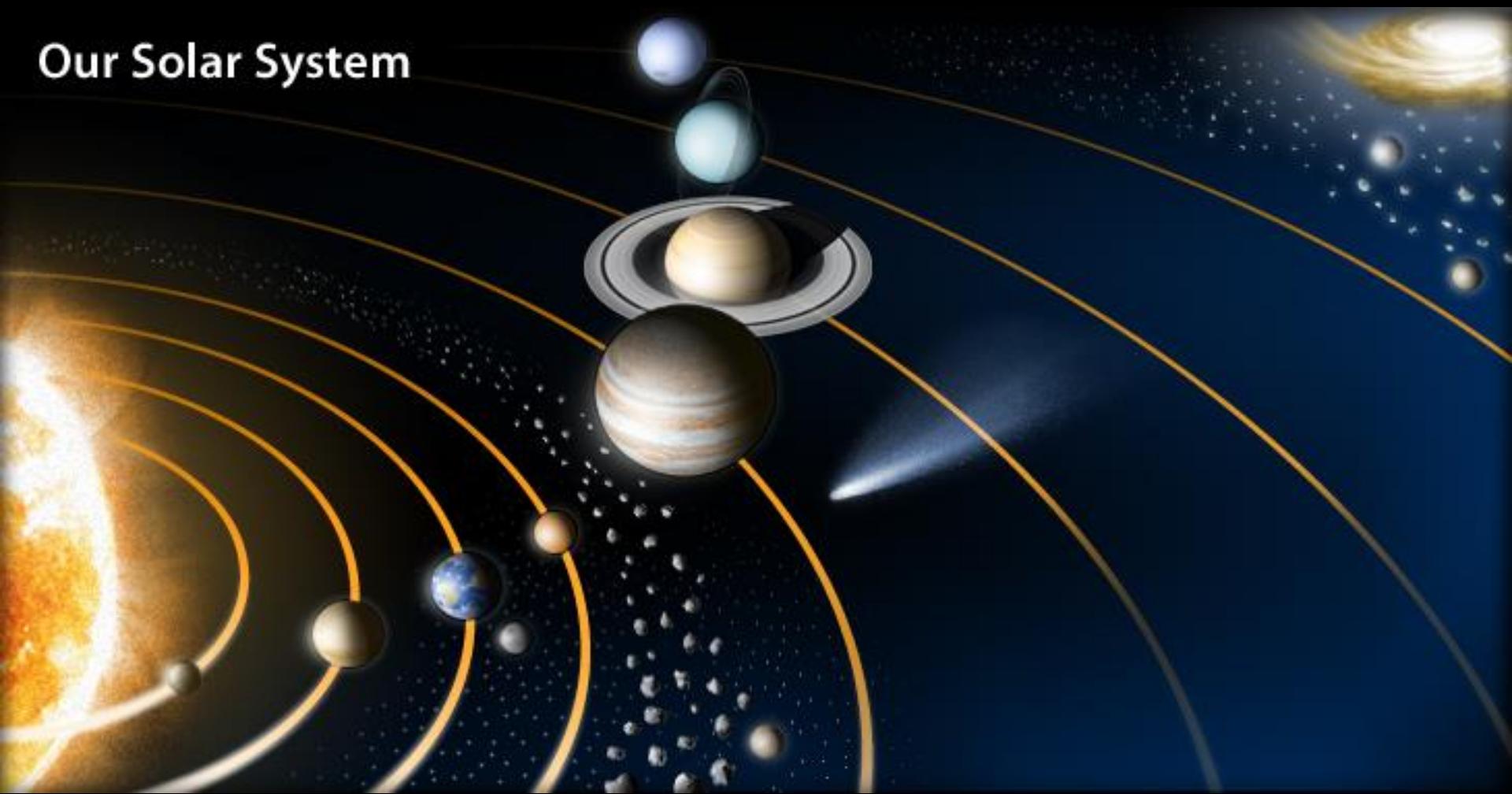
Carl Anderson

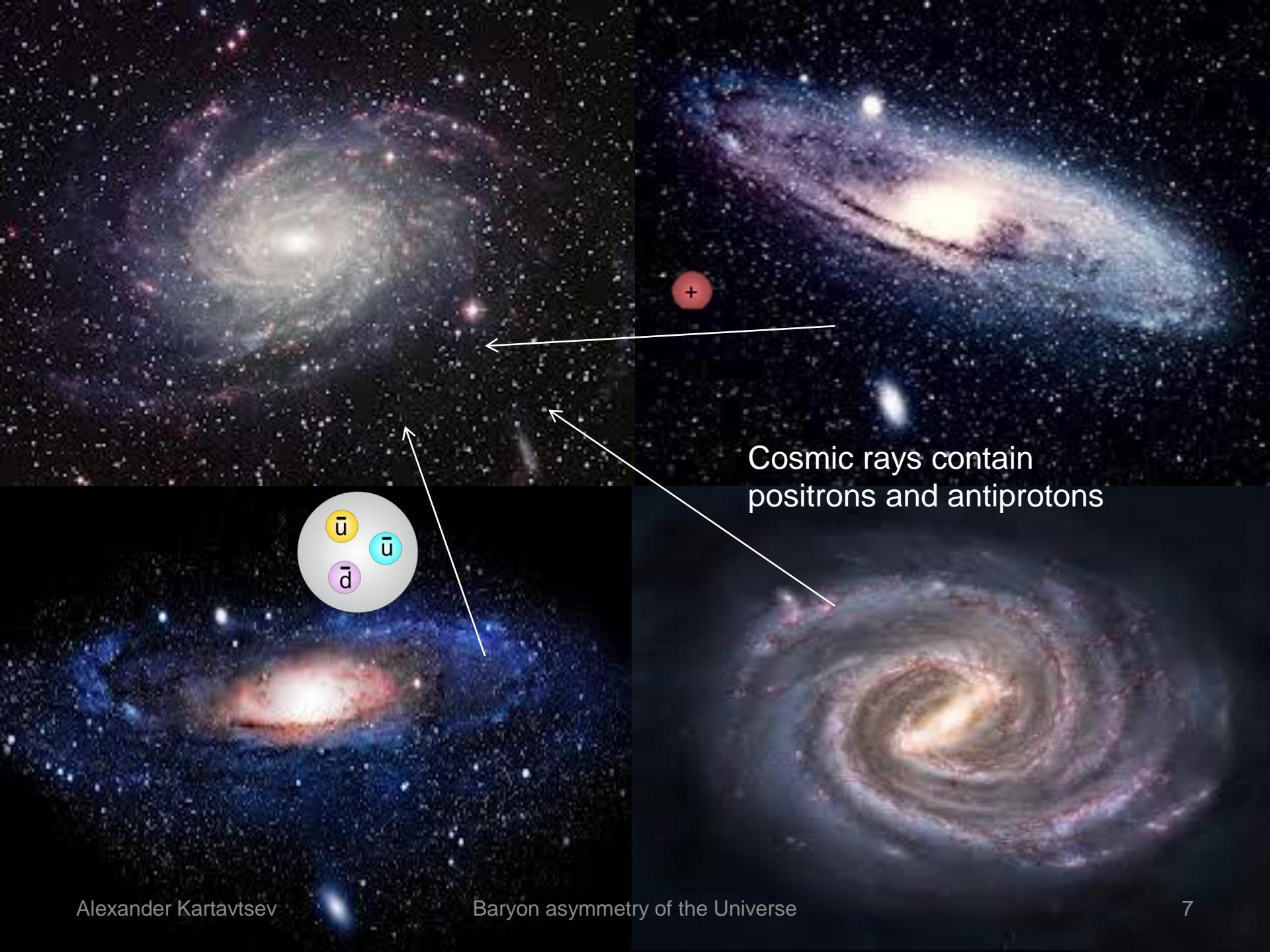


# Angels and demons



# Our Solar System



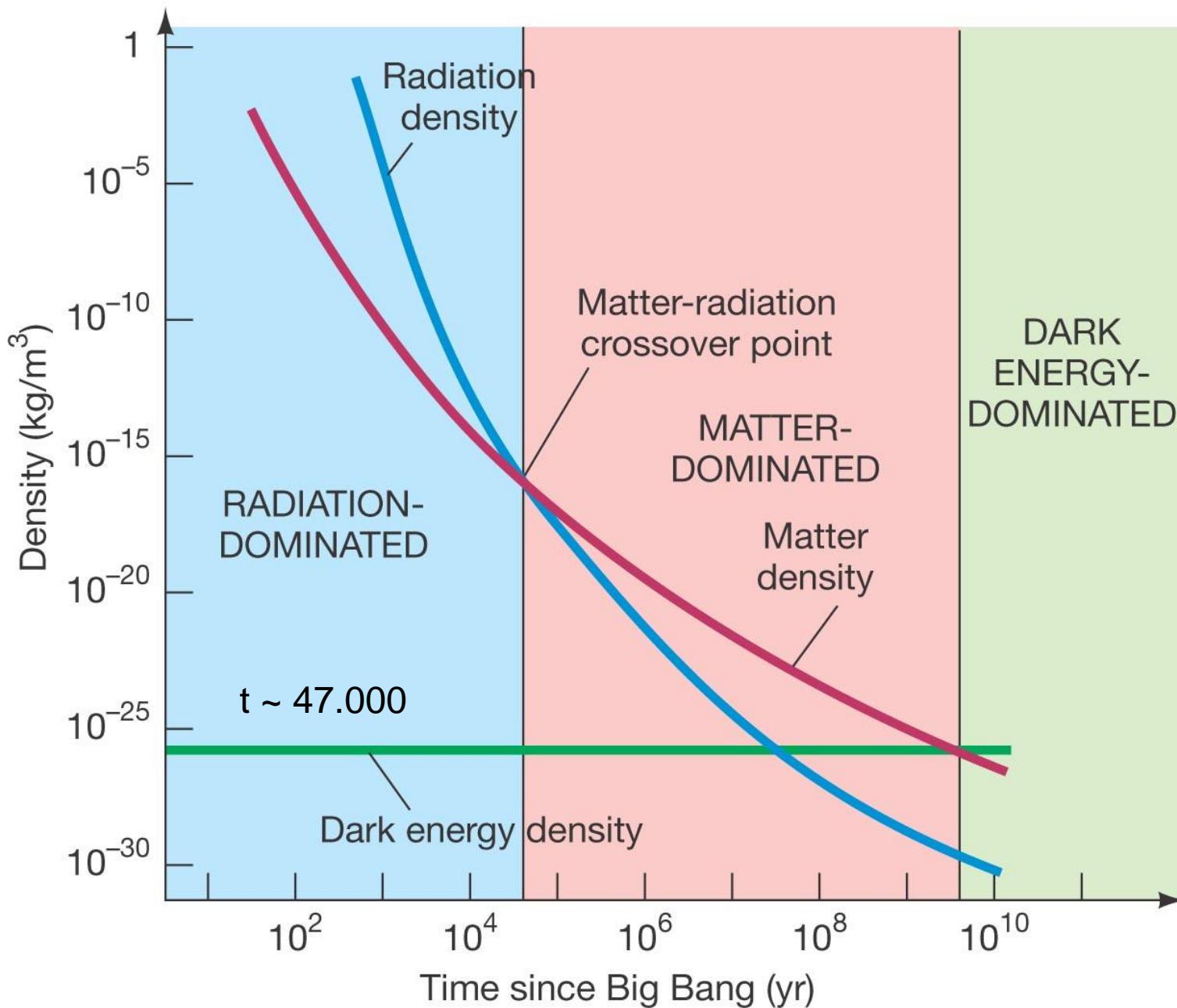


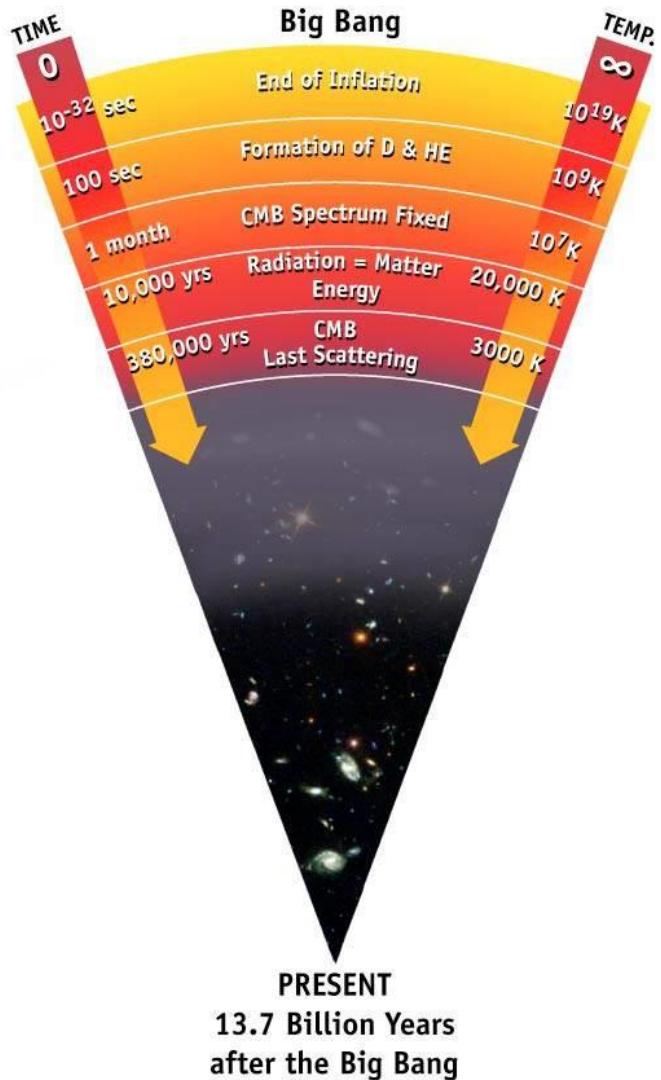
# Why is the Universe baryonically asymmetric ?

# Outline

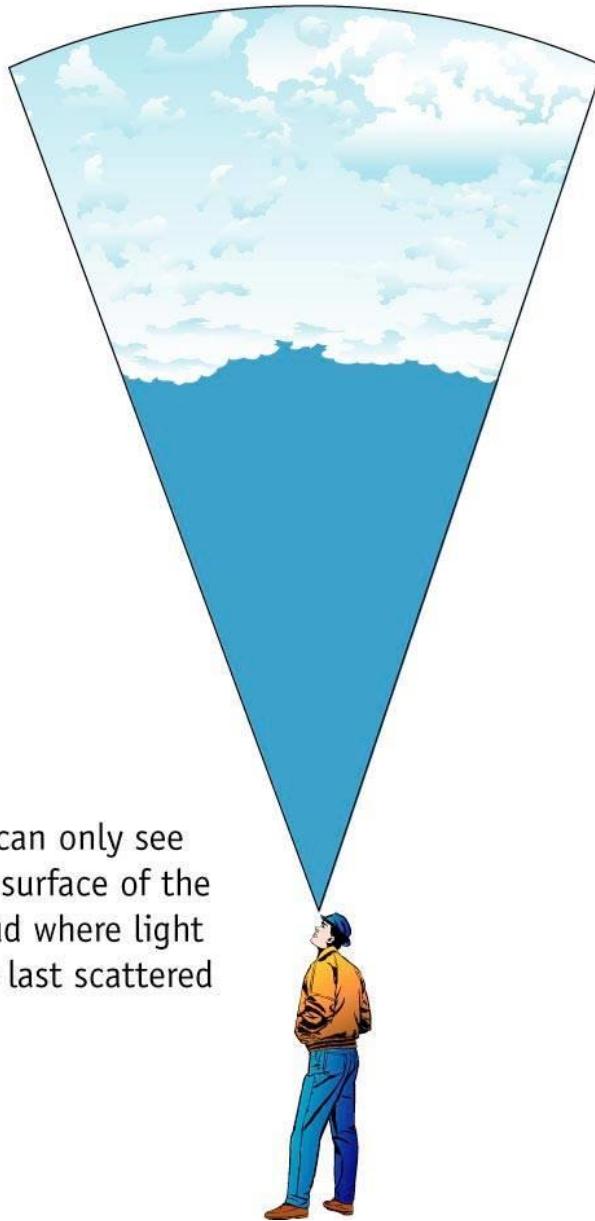
- Experimental evidence
  - Cosmic Microwave Background
  - Big Bang Nucleosynthesis
- Theoretical interpretation
  - Baryon number violation
  - Baryogenesis via leptogenesis

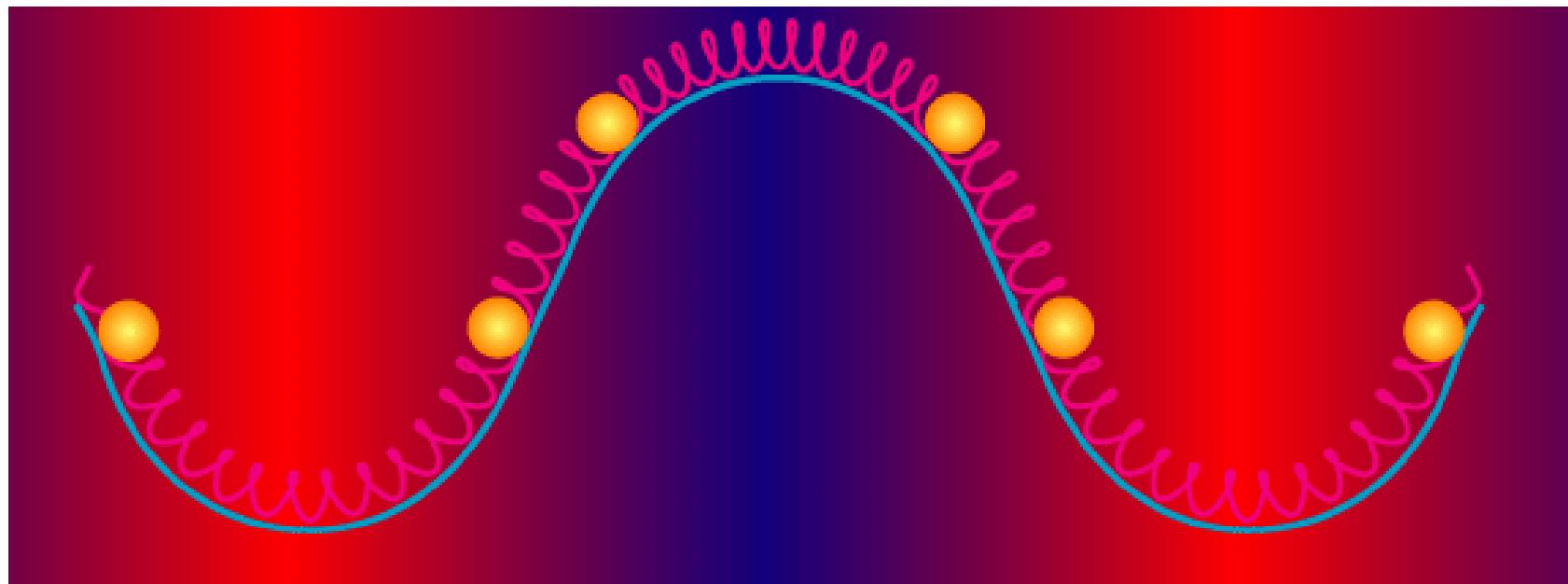
# Cosmic microwave background

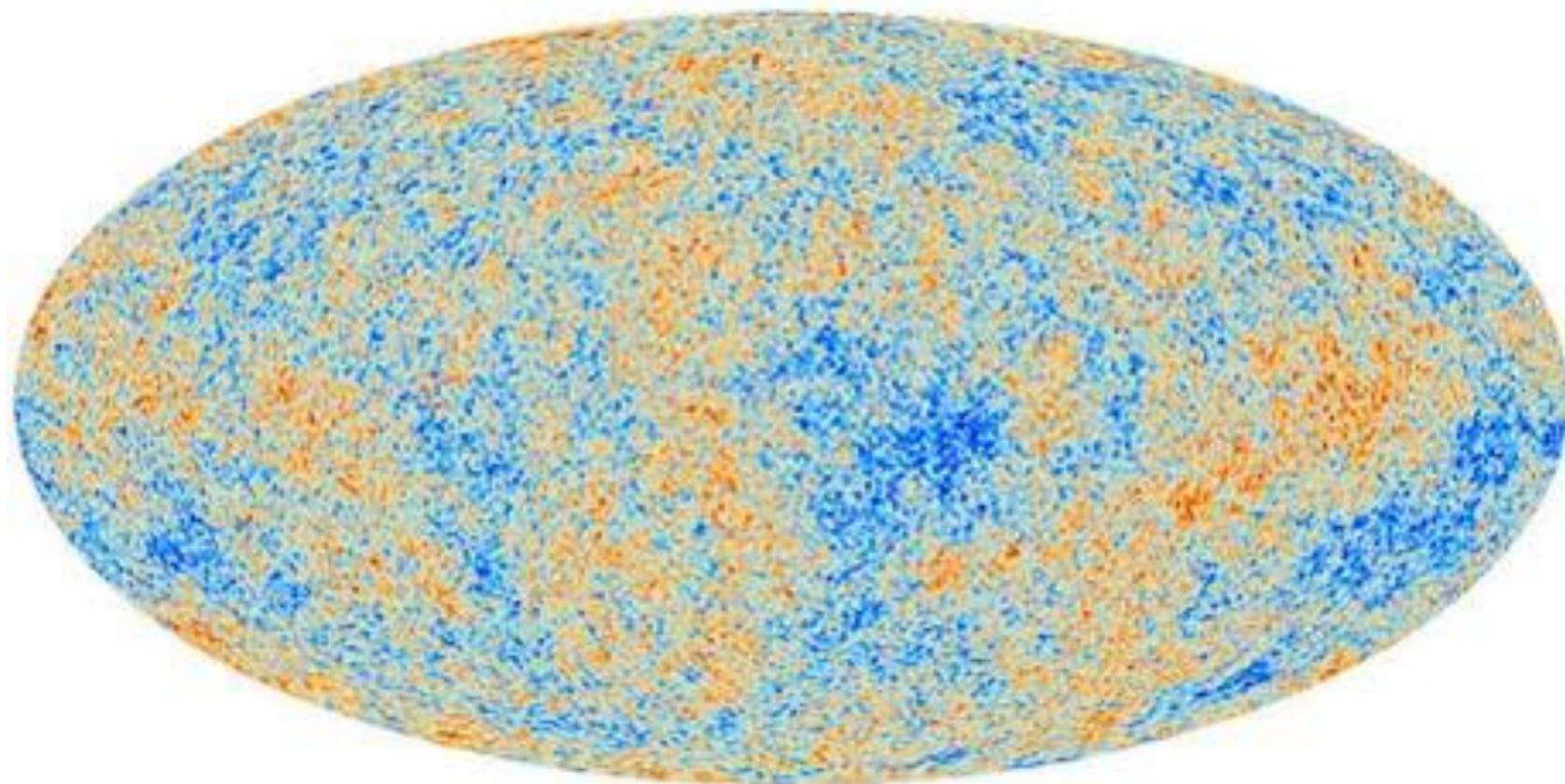




The cosmic microwave background Radiation's "surface of last scatter" is analogous to the light coming through the clouds to our eye on a cloudy day.



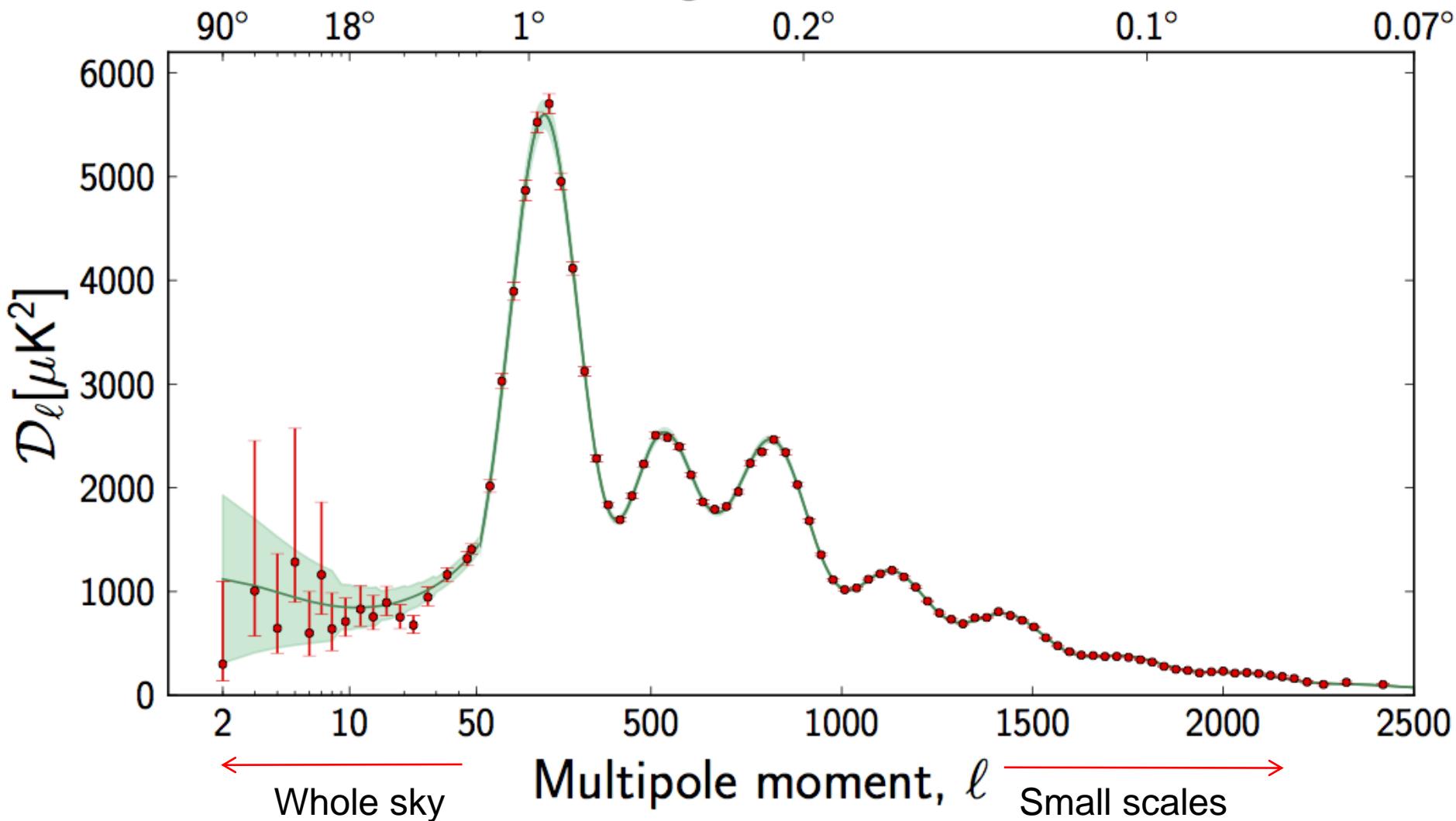


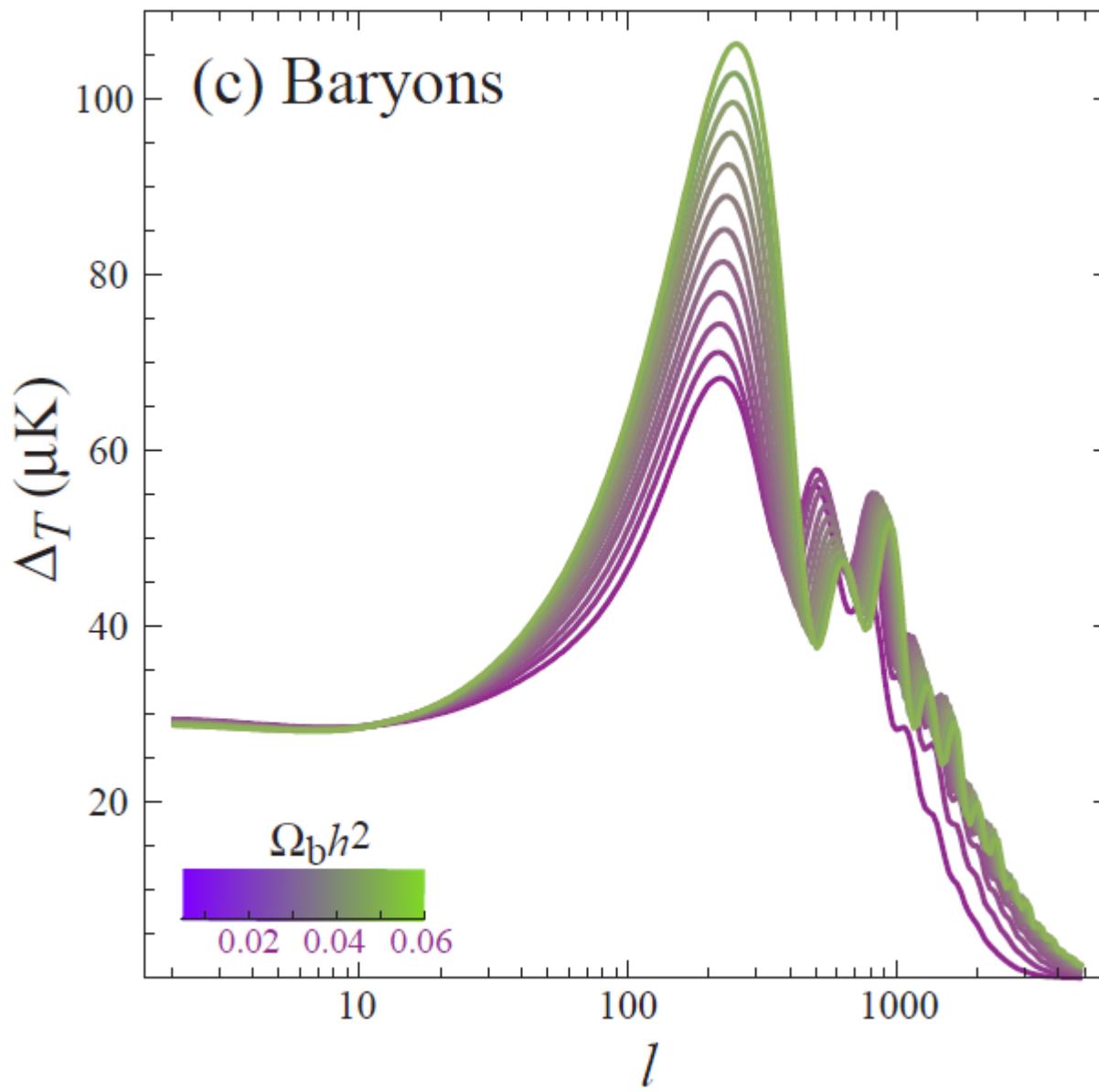


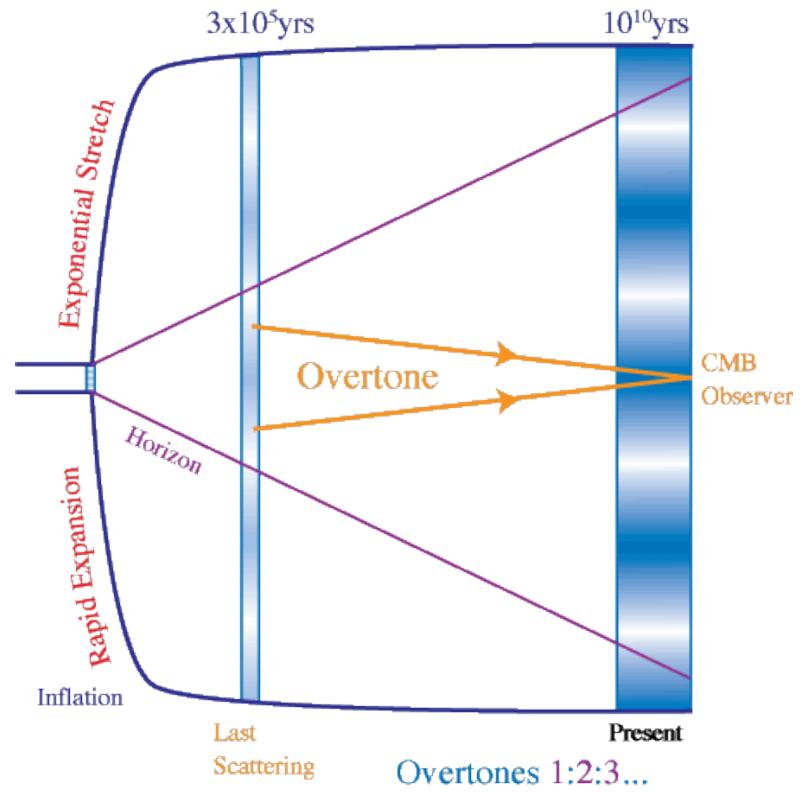
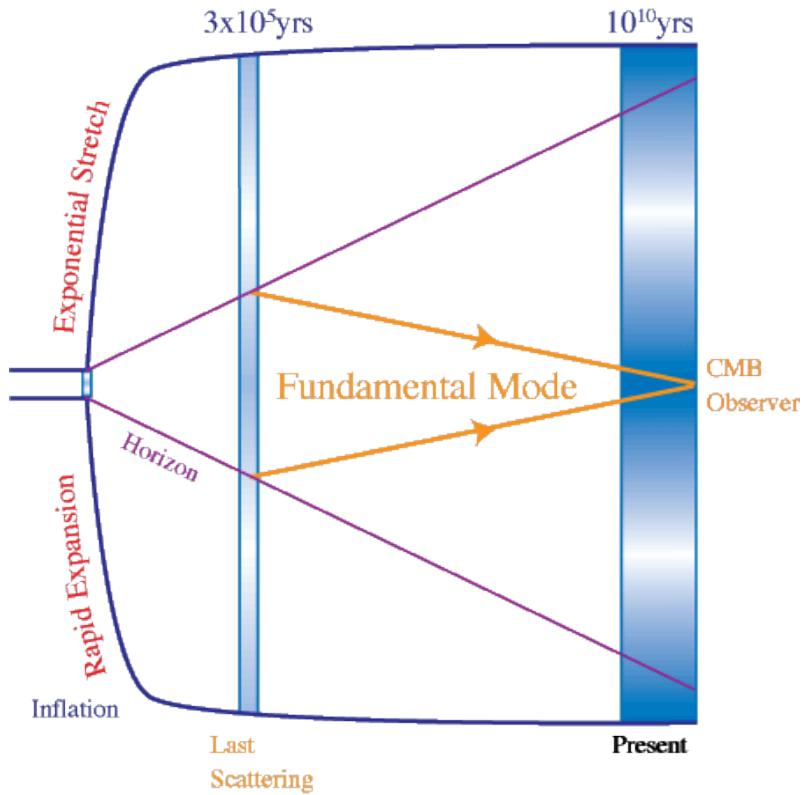
$$T(\theta, \phi) = \sum_{l,m} a_{lm} Y_l^m(\theta, \phi)$$

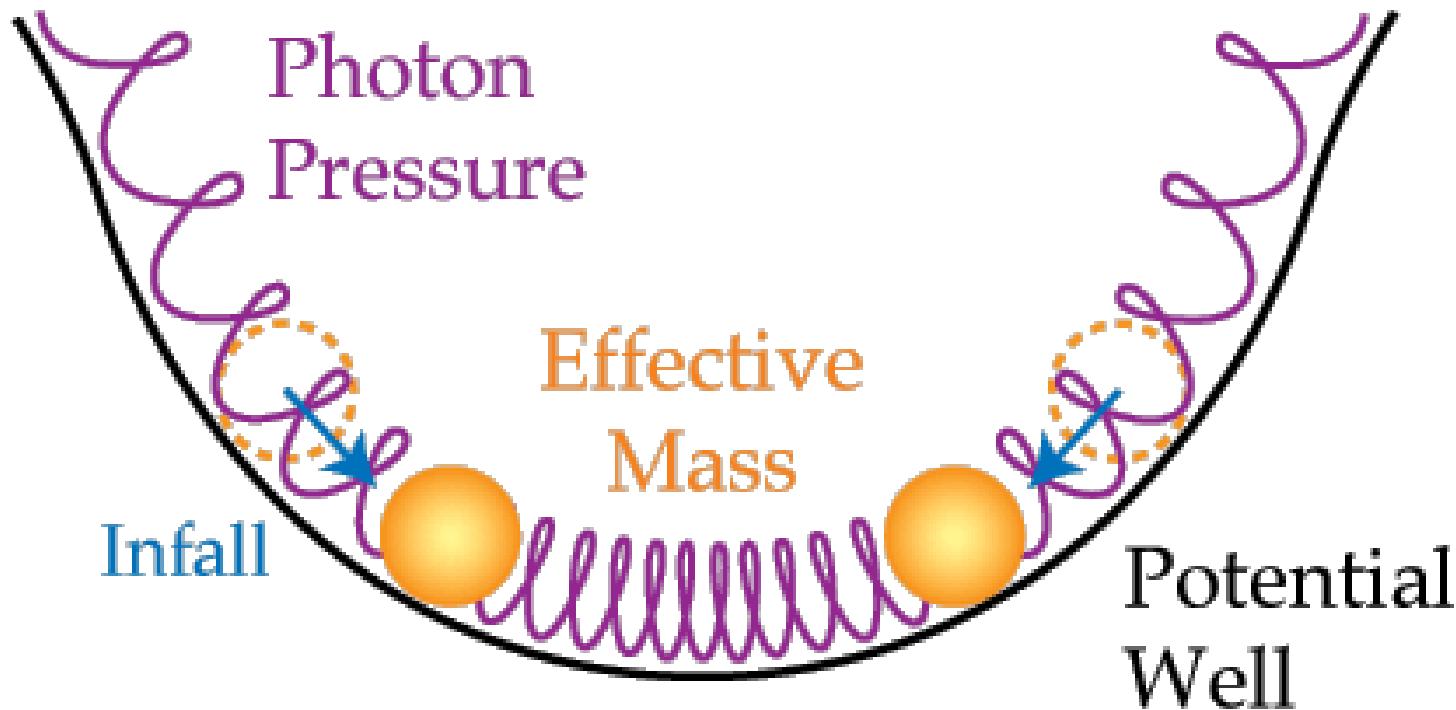
$$C_l = \langle a_{lm} a_{lm}^* \rangle_m$$

## Angular scale



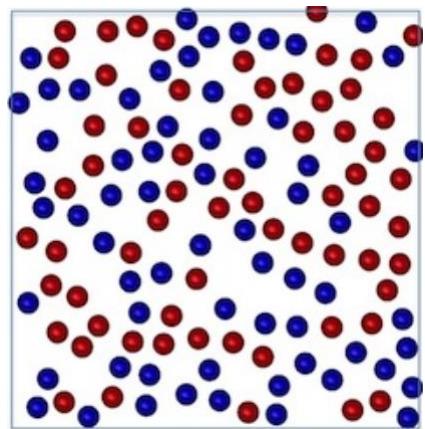






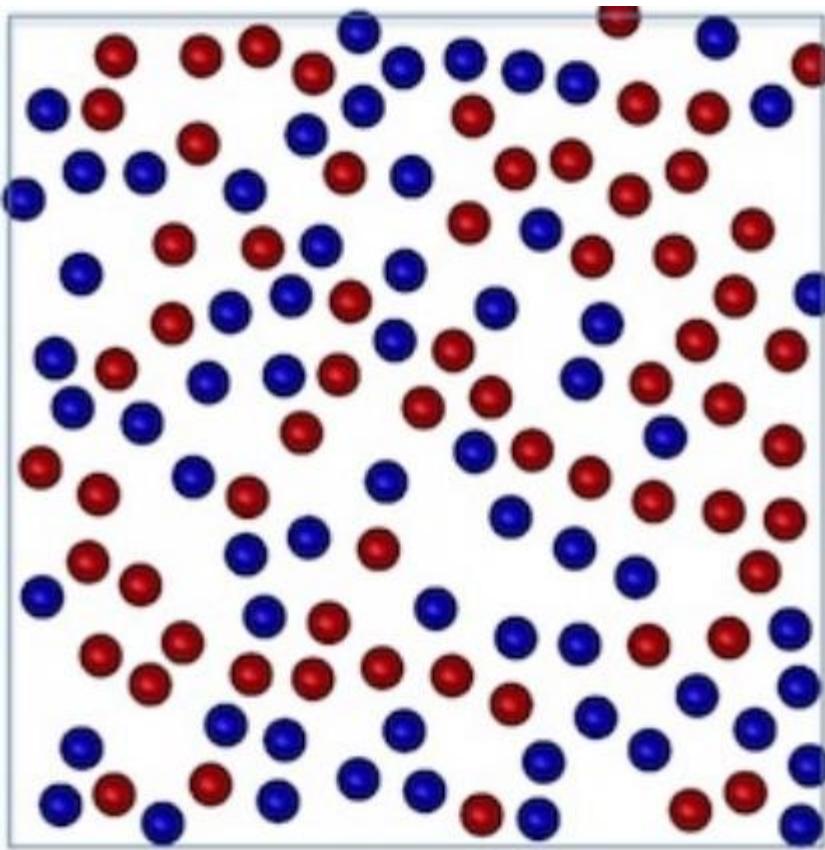
$$\eta = (6.19 \pm 0.14) \times 10^{-10}$$

$$\eta_B/\eta_\gamma = \text{const.}$$



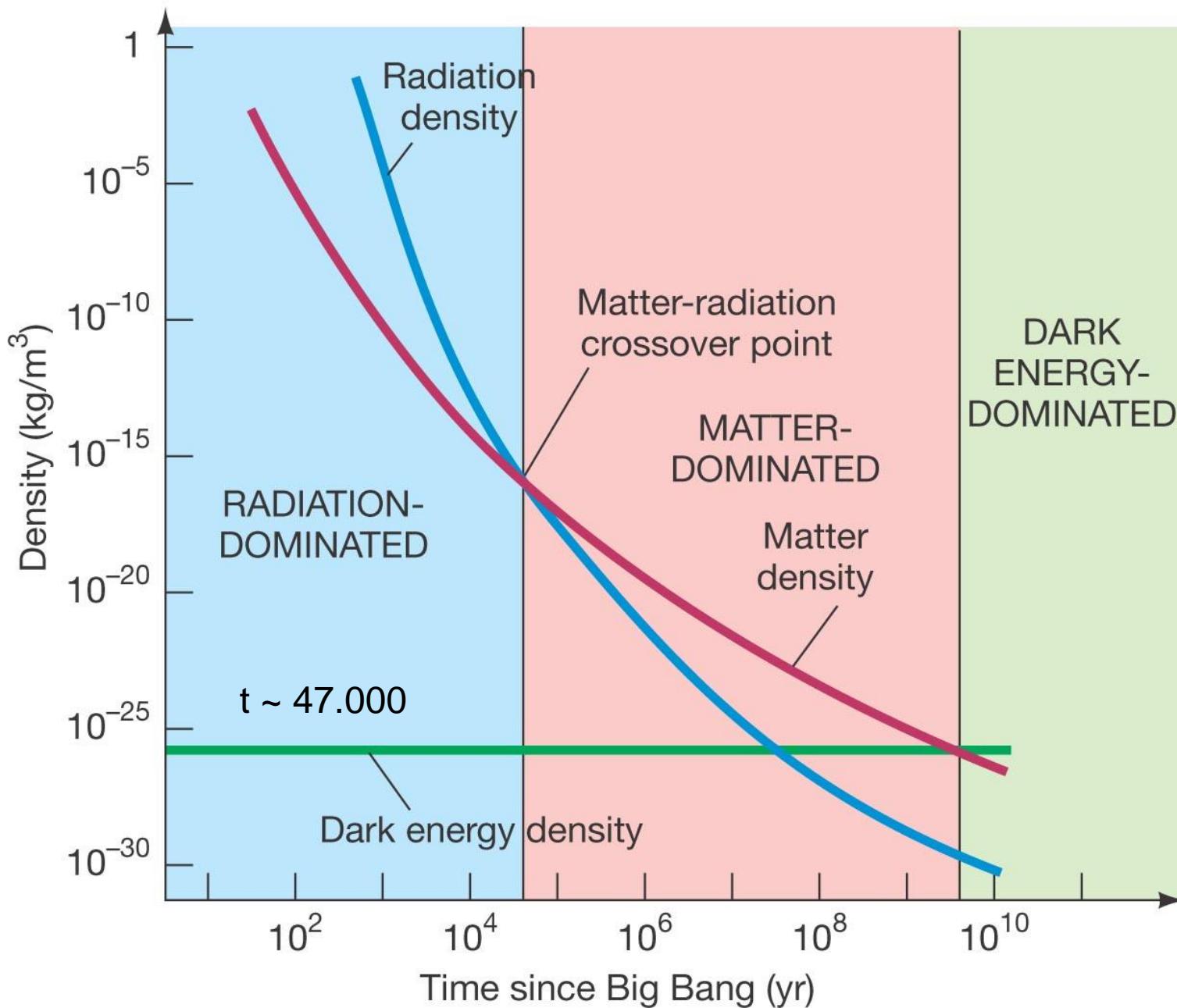
Comoving volume,  $t=t_0$

time  
→



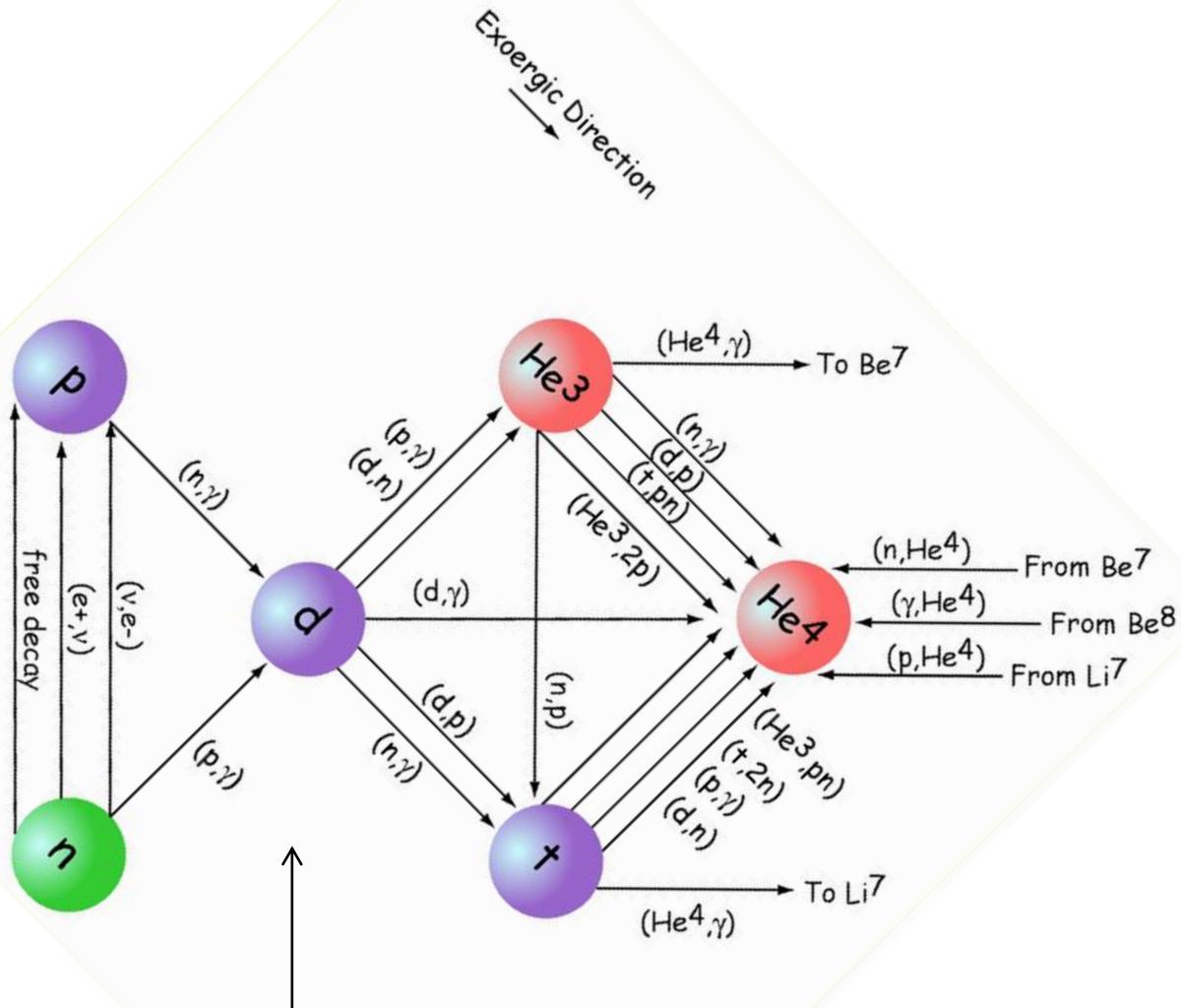
Comoving volume,  $t=t_1$

# Big Bang nucleosynthesis

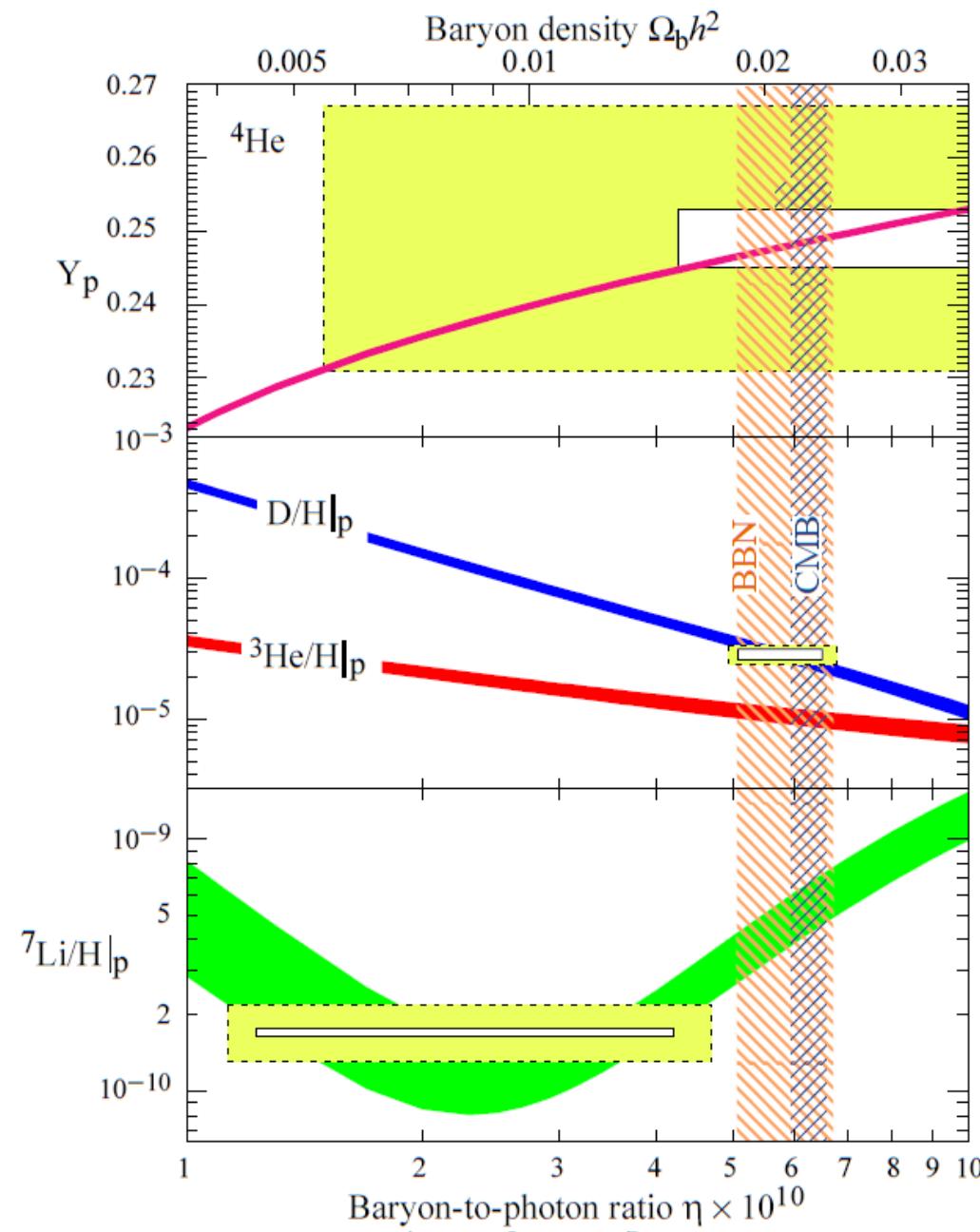


$t \sim 3$  min

$$T \sim 10^{10} \text{ K}$$



Deuterium bottleneck =  $\eta$  dependence

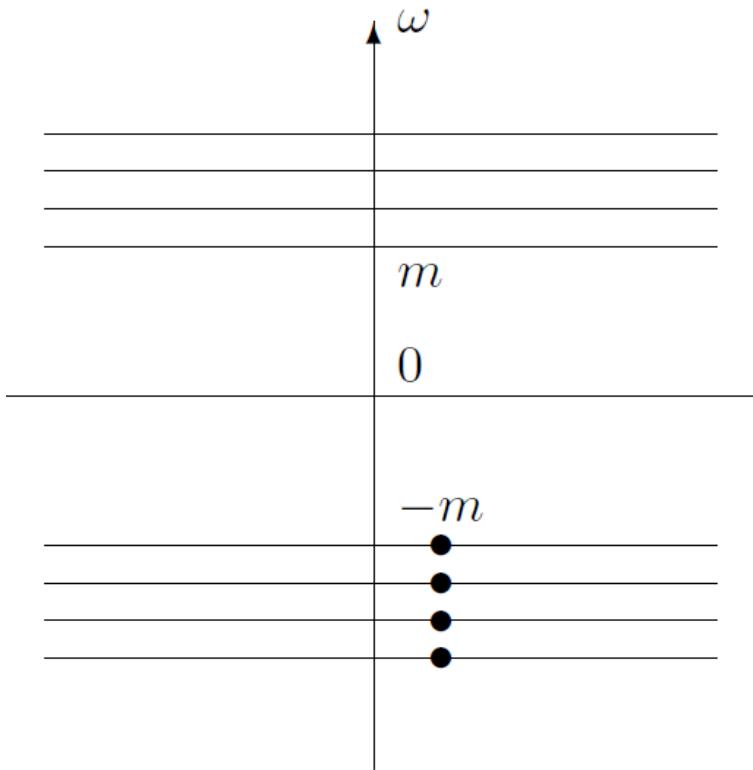


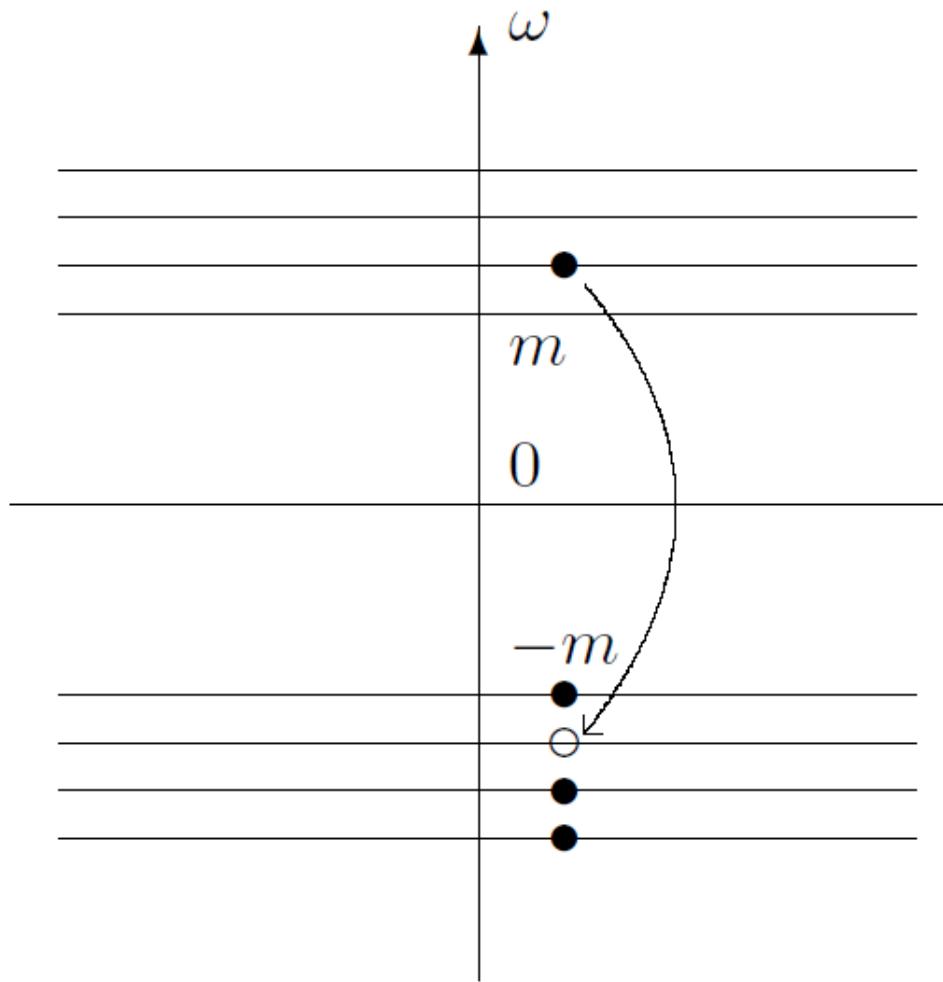
# Intermediate summary I

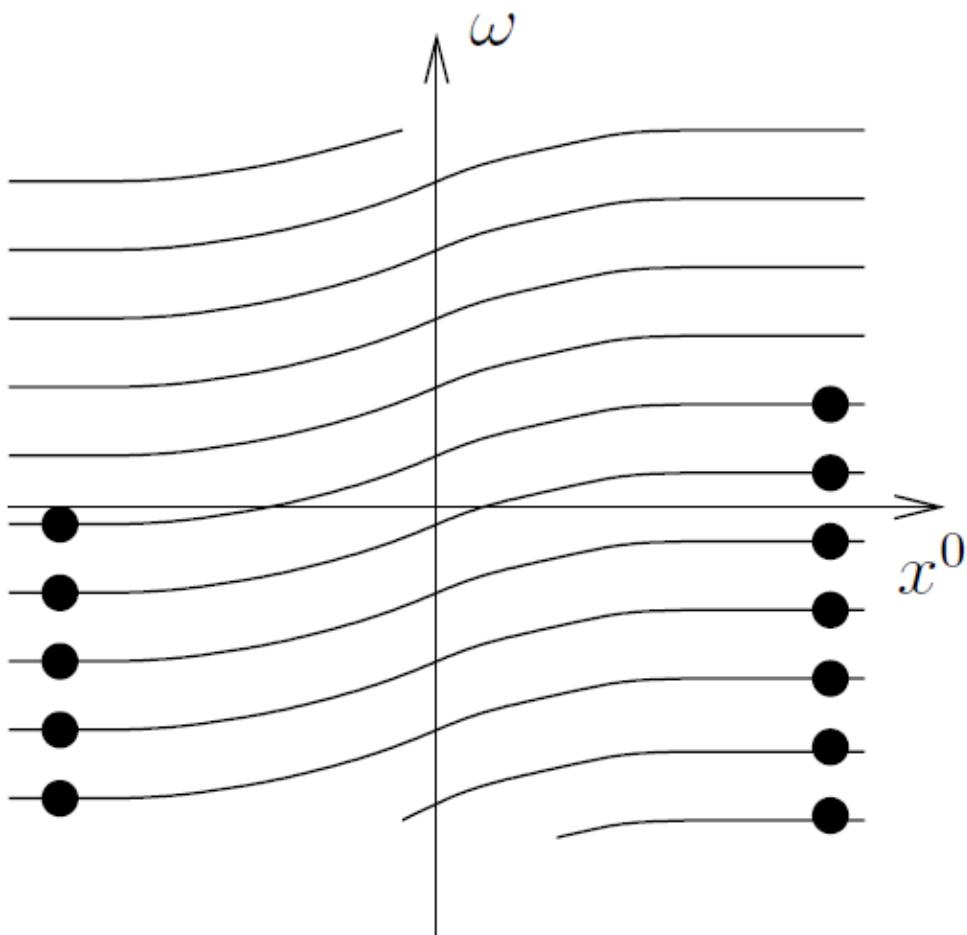
- Antimatter is a rare commodity nowadays
- Baryon to photon ratio:  $\eta \approx 6.2 \times 10^{-10}$
- $\eta_{\text{BBN}}$  is consistent with  $\eta_{\text{CMB}}$

# Why is the Universe baryonically asymmetric ?

# Baryon number violation

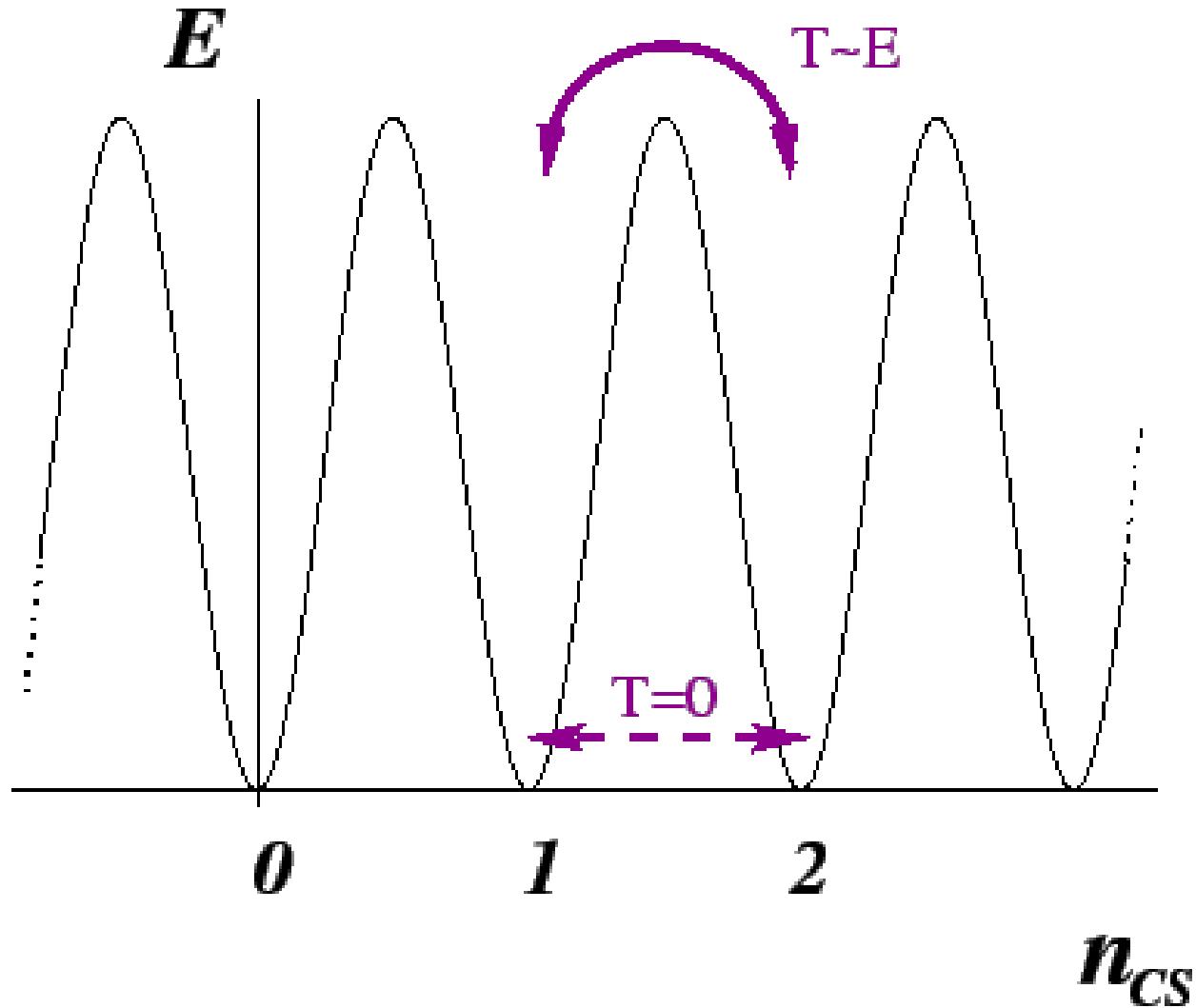






$n \neq \phi + e^+ \bar{\nu}$

$t \sim 10^{146}$  years

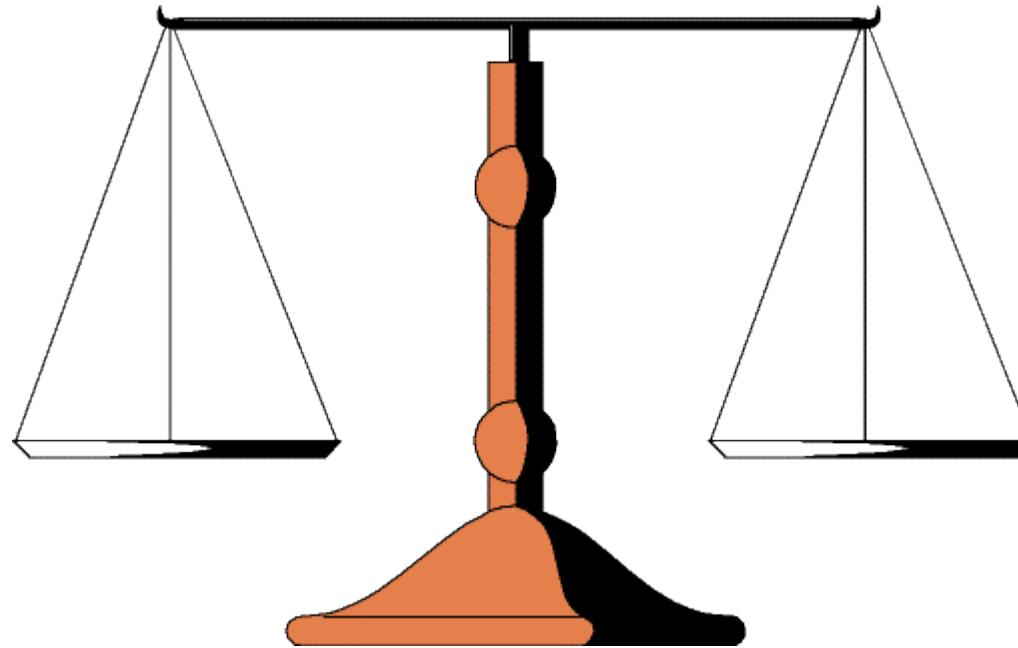


# Baryogenesis via leptogenesis

$B-L=\text{const.}$



Masataka Fukugita



sphaleron scales



Tsutomu Yanagida

# of Matter (Fermions) spin $\frac{1}{2}$

	I	II	III	
mass →	2.4 MeV	1.27 GeV	173.2 GeV	
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	
name →	Left <b>u</b> up	Left <b>c</b> charm	Left <b>t</b> top	Left <b>g</b> gluon
Quarks	$4.8 \text{ MeV}$ $-\frac{1}{3}$ <b>d</b> down	$104 \text{ MeV}$ $-\frac{1}{3}$ <b>s</b> strange	$4.2 \text{ GeV}$ $-\frac{1}{3}$ <b>b</b> bottom	$0$ $0$ <b><math>\gamma</math></b> photon
Leptons	$0$ $\nu_e$ Left electron neutrino	$0$ $\nu_\mu$ Left muon neutrino	$0$ $\nu_\tau$ Left tau neutrino	$91.2 \text{ GeV}$ $0$ <b><math>Z^0</math></b> weak force
	$0.511 \text{ MeV}$ $-1$ <b>e</b> electron	$105.7 \text{ MeV}$ $-1$ <b><math>\mu</math></b> muon	$1.777 \text{ GeV}$ $-1$ <b><math>\tau</math></b> tau	$126 \text{ GeV}$ $0$ <b>H</b> Higgs boson
				Bosons (Forces) spin 1
				$80.4 \text{ GeV}$ $\pm 1$ <b><math>W^+</math></b> weak force
				spin 0

	Free Fluxes + RSBL		Huber Fluxes, no RSBL	
	bfp $\pm 1\sigma$	$3\sigma$ range	bfp $\pm 1\sigma$	$3\sigma$ range
$\sin^2 \theta_{12}$	$0.302^{+0.013}_{-0.012}$	$0.267 \rightarrow 0.344$	$0.311^{+0.013}_{-0.013}$	$0.273 \rightarrow 0.354$
$\theta_{12}/^\circ$	$33.36^{+0.81}_{-0.78}$	$31.09 \rightarrow 35.89$	$33.87^{+0.82}_{-0.80}$	$31.52 \rightarrow 36.49$
$\sin^2 \theta_{23}$	$0.413^{+0.037}_{-0.025} \oplus 0.594^{+0.021}_{-0.022}$	$0.342 \rightarrow 0.667$	$0.416^{+0.036}_{-0.029} \oplus 0.600^{+0.019}_{-0.026}$	$0.341 \rightarrow 0.670$
$\theta_{23}/^\circ$	$40.0^{+2.1}_{-1.5} \oplus 50.4^{+1.3}_{-1.3}$	$35.8 \rightarrow 54.8$	$40.1^{+2.1}_{-1.6} \oplus 50.7^{+1.2}_{-1.5}$	$35.7 \rightarrow 55.0$
$\sin^2 \theta_{13}$	$0.0227^{+0.0023}_{-0.0024}$	$0.0156 \rightarrow 0.0299$	$0.0255^{+0.0024}_{-0.0024}$	$0.0181 \rightarrow 0.0327$
$\theta_{13}/^\circ$	$8.66^{+0.44}_{-0.46}$	$7.19 \rightarrow 9.96$	$9.20^{+0.41}_{-0.45}$	$7.73 \rightarrow 10.42$
$\delta_{\text{CP}}/^\circ$	$300^{+66}_{-138}$	$0 \rightarrow 360$	$298^{+59}_{-145}$	$0 \rightarrow 360$
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.50^{+0.18}_{-0.19}$	$7.00 \rightarrow 8.09$	$7.51^{+0.21}_{-0.15}$	$7.04 \rightarrow 8.12$
$\frac{\Delta m_{31}^2}{10^{-3} \text{ eV}^2}$ (N)	$+2.473^{+0.070}_{-0.067}$	$+2.276 \rightarrow +2.695$	$+2.489^{+0.055}_{-0.051}$	$+2.294 \rightarrow +2.715$
$\frac{\Delta m_{32}^2}{10^{-3} \text{ eV}^2}$ (I)	$-2.427^{+0.042}_{-0.065}$	$-2.649 \rightarrow -2.242$	$-2.468^{+0.073}_{-0.065}$	$-2.678 \rightarrow -2.252$

# Three Generations of Matter (Fermions) spin $\frac{1}{2}$

	I	II	III	
mass →	2.4 MeV	1.27 GeV	173.2 GeV	
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	
name →	u up	c charm	t top	
Quarks	d down	s strange	b bottom	
Leptons	$\nu_e$ electron neutrino	$\nu_\mu$ muon neutrino	$\nu_\tau$ tau neutrino	
	$\sim 10$ keV	$\sim$ GeV	$\sim$ GeV	
	Left Right	Left Right	Left Right	
	$e^-$ electron	$\mu^-$ muon	$\tau^-$ tau	
	0.511 MeV	105.7 MeV	1.777 GeV	
	-1	-1	-1	
	Left Right	Left Right	Left Right	

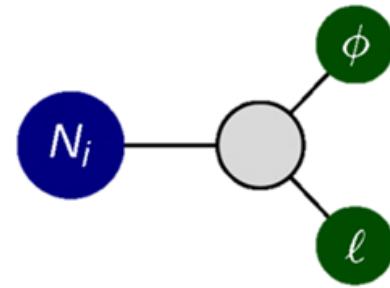
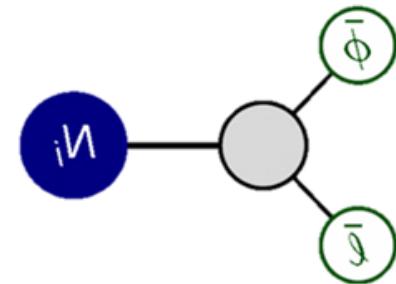
Bosons (Forces) spin 1

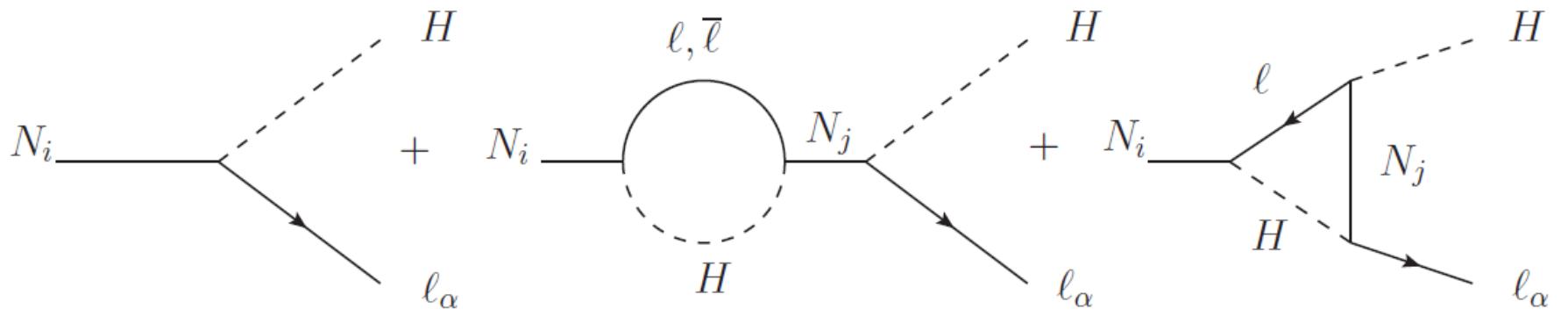
0	0	g gluon
0	0	$\gamma$ photon
91.2 GeV	0	$Z^0$ weak force
126 GeV	0	H Higgs boson
spin 0		



Right-handed neutrino

Left-handed neutrino

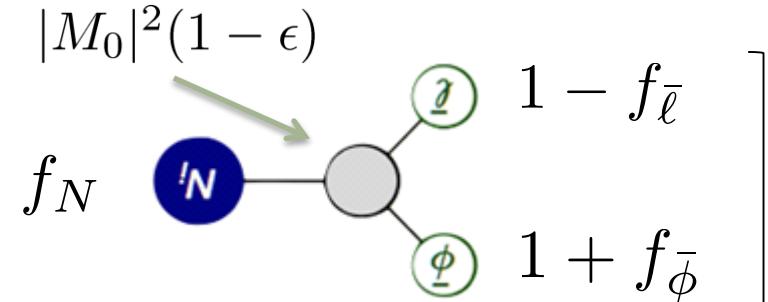
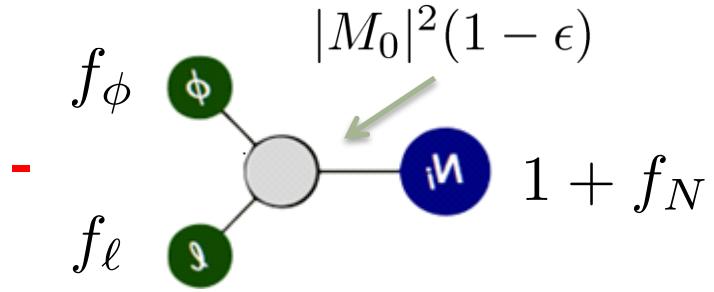
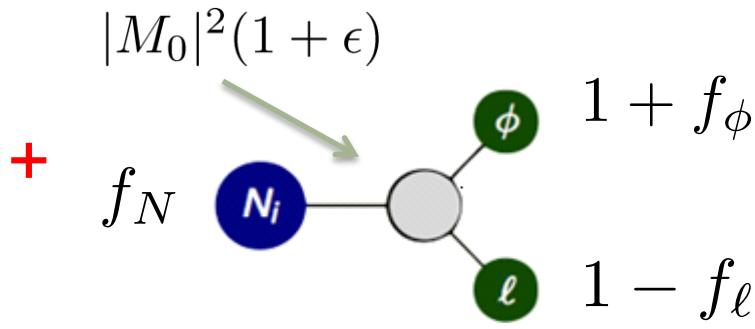
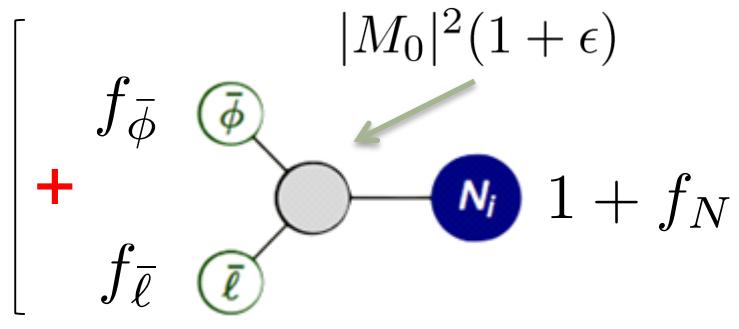




Time derivative of lepton number = Phase space integral  $\times$  Momentum-energy conserving delta-function  $\times$

$$\left[ + |M_0|^2(1 + \epsilon) f_N \begin{array}{c} \phi \\ \ell \end{array} \begin{array}{l} 1 + f_\phi \\ 1 - f_\ell \end{array} - |M_0|^2(1 - \epsilon) f_N \begin{array}{c} \bar{l} \\ \bar{\phi} \end{array} \begin{array}{l} 1 - f_{\bar{l}} \\ 1 + f_{\bar{\phi}} \end{array} \right]$$

Time derivative of lepton number = Phase space integral  $\times$  Momentum-energy conserving delta-function  $\times$



$$\frac{Y_N}{dz} = i \cdot {}^o_D(Y_N - Y_N^{eq})$$

$$\frac{Y_L}{dz} = 2 \cdot {}^o_D(Y_N + Y_N^{eq}) i \cdot {}^o_L Y_L$$

$$i_N = \frac{i_N}{H(T = M_1)}$$

$$z = \frac{M_1}{T}$$

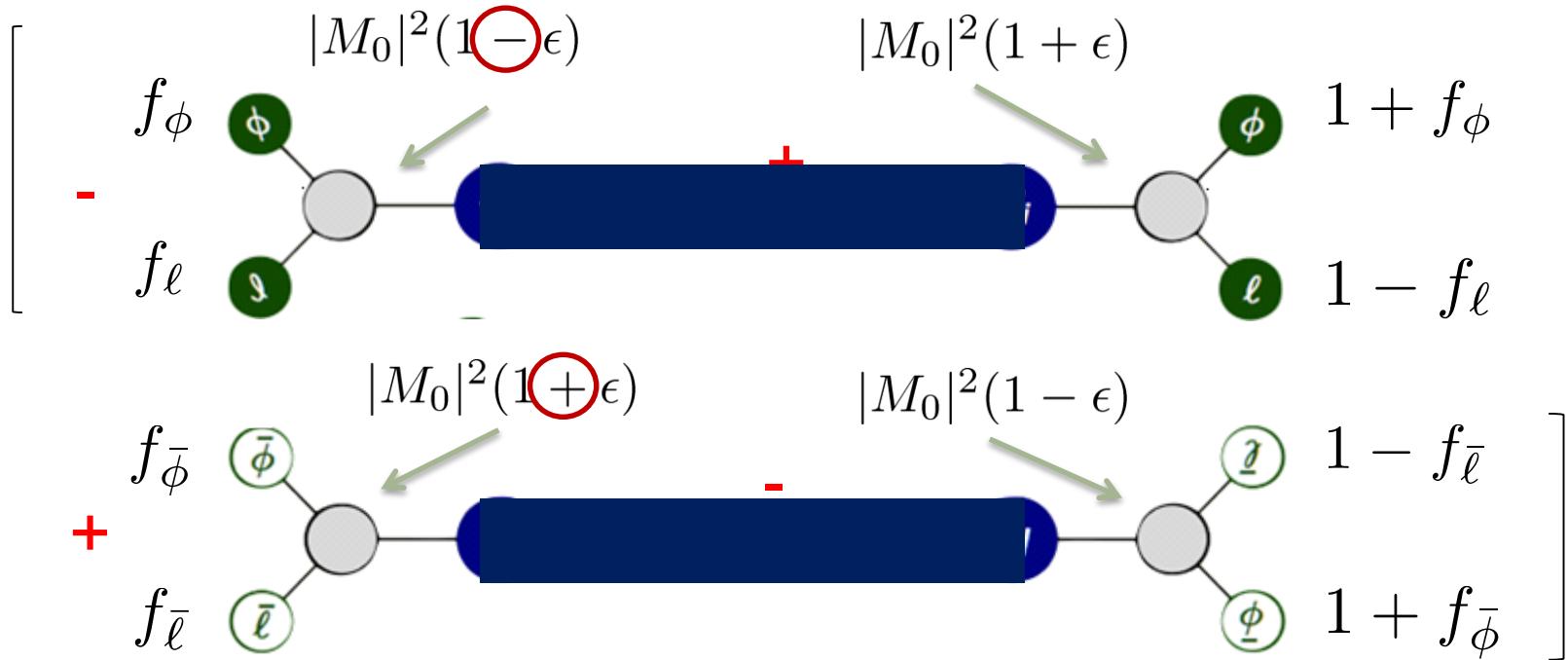


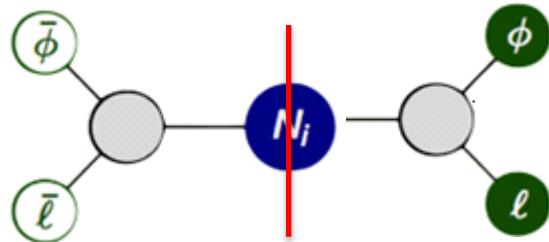
- Violation of baryon number
- C- and CP-violation
- Deviation from equilibrium

Andrei Sakharov

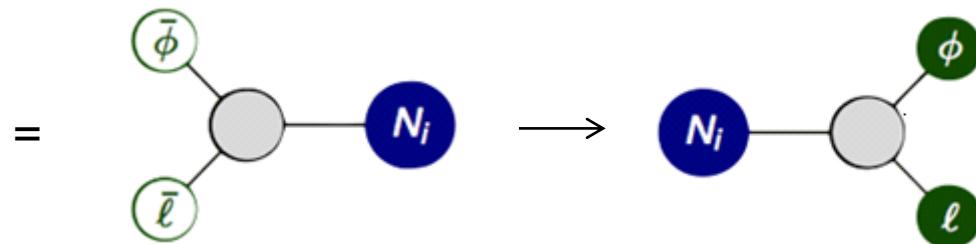
$$\begin{aligned}
 & \text{Time derivative of lepton number} = \text{Phase space integral} \times \text{Momentum-energy conserving delta-function} \times \\
 & \left[ \begin{array}{c}
 |M_0|^2(1-\epsilon) \\
 f_\phi \quad \phi \quad \text{---} \quad N_i \quad 1 + f_N \quad + \\
 -f_\ell \quad \ell \quad \text{---} \quad \text{---} \\
 \\ 
 |M_0|^2(1+\epsilon) \\
 f_{\bar{\phi}} \quad \bar{\phi} \quad \text{---} \quad N_i \quad 1 + f_N \quad - \\
 +f_{\bar{\ell}} \quad \bar{\ell} \quad \text{---} \quad \text{---} \\
 \end{array} \right. \\
 & \qquad \qquad \qquad \left. \begin{array}{c}
 |M_0|^2(1+\epsilon) \\
 f_N \quad N_i \quad \phi \quad 1 + f_\phi \\
 \text{---} \quad \text{---} \quad \ell \quad 1 - f_\ell \\
 \\ 
 |M_0|^2(1-\epsilon) \\
 f_N \quad N_i \quad \bar{\phi} \quad 1 - f_{\bar{\ell}} \\
 \text{---} \quad \text{---} \quad \bar{\ell} \quad 1 + f_{\bar{\phi}}
 \end{array} \right]
 \end{aligned}$$

Time derivative of lepton number = Phase space integral  $\times$  Momentum-energy conserving delta-function  $\times$





if the intermediate state  
is on the mass shell, then



$$P_{ii}^{RIS}(s) \sim \frac{1}{(s_i - M_i^2)^2 + (M_{i\bar{i}i})^2} \propto \frac{1}{M_{i\bar{i}i}} \propto \frac{1}{M_i} \propto \frac{1}{M_i^2};$$

$$\frac{dY_N}{dz} = i \cdot \circ_D (Y_N - Y_N^{eq})$$

$$\frac{dY_L}{dz} = 2 \cdot \circ_D (Y_N - Y_N^{eq}) i \cdot \circ_L Y_L$$

$$\cdot = \frac{i_N}{H(T = M_1)}$$

$$z \cdot \frac{M_1}{T}$$

$$\gg \frac{z}{Z_f}$$

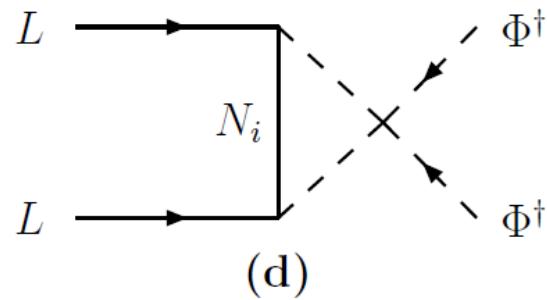
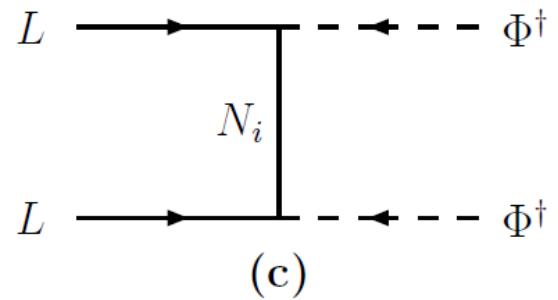
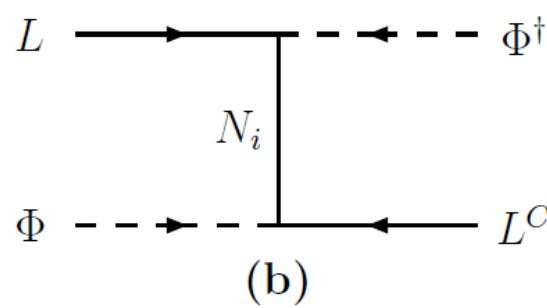
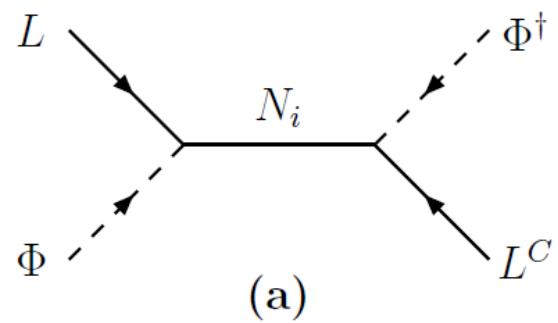
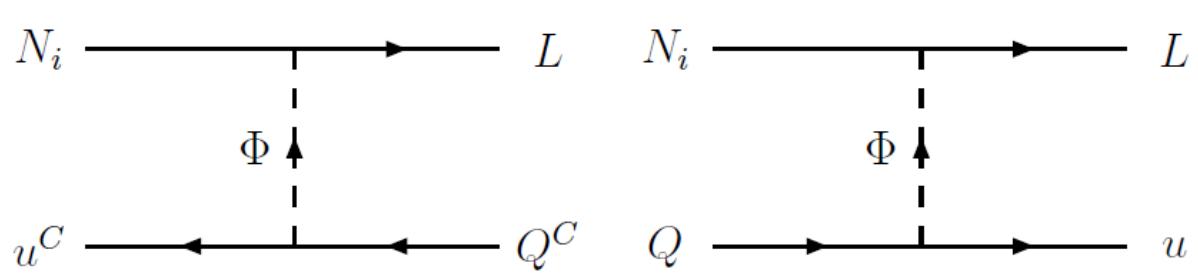
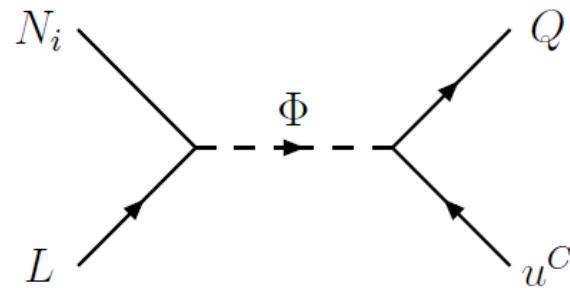
$$= \frac{i_1}{H(M_1)} \cdot \frac{m_1}{m_\alpha}$$

$$m_\alpha \gg 10^{-3} \text{ eV}$$

$$m_1 < 5 \times 10^{-3} \text{ eV}$$

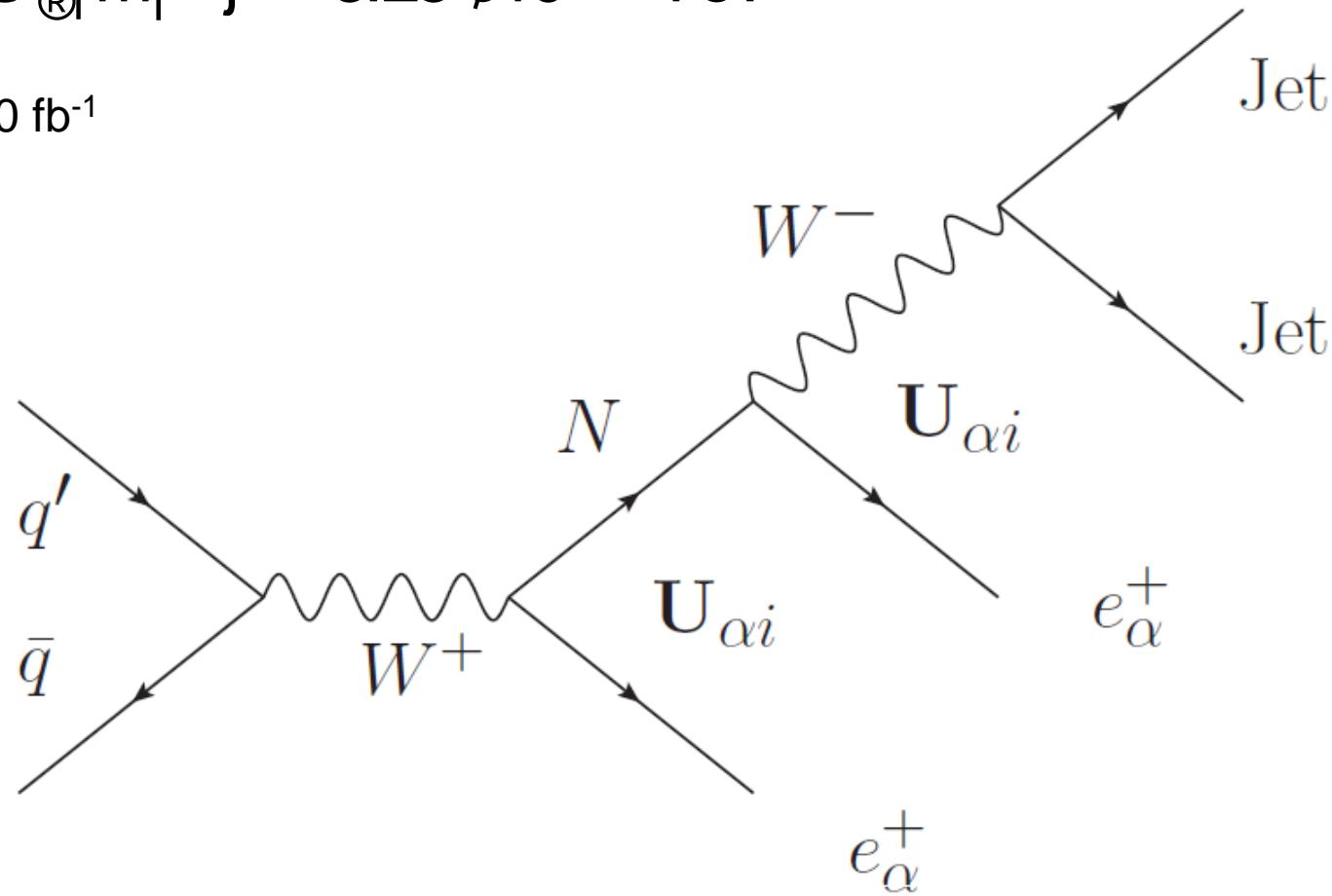
$$^2_1 \cdot \frac{3}{8\pi} \frac{M_1 m_3}{v^2}$$

$$M_1 \gg 10^8 \text{ GeV}$$



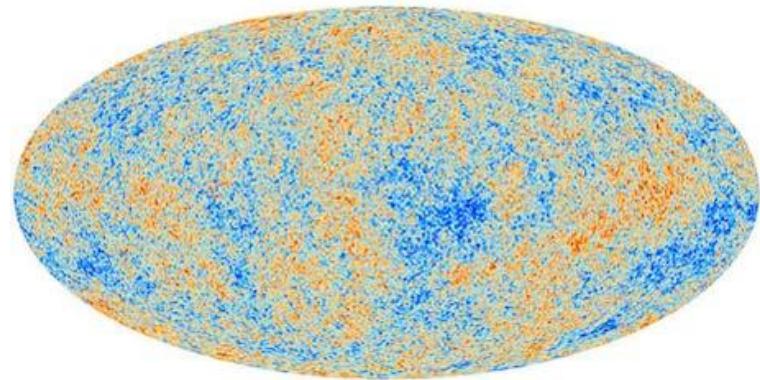
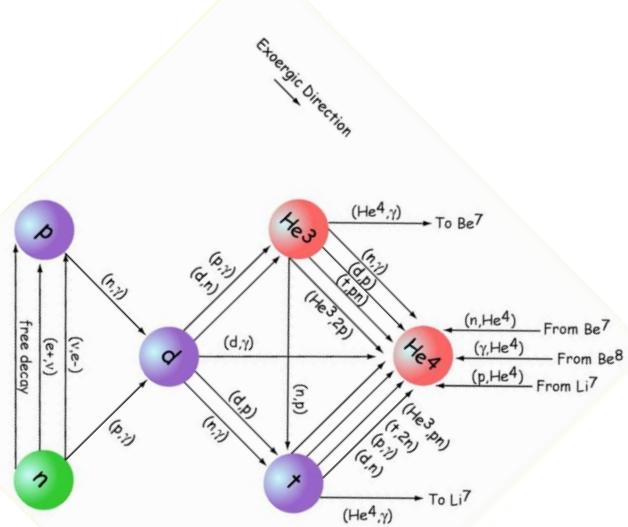
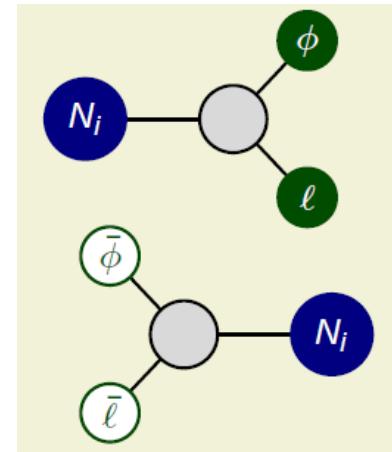
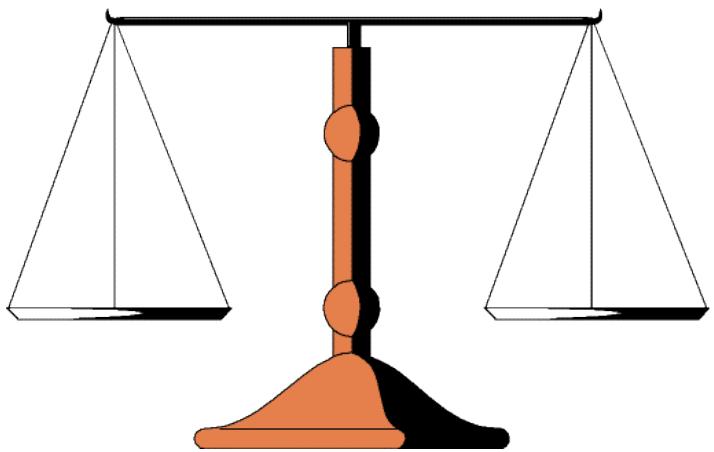
$j \Gamma_i U_{\alpha i}^2 m_i^{-1} j' \sim 3:25 \times 10^{-3} \text{ TeV}^{-1}$

for  $400 \text{ fb}^{-1}$



# Intermediate summary II

- Heavy Majoranas explain the BAU
- predict  $0\beta\beta$  decay
- and can be searched for in colliders



$$\begin{aligned}
\langle B \rangle &= \text{Tr} e^{-\beta \hat{H}} \hat{B} \\
&= \text{Tr} (CPT)(CPT)^{-1} e^{-\beta \hat{H}} \hat{B} \\
&= \text{Tr} e^{-\beta \hat{H}} (CPT)^{-1} \hat{B} (CPT) \\
&= -\text{Tr} e^{-\beta \hat{H}} \hat{B} \\
&= -\langle B \rangle
\end{aligned}$$

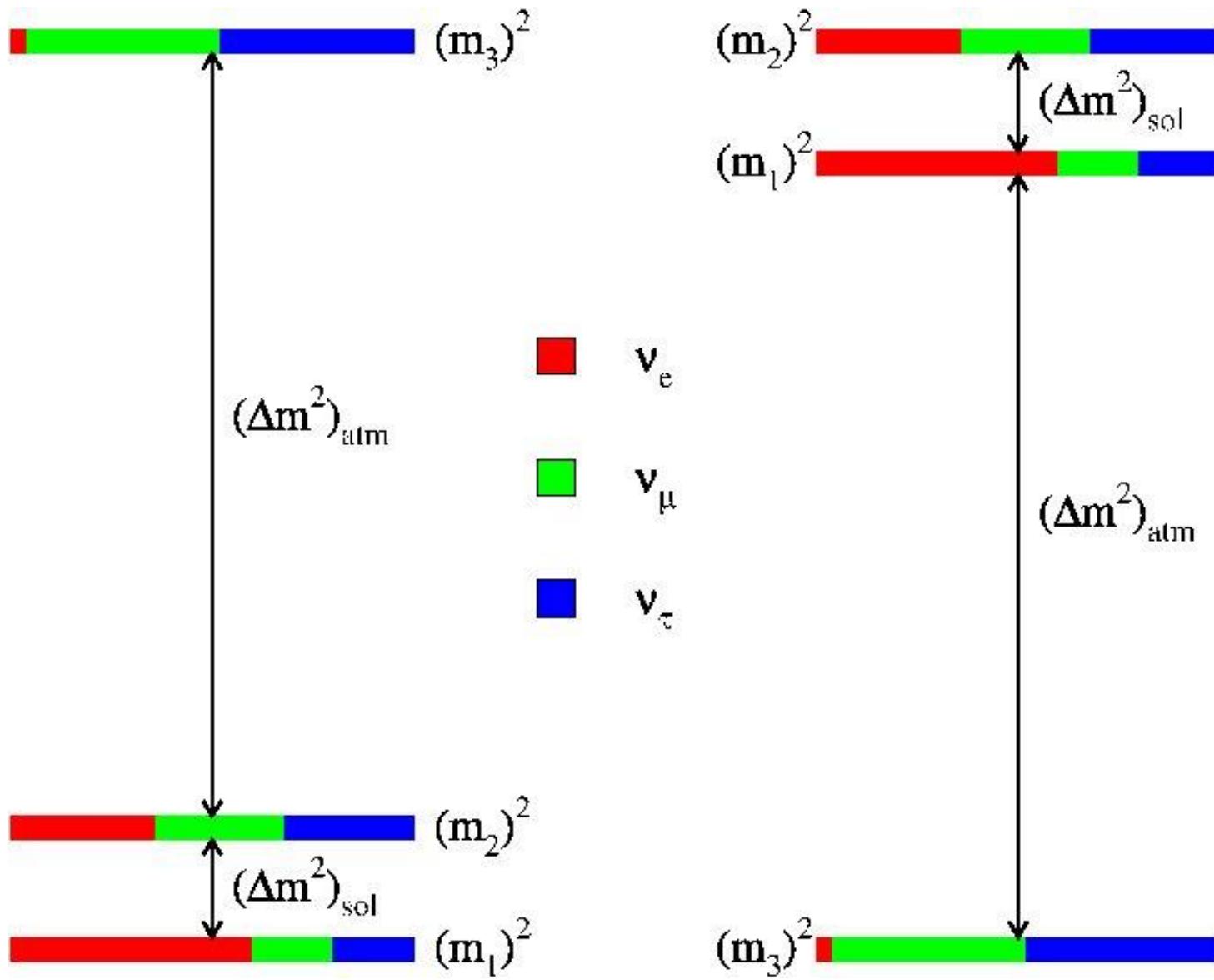
$$\mathbf{Y}_\nu = \frac{1}{\langle H_u^0 \rangle} D_{\sqrt{M}} R D_{\sqrt{m}} U^+$$

$$\epsilon_1 \simeq -\frac{3}{8\pi} \frac{1}{[\mathbf{Y}_\nu \mathbf{Y}_\nu^\dagger]_{11}} \sum_j \text{Im} \left\{ [\mathbf{Y}_\nu \mathbf{Y}_\nu^\dagger]_{1j}^2 \right\} \left( \frac{M_1}{M_j} \right)$$

$$= -\frac{3}{8\pi} \frac{M_1}{\langle H_u^0 \rangle^2} \frac{1}{[\mathbf{Y}_\nu \mathbf{Y}_\nu^\dagger]_{11}} \text{Im} \left\{ [\mathbf{Y}_\nu \mathcal{M}_\nu^\dagger \mathbf{Y}_\nu^T]_{11} \right\}$$

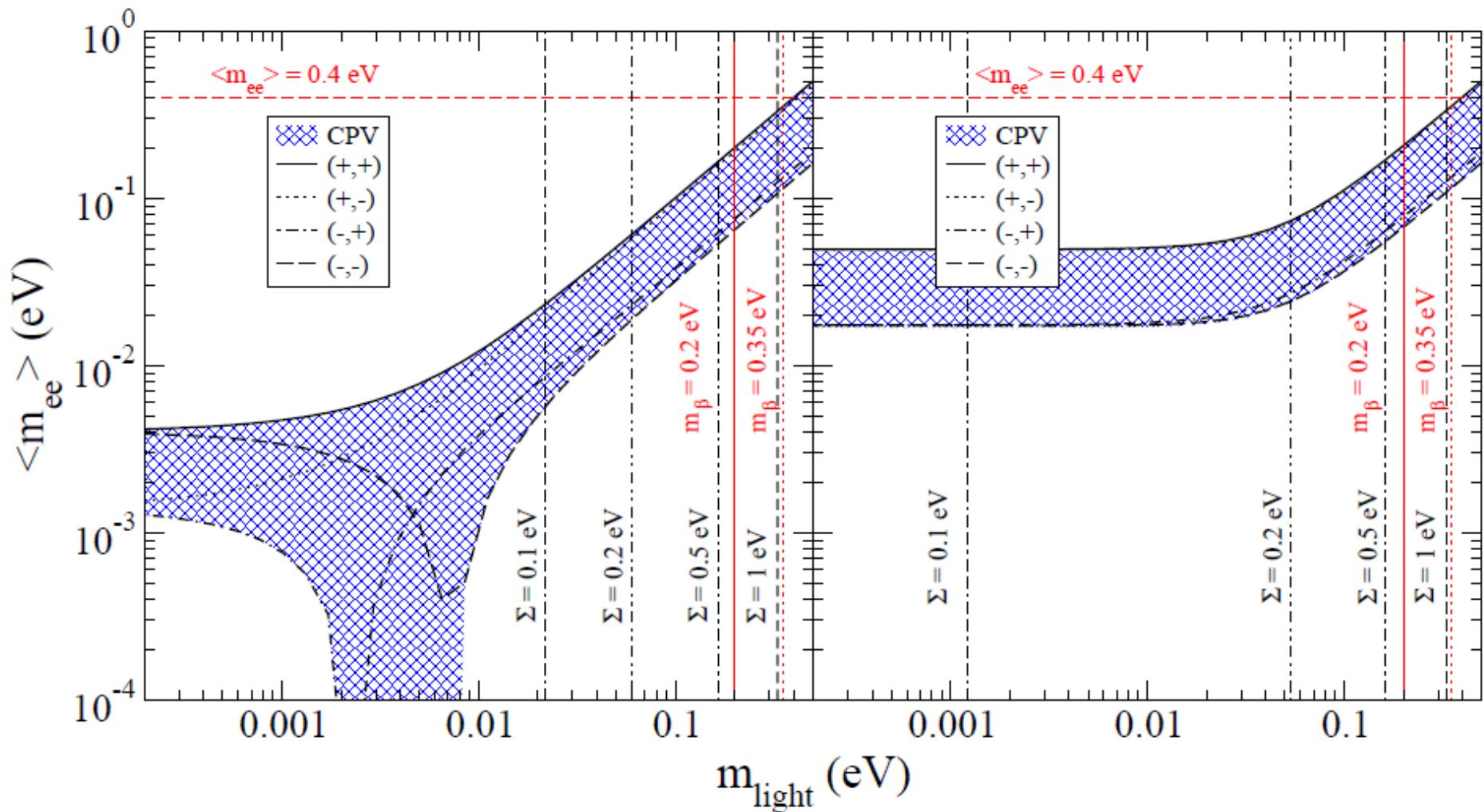
$$\epsilon_1 \simeq -\frac{3}{8\pi} \frac{M_1}{\langle H_u^0 \rangle^2} \frac{\sum_j m_j^2 \text{Im}(R_{1j}^2)}{\sum_j m_j |R_{1j}|^2}$$

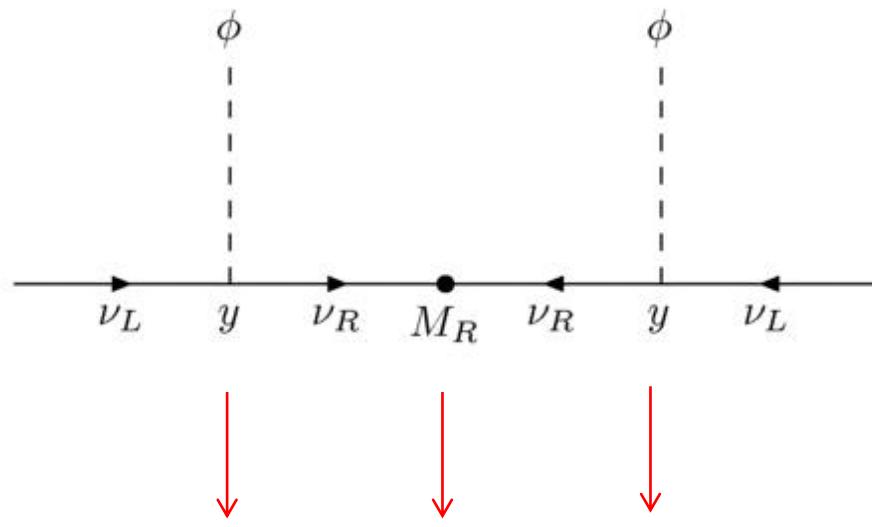
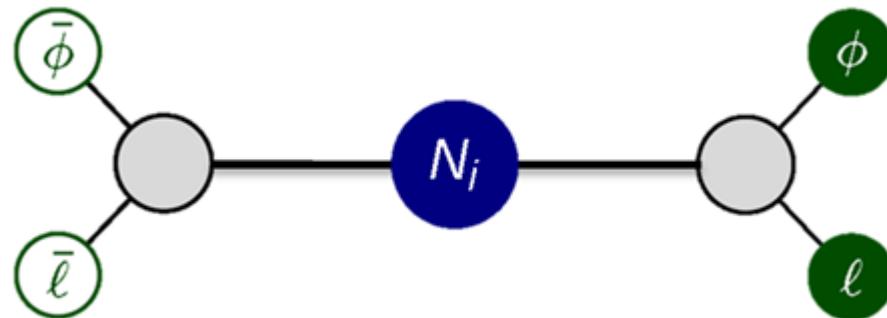
$$\tilde{m}_1 = \sum_j m_j |R_{1j}|^2$$



Normal

Inverted





$$\mathcal{M}_\nu = \mathcal{M}_D^T \mathcal{M}_M^{-1} \mathcal{M}_D$$



Valery Rubakov



Vadim Kuzmin



Mikhail Shaposhnikov

