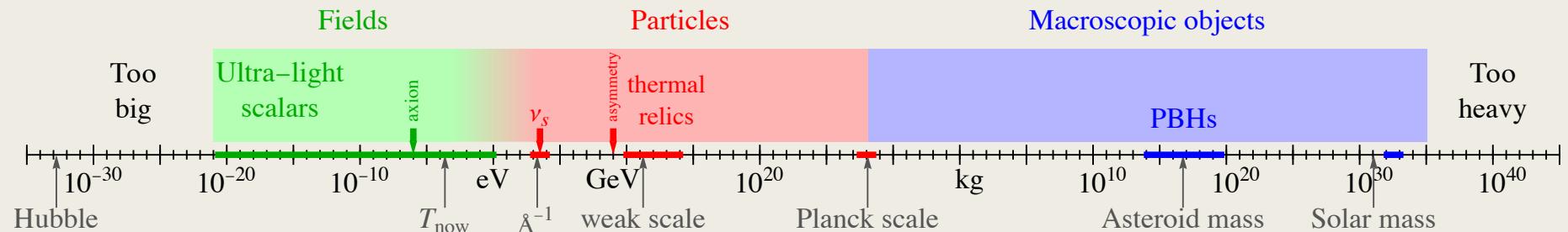


DARK MATTER

Yasaman Farzan
IPM, Tehran

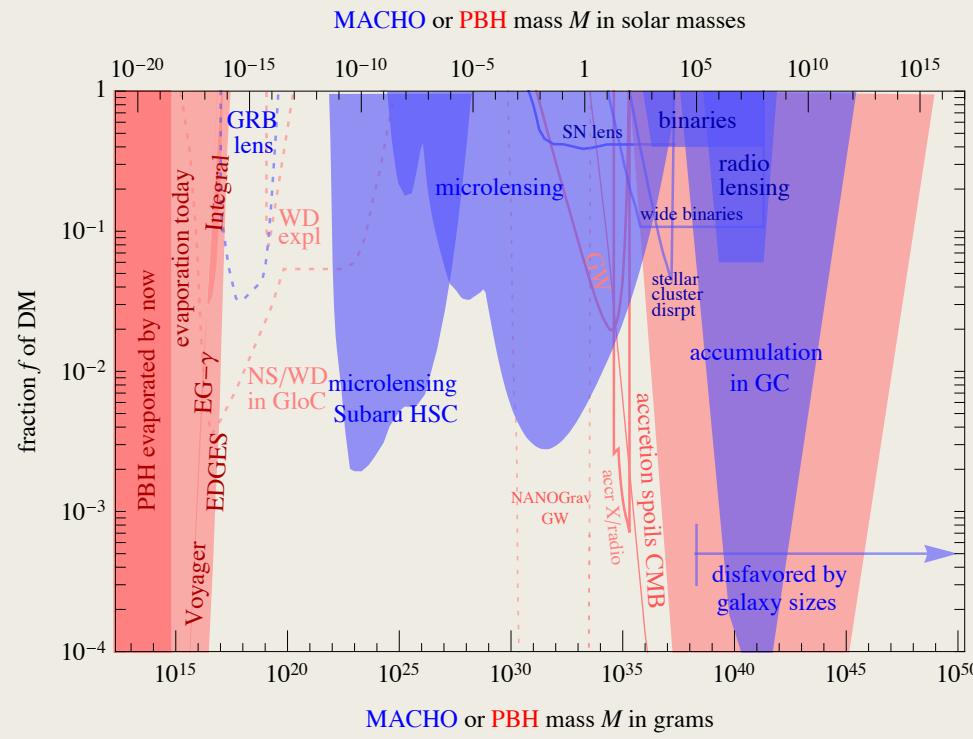
DM mass range



$$10^{-21} \text{ eV} < M < 10^{37} \text{ kg.}$$

Massive Astrophysical Compact Halo Objects

■ MACHO



Particle Dark Matter

1. DM must be *cold* or at least *not too hot*.
2. The *electric charge* q of a DM particle must be *null or very small*.
3. Bounds from direct detection experiments,
4. The *cross section among two DM particles*
5. The DM particle must be *stable*,

Fermionic dark matter

Fermionic DM is subject to the Pauli exclusion principle,

The de Broglie wave-length is $\lambda = 2\pi/Mv$,

$$\rho \lesssim M/\lambda^3,$$

$M > 0.1 \text{ keV}$ (fermionic DM).

Can SM neutrinos play the role of DM?

- No
- They would be hot which is in conflict with structure formation.

Warm dark matter

$$M \gtrsim 1.9 \text{ keV} \left\langle \frac{p}{T} \right\rangle_{\text{prod}} \left(\frac{106.75}{g_{\text{SM}}(T_{\text{prod}})} \right)^{1/3}.$$

Self-Interacting Dark Matter

Cusped cored problem

$$\frac{\sigma}{M} \sim (0.1 - 1) \frac{\text{cm}^2}{\text{g}},$$

Dark Matter as waves of light and ultra-light fields

- Axion
- Fuzzy dark matter
-

Fuzzy dark matter

$$\lambda_{dB} \sim \text{Galaxy core}$$

Suarez, Robles and Matos, *Astrophys Space Sci Proc* 38 (2014) 107;
Rindler-Daller and Shapiro, *Mod Phys Lett A* 29; Chavanis, *PRD* 84 (2011) 43531;
Marsh, *Phys Rep* 643 (2016);
Hui, Ostriker, Tremaine and Witten, *PRD* 95 (2017) 043541

Lower bound on scalar

- Lyman alpha
- Rotation curves
- Superradiance M87*
- Precision cosmology
- ...

$$m_{DM} \gtrsim 10^{-21} \text{ eV}$$

Classical limit

$$\lambda_{dB} \sim n_{DM}^{-1/3} = \left(\frac{m_{DM}}{\rho_{DM}} \right)^{1/3}$$

Real scalar:

$$\phi = A \cos(m_{DM} t)$$



$$T^{00} = \rho_{DM}$$



$$A^2 = \frac{2\rho_{DM}}{m_{DM}^2}$$

Complex scalar:



$$\phi = A \cos(m_{DM} t) + iB \sin(m_{DM} t + c)$$



$$A^2 + B^2 = \frac{\rho_{DM}}{m_{DM}^2}$$

Two main classes of DM models

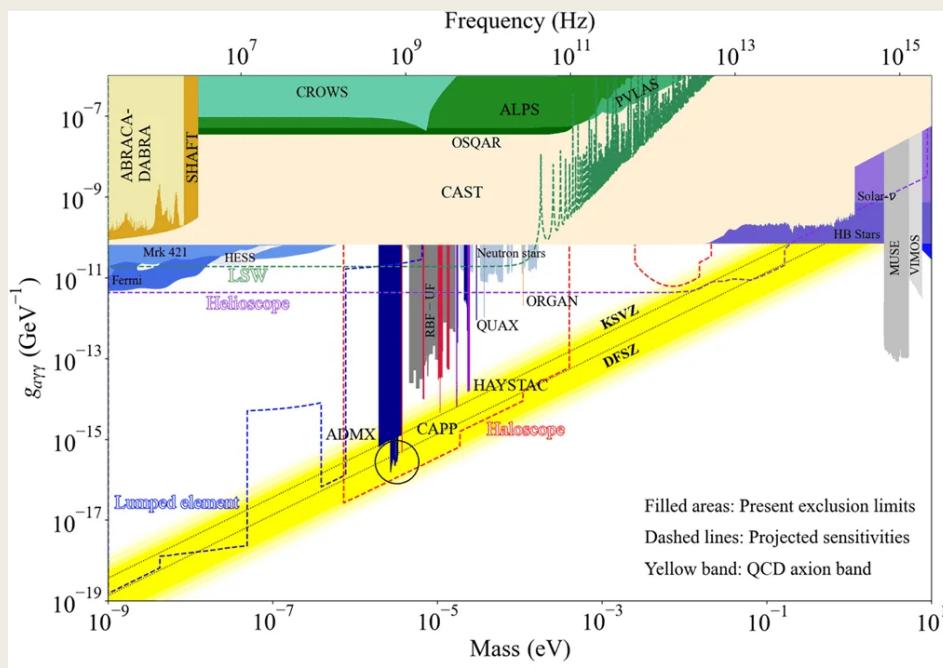
- WIMP=Weekly Interacting Massive Particle

Like neutralino, KK modes in LED,...

- Axion (or ALP=Axion-Like Particle)

Axion

- <https://www.azoquantum.com/News.aspx?newsID=9446>



$$g_{a\gamma\gamma} a [\epsilon_{\mu\nu\alpha\beta} F^{\mu\nu} F^{\alpha\beta}]$$

Production

- Freeze-in
- Freeze-out
- Decay of heavier particle

- Freeze-out scenario

Boltzmann equation

$$\frac{dn}{dt} = -3Hn + \langle \sigma v \rangle (n^2 - n_{eq}^2)$$

$$n_{eq} = g_X \left(\frac{m_X T}{2\pi} \right)^{3/2} e^{-m_X/T}$$

Average time before annihilation

$$\tau = \frac{1}{n_x} \frac{1}{\langle \sigma_{\text{ann}} v \rangle},$$

Annihilation ends when

$$\frac{1}{n_x} \frac{1}{\langle \sigma_{\text{ann}} v \rangle} = H^{-1}(T_f),$$

where T_f is the freeze-out temperature in question.

$X\bar{X}$ -annihilation often occurs in s -wave.

$$\sigma_{\text{ann}} = \frac{\sigma_0}{v}$$

$$\frac{1}{g_x \sigma_0} \left(\frac{2\pi}{M_x T_f} \right)^{3/2} e^{\frac{M_x}{T_f}} = H^{-1}(T_f) \equiv \frac{M_{Pl}^*}{T_f^2},$$

Freeze-out temperature

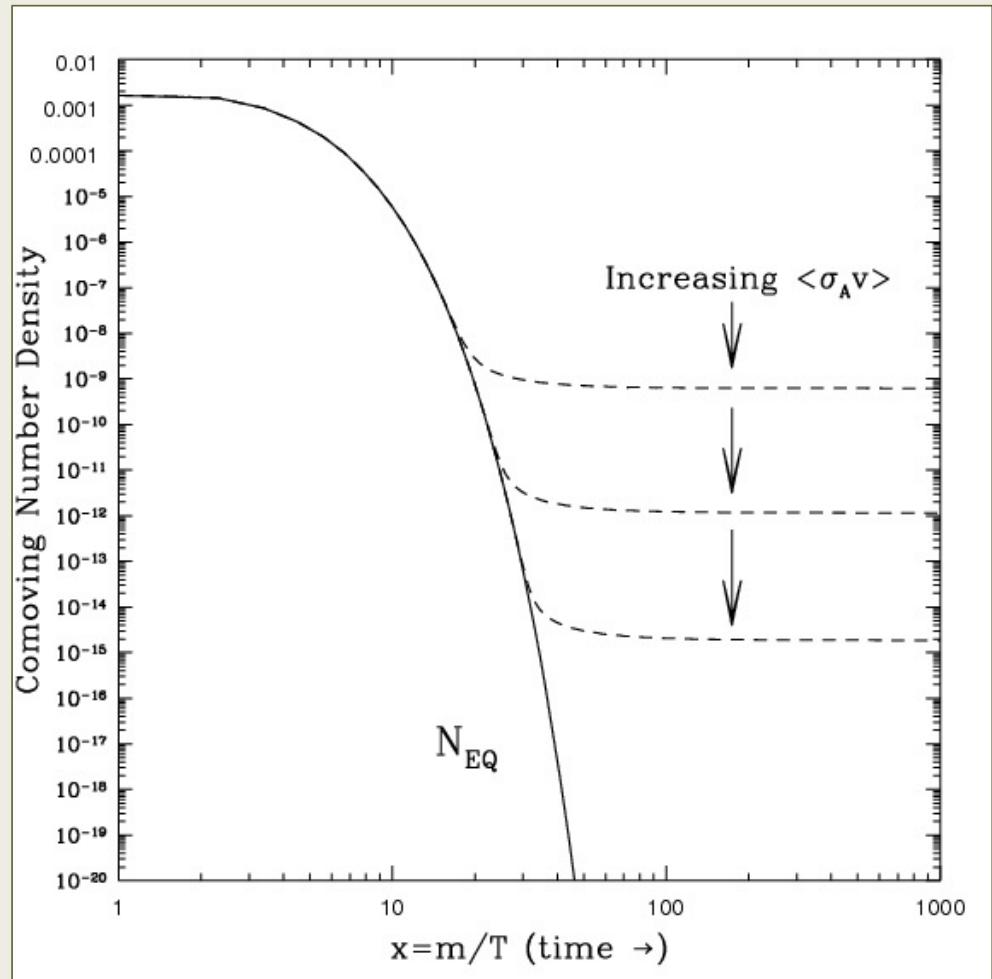
$$T_f = \frac{M_X}{\log\left(\frac{g_X M_X M_{Pl}^* \sigma_0}{(2\pi)^{3/2}}\right)}.$$

$$\frac{1}{n_X} \frac{1}{\langle \sigma_{\text{ann}} v \rangle} = H^{-1}(T_f), \quad \Rightarrow \quad n_X(t_f) = \frac{T_f^2}{M_{Pl}^* \sigma_0}.$$

$$n_x(t_0) = \left(\frac{a(t_f)}{a(t_0)} \right)^3 n_x(t_f).$$

$$n_x(t_0) = \left(\frac{s_0}{s(t_f)} \right) n_x(t_f),$$

$$M_{Pl}^* = \frac{M_{Pl}}{1.66g_*^{1/2}}, \quad s(t_f) = g_*(t_f) \cdot \frac{2\pi^2}{45} T_f^3.$$



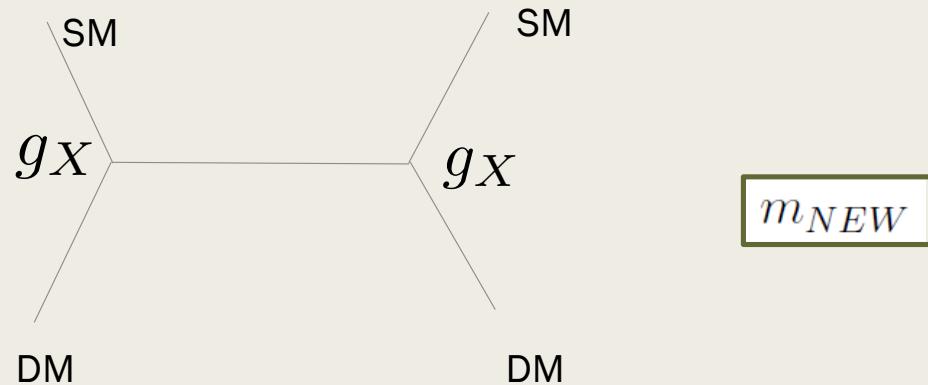
$$\Omega_X = 2\frac{M_X n_X(t_0)}{\rho_c} = 7.6 \frac{s_0 \log\left(\frac{g_X M_{Pl}^* M_X \sigma_0}{(2\pi)^{3/2}}\right)}{\rho_c \sigma_0 M_{Pl} \sqrt{g_*(t_f)}}.$$

$$\log \frac{g_X M_{Pl}^* M_X \sigma_0}{(2\pi)^{3/2}} \sim \log \frac{g_X M_{Pl}^*}{(2\pi)^{3/2} M_X} \sim 30.$$

$$\boxed{\sigma_0 \sim 1~pb \sim 10^{-36} cm^2 \qquad \qquad 1~pb \sim 3 \times 10^{-26} cm^3/sec}$$

WIMP

- Weekly Interacting Massive Particles

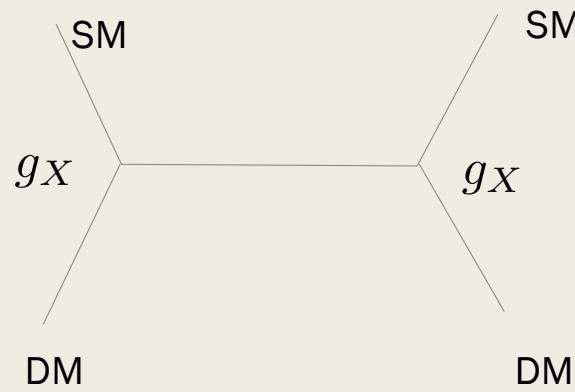


m_{NEW}

$$\sigma_0 \sim \frac{g_X^4}{4\pi m_{NEW}^2}$$

WIMP

- Weekly Interacting Massive Particles



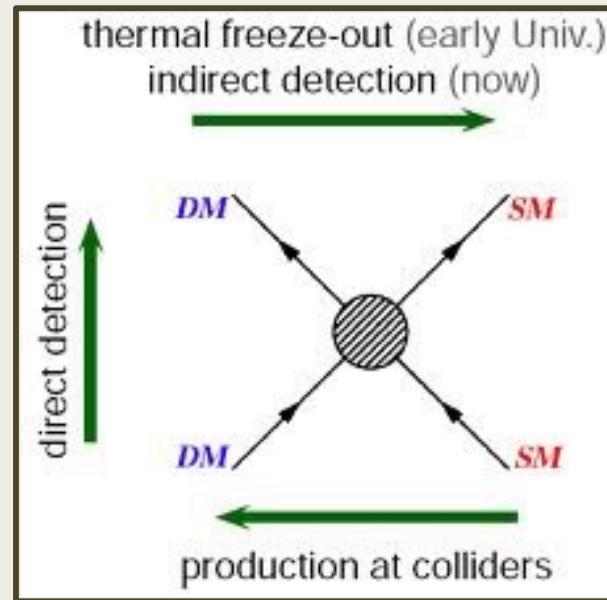
$$\sigma_0 \sim \frac{g_X^4}{4\pi m_{NEW}^2}$$

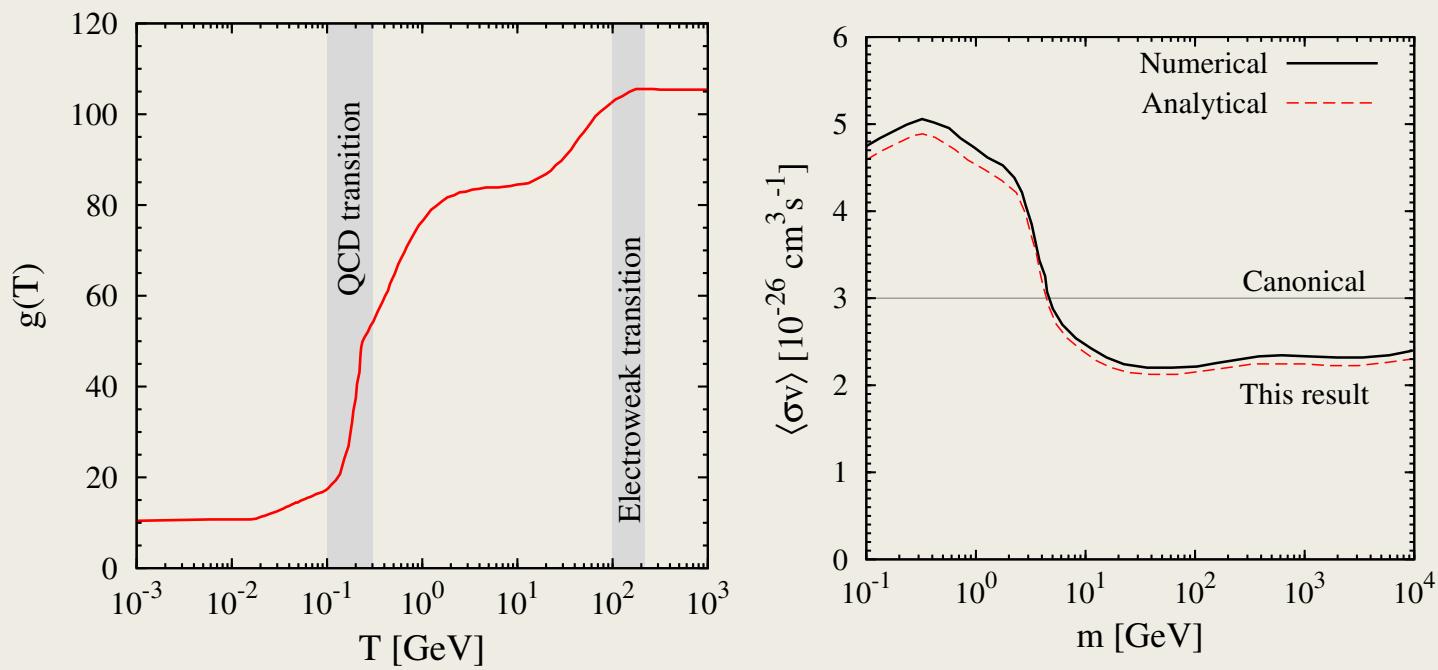
$$g_X \sim e \quad \text{and} \quad \sigma_0 \sim 1 \text{ pb}$$



$$m_{NEW} \sim 100 \text{ GeV} - 1000 \text{ GeV}$$

The reason to be excited





Steigman, Dasgupta, Beacom,
PRD 86 (2012) 023506

Freeze-In

$$A+B\rightarrow \mathrm{DM}+\mathrm{DM}\quad A,B\in \mathrm{SM}$$

$$\rho_{DM}=n_{DM}m_{DM}=2m_{DM}\int_0^{t_{NEW}} n_A(T)n_N(T)\sigma(T)dt$$

UV vs IR Freeze-In

IR freeze-in.

small renormalizable interactions g

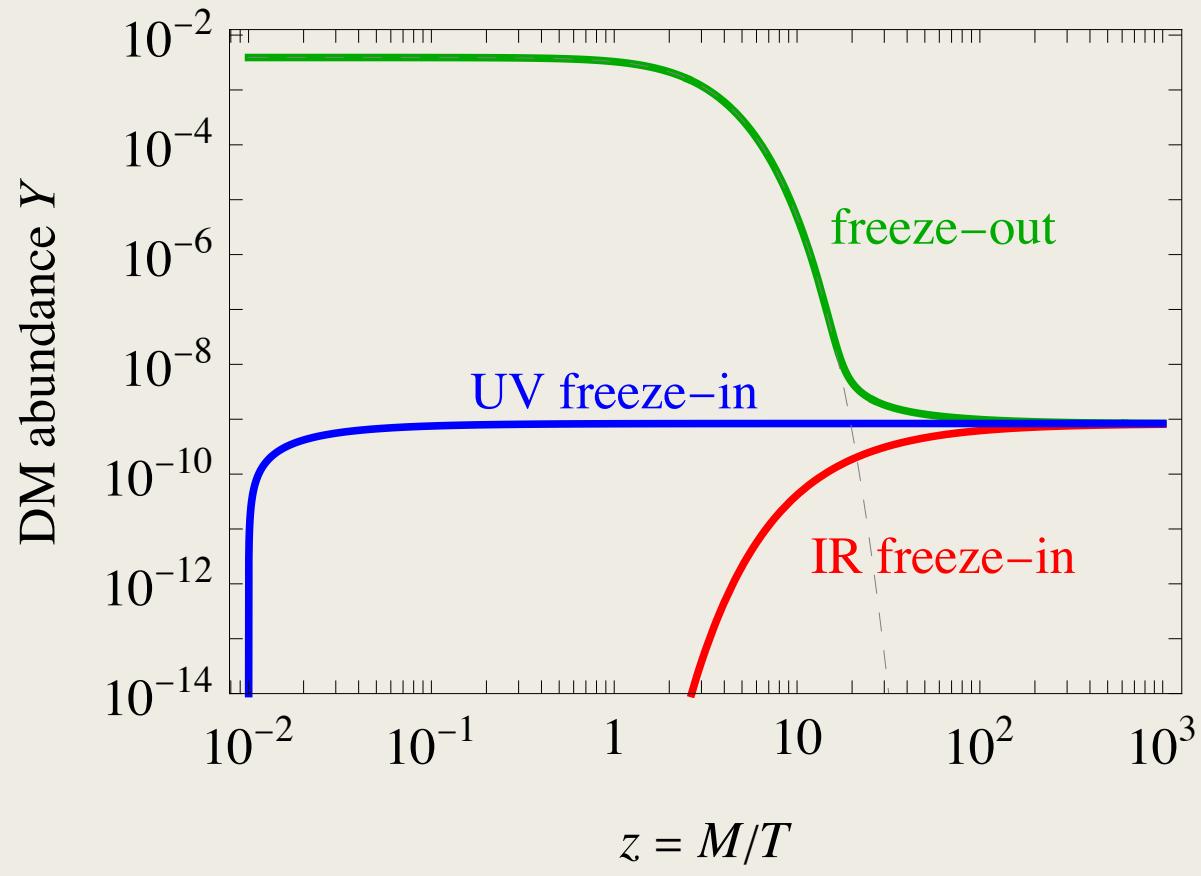
$$\dot{n}_{DM} \propto g^4 T^4$$

UV freeze-in.

small non-renormalizable interactions

$$\frac{1}{\mathcal{M}^n}$$

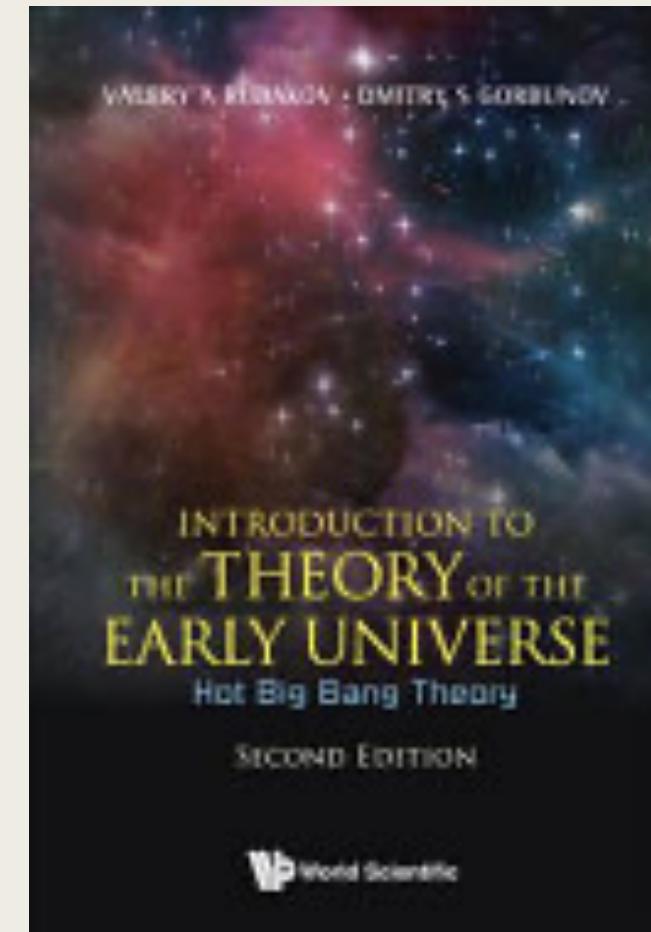
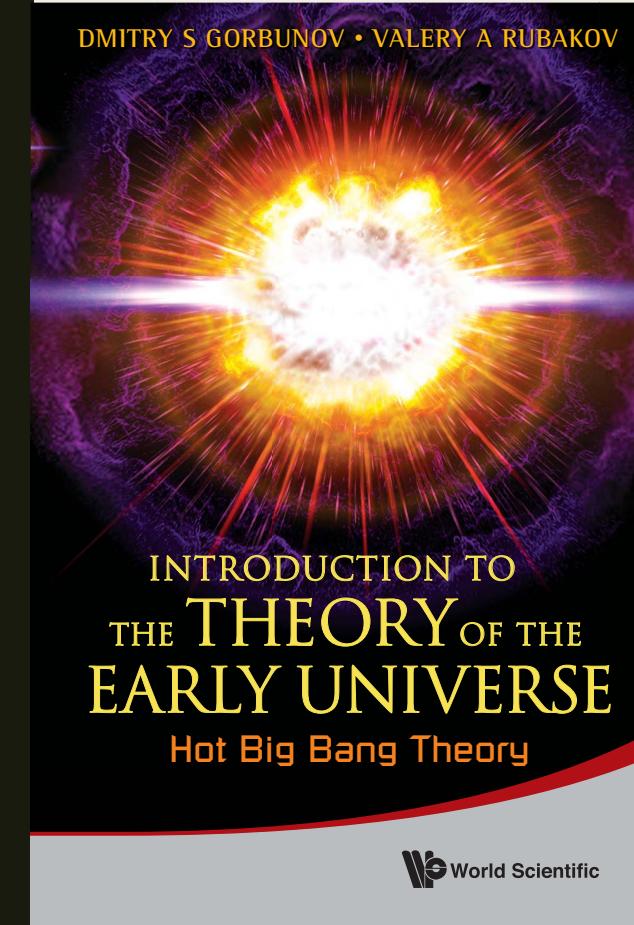
$$\dot{n}_{DM} \propto \frac{T^{4+2n}}{\mathcal{M}^{2n}}$$



$$Y = n/s$$

$$z = M/T$$

Standard cosmology in a nutshell



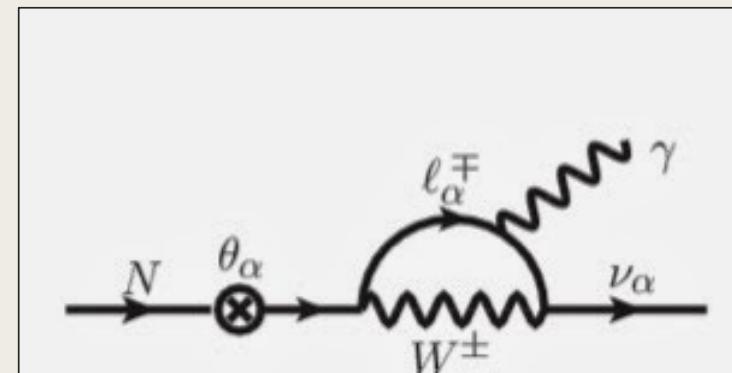
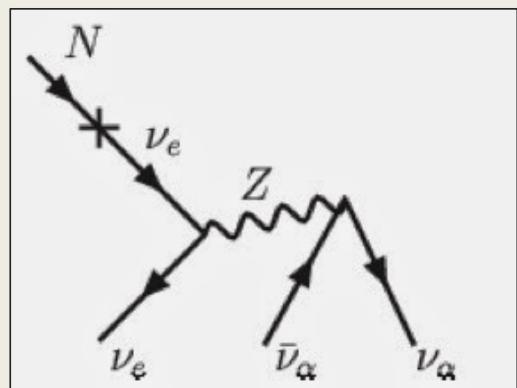
Sterile neutrinos

$$|\nu_\alpha\rangle = \cos\theta_\alpha |\nu_1\rangle + \sin\theta_\alpha |\nu_2\rangle, \quad |\nu_s\rangle = -\sin\theta_\alpha |\nu_1\rangle + \cos\theta_\alpha |\nu_2\rangle,$$

$$P(\nu_\alpha \rightarrow \nu_s) = \sin^2 2\theta_\alpha \cdot \sin^2 \left(\frac{t}{2t_\alpha^{vac}} \right),$$

$$t_\alpha^{vac} = \frac{2E_\nu}{\Delta m^2}, \quad \Delta m^2 = m_s^2 - m_1^2 \simeq m_s^2.$$

Mixing makes unstable



Matter effects

$$H = U \cdot \text{diag} \left(\frac{m_1^2}{2E_\nu}, \frac{m_2^2}{2E_\nu} \right) \cdot U^\dagger + V_{int},$$

where the mixing matrix U and matrix V_{int} describing matter effects are

$$U = \begin{pmatrix} \cos \theta_\alpha & \sin \theta_\alpha \\ -\sin \theta_\alpha & \cos \theta_\alpha \end{pmatrix}, \quad V_{int} = \begin{pmatrix} V_{\alpha\alpha} & 0 \\ 0 & 0 \end{pmatrix}.$$

- Shi-Fuller (requires lepton asymmetry)

$$V_{int} \propto G_F$$

- Dodelson- Widrow (in absence of lepton asymmetry)

$$V_{int} \propto G_F^2$$

the momentum dependence of the W -boson propagator.

$$V_{\tau\tau} = \frac{14\pi}{45\alpha} \sin^2 \theta_W \cos^2 \theta_W \cdot G_F^2 T^4 \cdot E_\nu \approx 25 \cdot G_F^2 T^4 \cdot E_\nu,$$

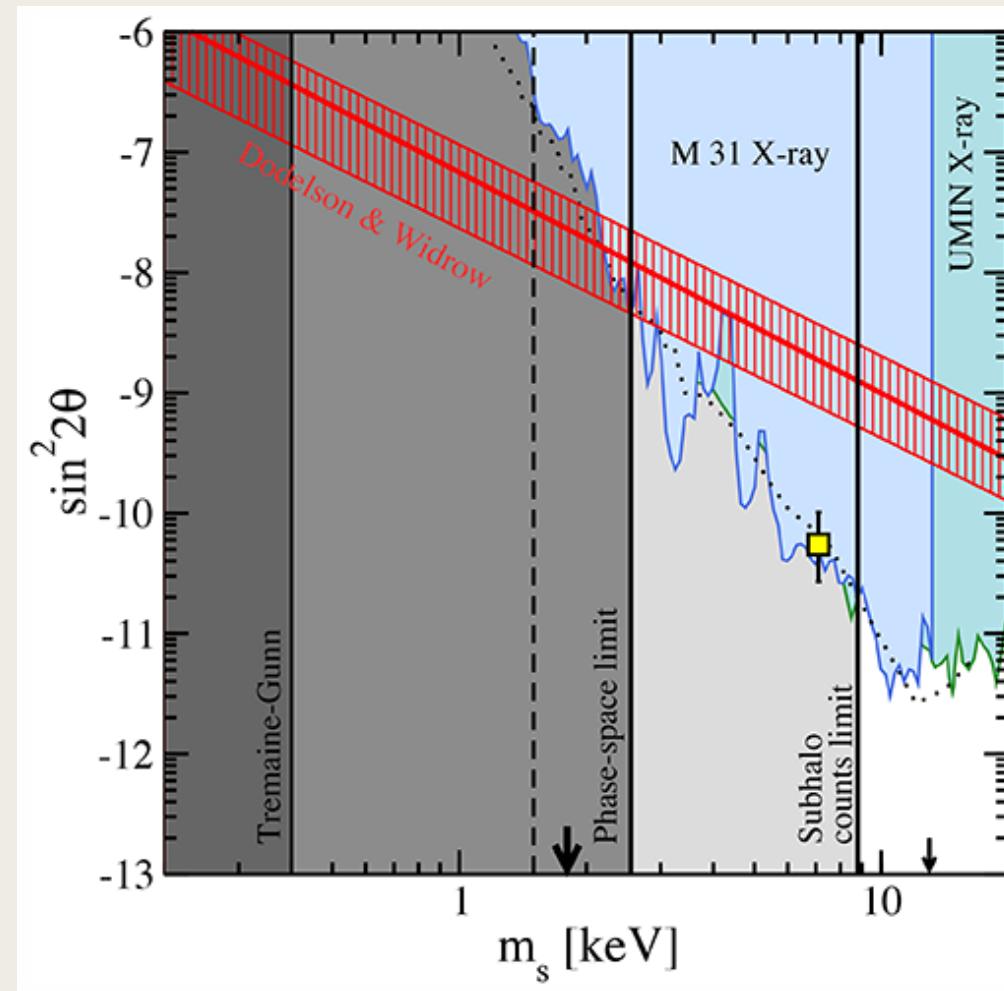
$$\begin{aligned}
P(\nu_\alpha \rightarrow \nu_s) &= \sin^2 2\theta_\alpha^{\text{mat}} \cdot \sin^2 \left(\frac{t}{2t_\alpha^{\text{mat}}} \right), \\
t_\alpha^{\text{mat}} &= \frac{t_\alpha^{\text{vac}}}{\sqrt{\sin^2 2\theta_\alpha + (\cos 2\theta_\alpha - V_{\alpha\alpha} \cdot t_\alpha^{\text{vac}})^2}}, \\
\sin 2\theta_\alpha^{\text{mat}} &= \frac{t_\alpha^{\text{mat}}}{t_\alpha^{\text{vac}}} \cdot \sin 2\theta_\alpha,
\end{aligned}$$

$$T_* \sim \left(\frac{m_s}{5 G_F}\right)^{1/3} \simeq 200\,\mathrm{MeV} \cdot \left(\frac{m_s}{1\,\mathrm{keV}}\right)^{1/3}.$$

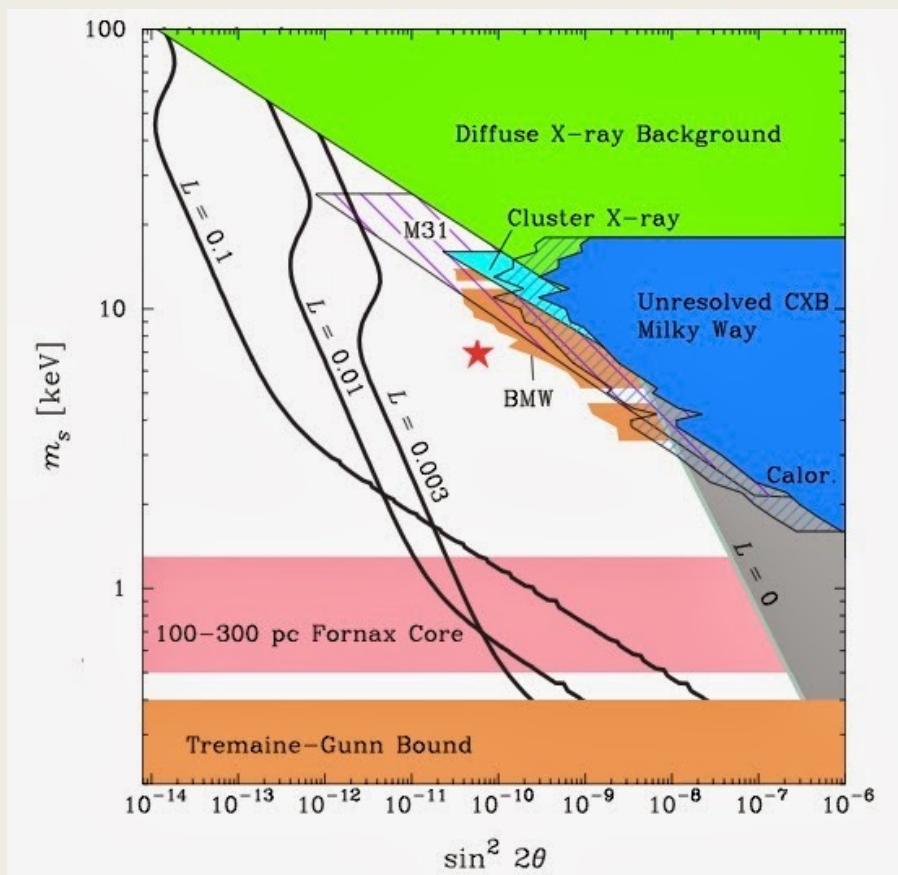
$$\begin{aligned} \frac{n_{\nu_s}(T_*)}{n_{\nu_\alpha}(T_*)} &\sim \frac{\sin^2 2\theta_\alpha}{H(T_*) \cdot \tau_\nu(T_*)} \sim T_*^3 M_{Pl}^* G_F^2 \cdot \sin^2 2\theta_\alpha \\ &\sim 10^{-2} \cdot \left(\frac{m_s}{1\,\mathrm{keV}}\right) \cdot \left(\frac{\sin 2\theta_\alpha}{10^{-4}}\right)^2. \end{aligned}$$

$$\Omega_{\nu_s} \simeq 0.2 \cdot \left(\frac{\sin 2\theta_\alpha}{10^{-4}}\right)^2 \cdot \left(\frac{m_\nu}{1\,\mathrm{keV}}\right)^2.$$

<http://resonaances.blogspot.com/2014/02/signal-of-neutrino-dark-matter.html>



<http://resonaances.blogspot.com/2014/02/signal-of-neutrino-dark-matter.html>



Exotic production mechanisms

Hawking radiation

Inflation decay to DM $m_\phi \gtrsim 2M,$

Quantum fluctuations during inflation: heavy fields

Quantum fluctuations during inflation: light scalar

Asymmetric DM

