

Solar Neutrinos & MSW Effect

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General Seminar Course

Nov. 2012 - IPM

Outline

- Introduction
- Neutrino Oscillation
- Solar Neutrinos
- Solar Neutrino Experiments
- Conclusions
- Summary

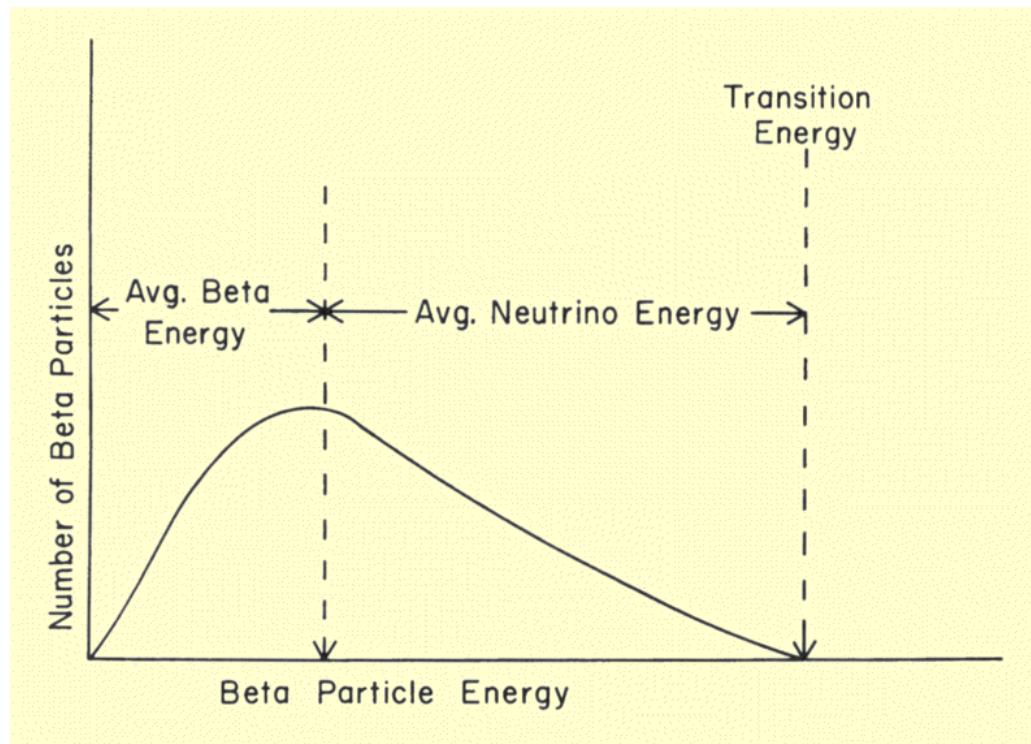
Introduction

Introduction

- History
- Standard Model
- Neutrino Interactions
- Neutrino Sources

History

- 1914, Chadwick, β -spectrum continuous
 α - and γ -rays unique in energy



http://en.wikipedia.org/wiki/Beta_decay

History

- N. Bohr: statistical energy conservation
- 1930, W. Pauli: neutron

I have done something very bad today by proposing a particle that cannot be detected; it is something no theorist shoulever do.

Wolfgang Pauli

History

- N. Bohr: statistical energy conservation
- 1930, W. Pauli: neutron
- 1933, E. Fermi: neutrino, massless
- 1942, Wang Ganchang: proposed detection
- 1956, Reines & Cowan: Detected



ON THE DETECTION OF THE FREE NEUTRINO*

F. Reines and C. L. Cowan, Jr.

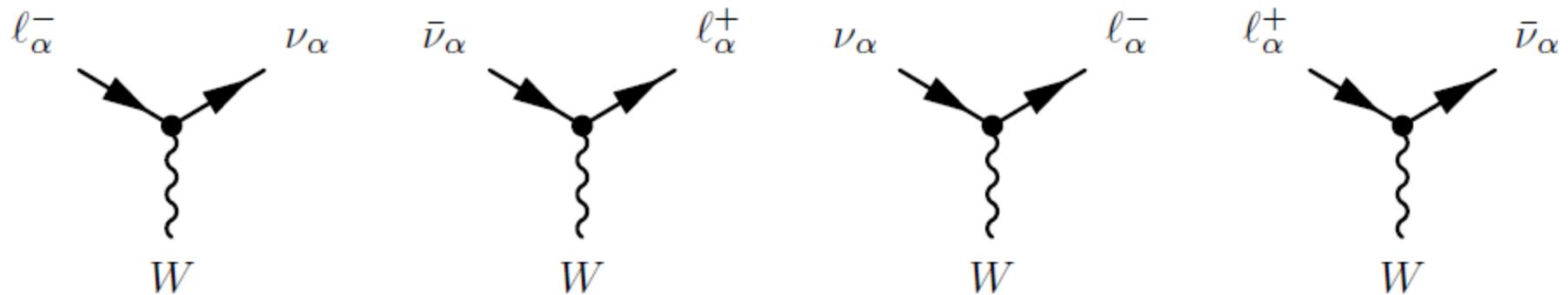
Los Alamos Scientific Laboratory

Standard Model

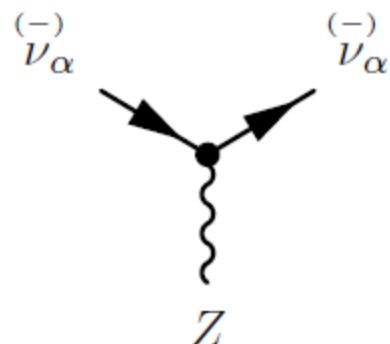
Three generations of matter (fermions)				
	I	II	III	
mass →	2.4 MeV/c ²	1.27 GeV/c ²	171.2 GeV/c ²	
charge →	2/3	2/3	2/3	0
spin →	1/2	1/2	1/2	0
name →	u up	c charm	t top	γ photon
Quarks	4.8 MeV/c ² -1/3 1/2 d down	104 MeV/c ² -1/3 1/2 s strange	4.2 GeV/c ² -1/3 1/2 b bottom	0 0 1 g gluon
	<2.2 eV/c ² 0 1/2 νe electron neutrino	<0.17 MeV/c ² 0 1/2 νμ muon neutrino	<15.5 MeV/c ² 0 1/2 ντ tau neutrino	91.2 GeV/c ² 0 1 Z ⁰ Z boson
	0.511 MeV/c ² -1 1/2 e electron	105.7 MeV/c ² -1 1/2 μ muon	1.777 GeV/c ² -1 1/2 τ tau	80.4 GeV/c ² ±1 1 W [±] W boson
	Leptons			Gauge bosons

Neutrino Interactions

- Charged Current

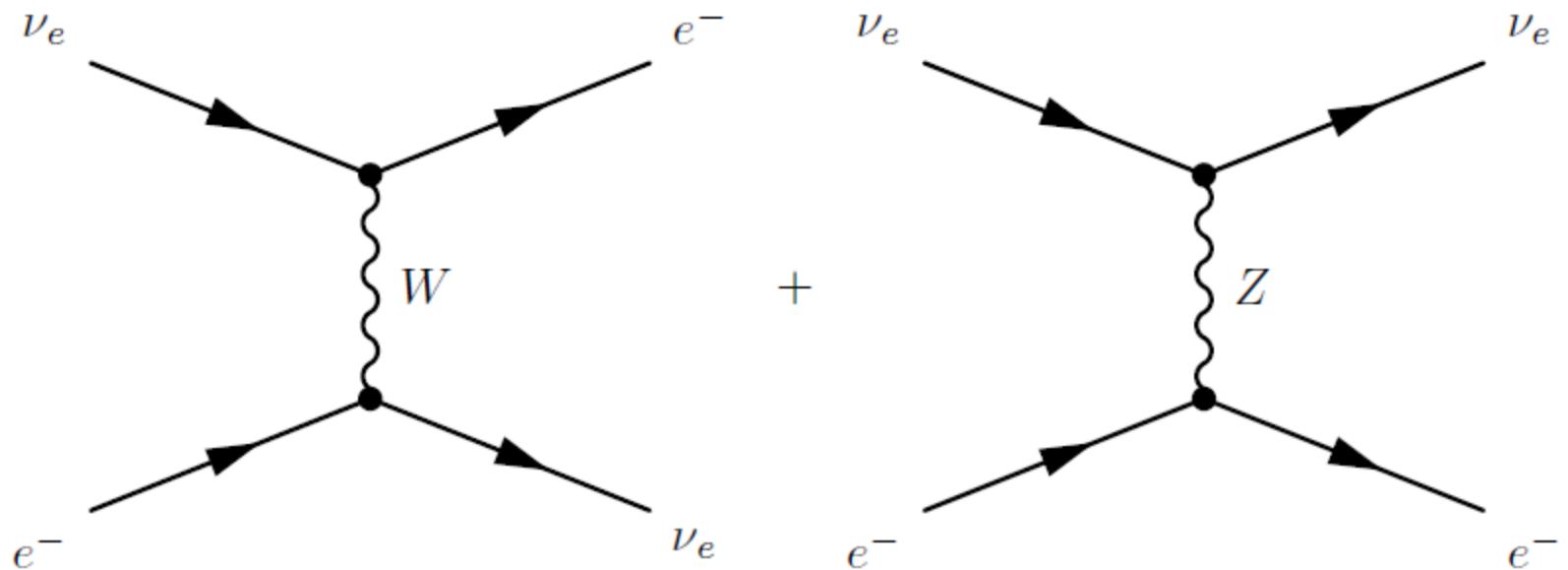


- Neutral Current

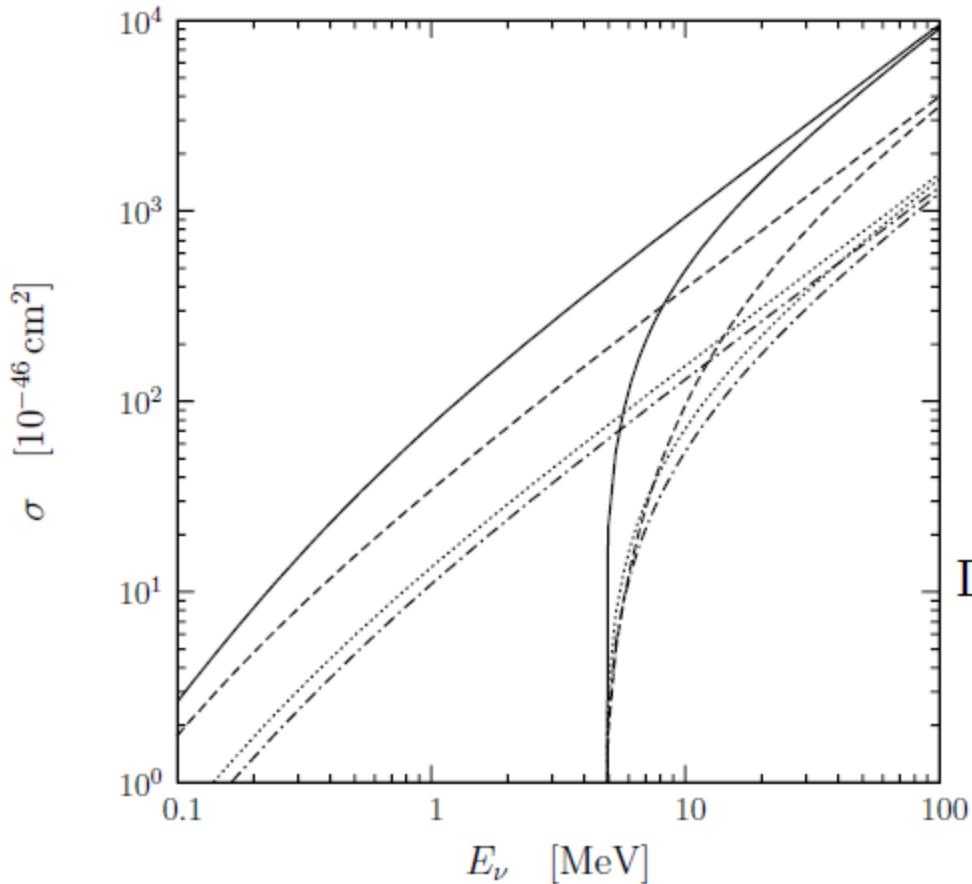


Neutrino Interactions

- Electron + electron neutrino elastic scattering



Neutrino Interactions



Solid line: $\nu_e + e^- \rightarrow \nu_e + e^-$

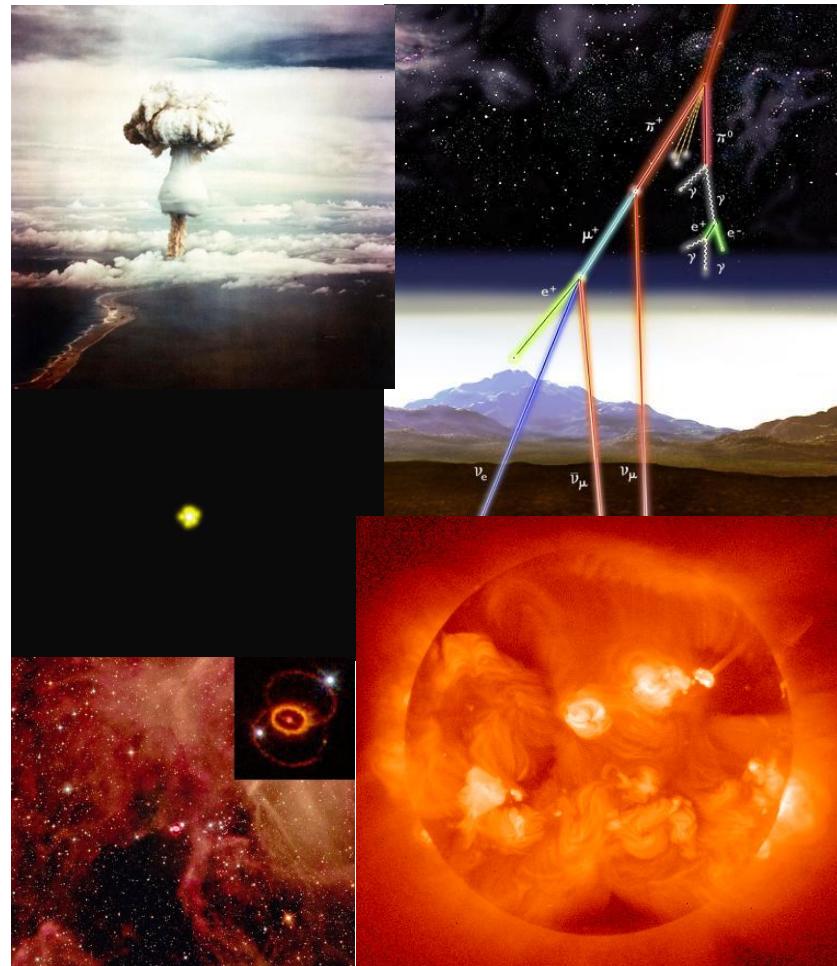
Dashed line: $\bar{\nu}_e + e^- \rightarrow \bar{\nu}_e + e^-$

Dotted line: $\nu_{\mu,\tau} + e^- \rightarrow \nu_{\mu,\tau} + e^-$

dash-dotted line: $\bar{\nu}_{\mu,\tau} + e^- \rightarrow \bar{\nu}_{\mu,\tau} + e^-$

Neutrino Sources

- Artificial
- Atmospheric
- Supernova
- Solar
- Big bang
- Geologic
- & ...



Neutrino Oscillation

Neutrino Oscillation

- Mixing
- Neutrino Oscillations in vacuum
- Neutrino Oscillations in matter
- MSW effect

Mixing

- Flavour states & mass eigenstates

$$v_l = U_{li} v_i \quad l = e, \mu, \tau \quad \& \quad i = 1, 2, 3$$

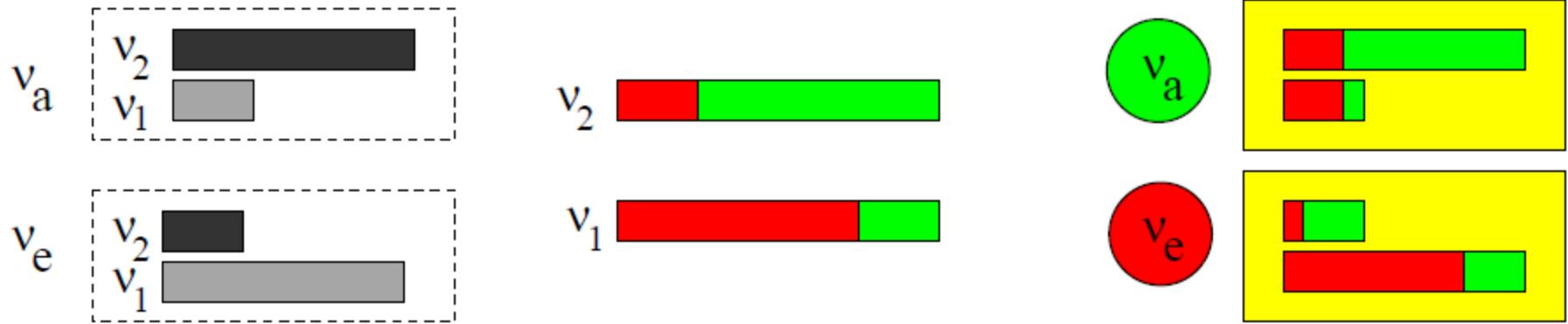
- PMNS mixing matrix
- Two neutrino mixing

$$v_l = \cos \theta v_1 + \sin \theta v_2 \quad v_1 = \cos \theta v_e - \sin \theta v_a$$

$$v_l = \cos \theta v_2 - \sin \theta v_1 \quad v_2 = \cos \theta v_a + \sin \theta v_e$$

Mixing

- Portrait of electron neutrino



The MSW effect and Solar Neutrinos, A. Yu. Smirnov, arXiv:hep-ph/0305106

Neutrino Oscillations in vacuum

$$\mathcal{H}|\nu_k\rangle = E_k |\nu_k\rangle$$

$$E_k = \sqrt{\vec{p}^2 + m_k^2}$$

$$i \frac{d}{dt} |\nu_k(t)\rangle = \mathcal{H} |\nu_k(t)\rangle$$

$$|\nu_k(t)\rangle = e^{-iE_k t} |\nu_k\rangle$$

$$|\nu_\alpha\rangle = \sum_k U_{\alpha k}^* |\nu_k\rangle \quad (\alpha = e, \mu, \tau)$$

Neutrino Oscillations in vacuum

$$|\nu_\alpha(t)\rangle = \sum_k U_{\alpha k}^* e^{-iE_k t} |\nu_k\rangle$$

$$|\nu_k\rangle = \sum_\alpha U_{\alpha k} |\nu_\alpha\rangle$$

$$|\nu_\alpha(t)\rangle = \sum_{\beta=e,\mu,\tau} \left(\sum_k U_{\alpha k}^* e^{-iE_k t} U_{\beta k} \right) |\nu_\beta\rangle$$

$$P_{\nu_\alpha \rightarrow \nu_\beta}(L, E) = \sum_{k,j} U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^* \exp \left(-i \frac{\Delta m_{kj}^2 L}{2E} \right)$$

Neutrino Oscillations in vacuum

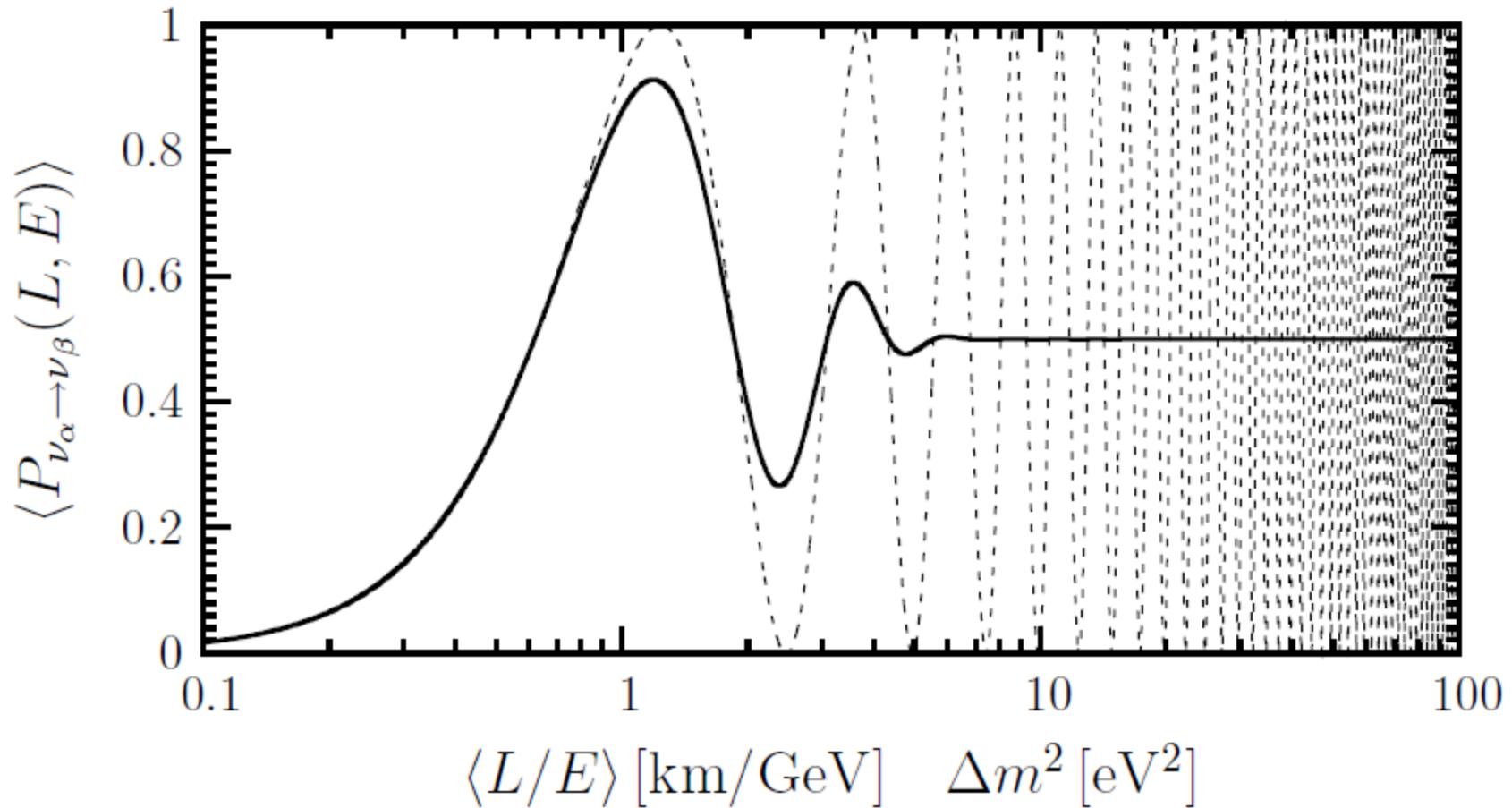
- Two neutrinos

$$U = \begin{pmatrix} \cos \vartheta & \sin \vartheta \\ -\sin \vartheta & \cos \vartheta \end{pmatrix}$$

$$P_{\nu_\alpha \rightarrow \nu_\beta}(L, E) = \sin^2 2\vartheta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right) \quad (\alpha \neq \beta)$$

$$\langle P_{\nu_\alpha \rightarrow \nu_\beta}(L, E) \rangle = \frac{1}{2} \sin^2 2\vartheta \left[1 - \left\langle \cos \left(\frac{\Delta m^2 L}{2E} \right) \right\rangle \right]$$

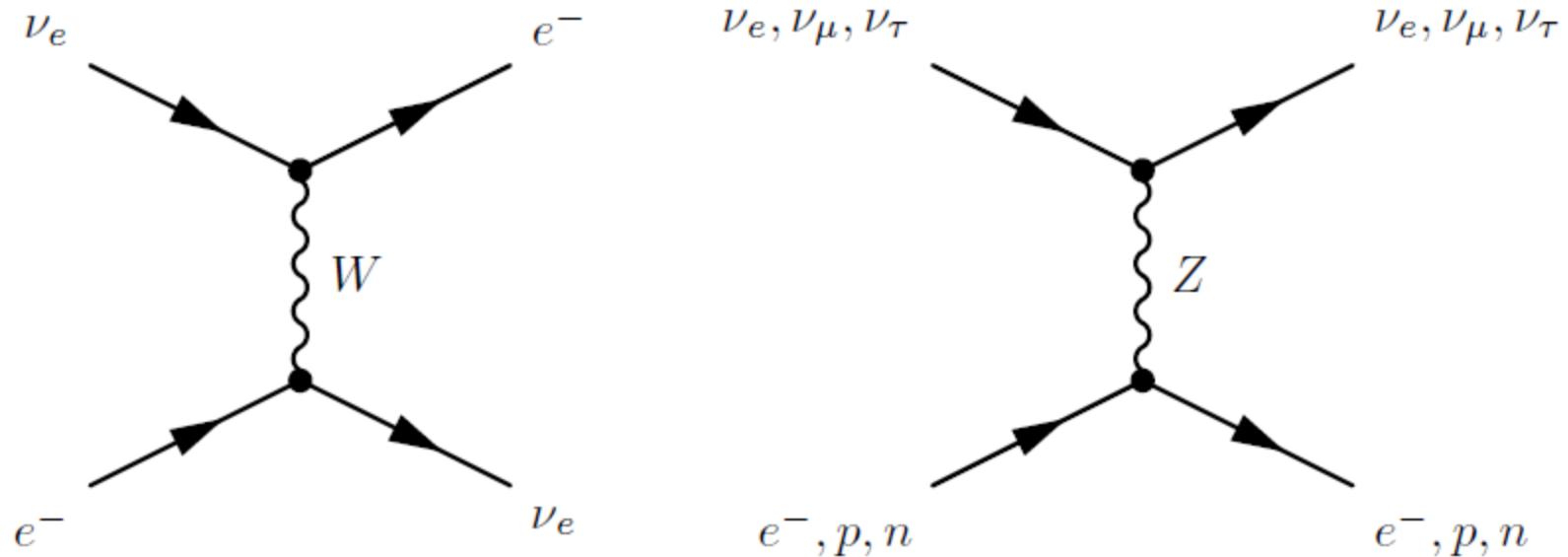
Neutrino Oscillations in vacuum



Fundamentals of Neutrino Physics and Astrophysics, Carlo Giunti & Chung W. Kim.

Neutrino Oscillations in matter

- Coherent forward elastic scattering



Neutrino Oscillations in matter

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_I$$

$$\mathcal{H}_I |\nu_\alpha\rangle = V_\alpha |\nu_\alpha\rangle$$

$$V_\alpha = V_{\text{CC}} \delta_{\alpha e} + V_{\text{NC}} = \sqrt{2} G_F \left(N_e \delta_{\alpha e} - \frac{1}{2} N_n \right)$$

$$U_M = \begin{pmatrix} \cos \vartheta_M & \sin \vartheta_M \\ -\sin \vartheta_M & \cos \vartheta_M \end{pmatrix}$$

$$\Delta m_M^2 = \sqrt{(\Delta m^2 \cos 2\vartheta - A_{\text{CC}})^2 + (\Delta m^2 \sin 2\vartheta)^2}$$

MSW effect

$$A_{\text{CC}} \equiv 2 E V_{\text{CC}} = 2 \sqrt{2} E G_F N_e$$

$$\tan 2\vartheta_M = \frac{\tan 2\vartheta}{1 - \frac{A_{\text{CC}}}{\Delta m^2 \cos 2\vartheta}}$$

$$A_{\text{CC}}^R = \Delta m^2 \cos 2\vartheta$$

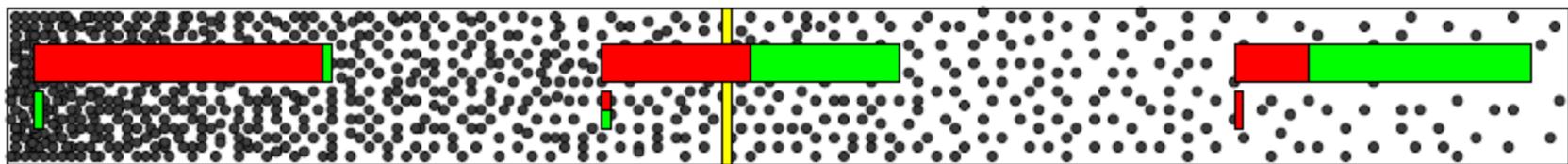
$$N_e^R = \frac{\Delta m^2 \cos 2\vartheta}{2\sqrt{2} E G_F}$$

$$\Delta m_M^2 |_R = \Delta m^2 \sin 2\vartheta$$

MSW effect

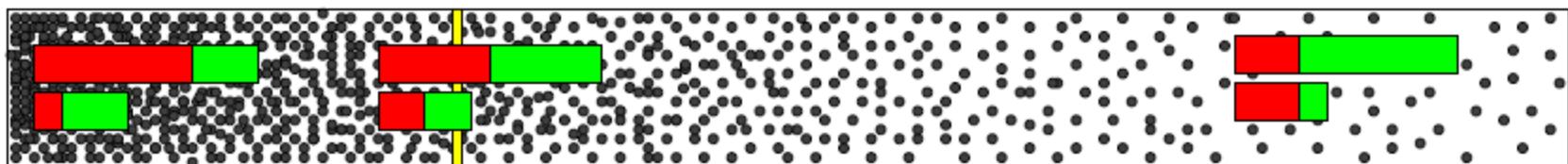
$$n_e^O \gg n_e^R$$

non-oscillatory conversion



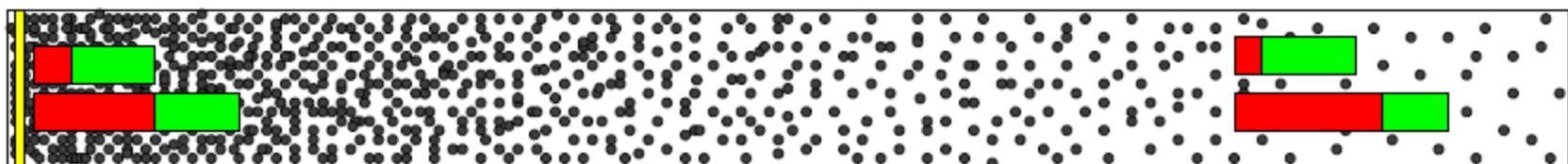
$$n_e^O > n_e^R$$

conversion + oscillations



$$n_e^O < n_e^R$$

oscillations + small matter effect

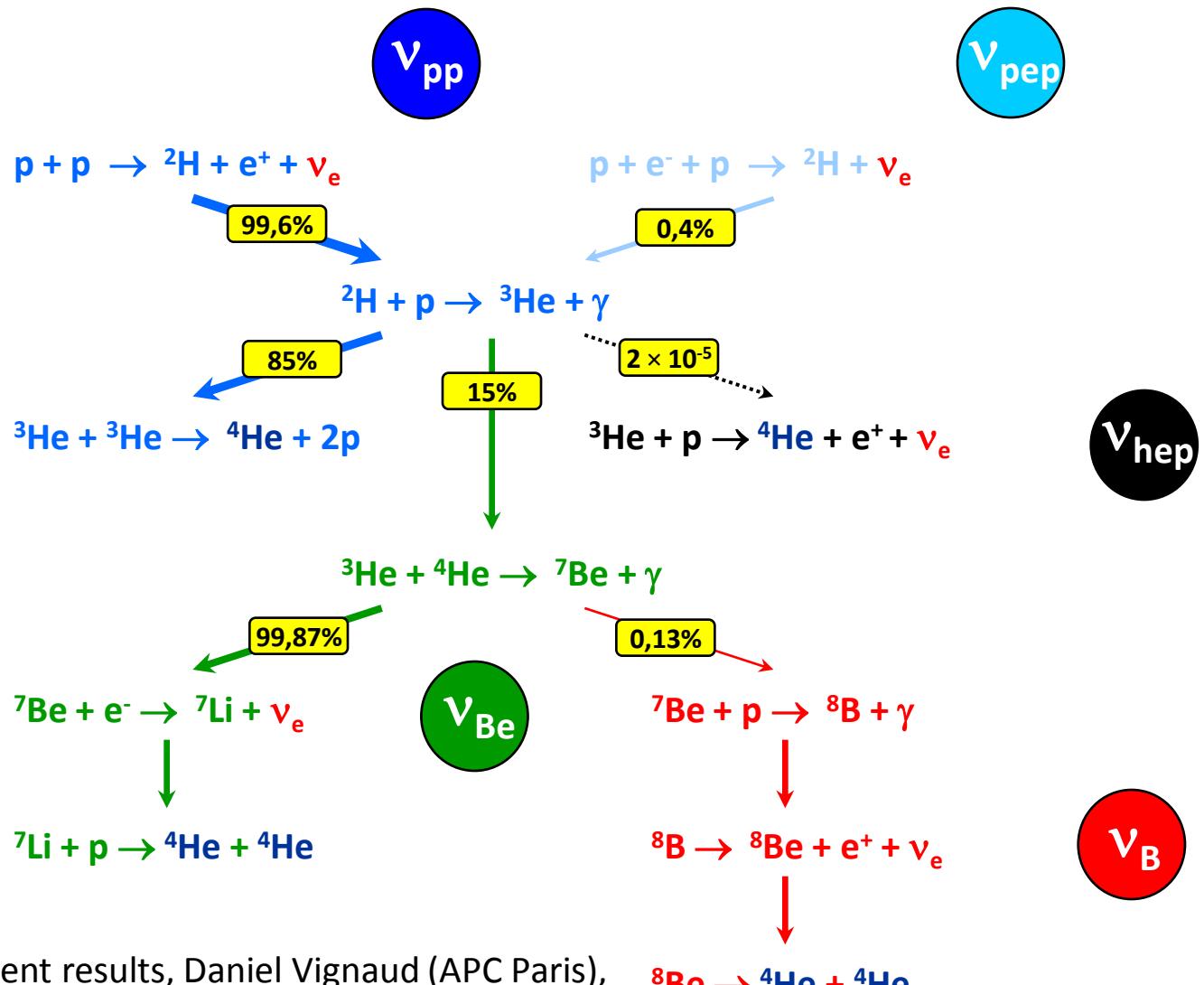


Solar Neutrinos

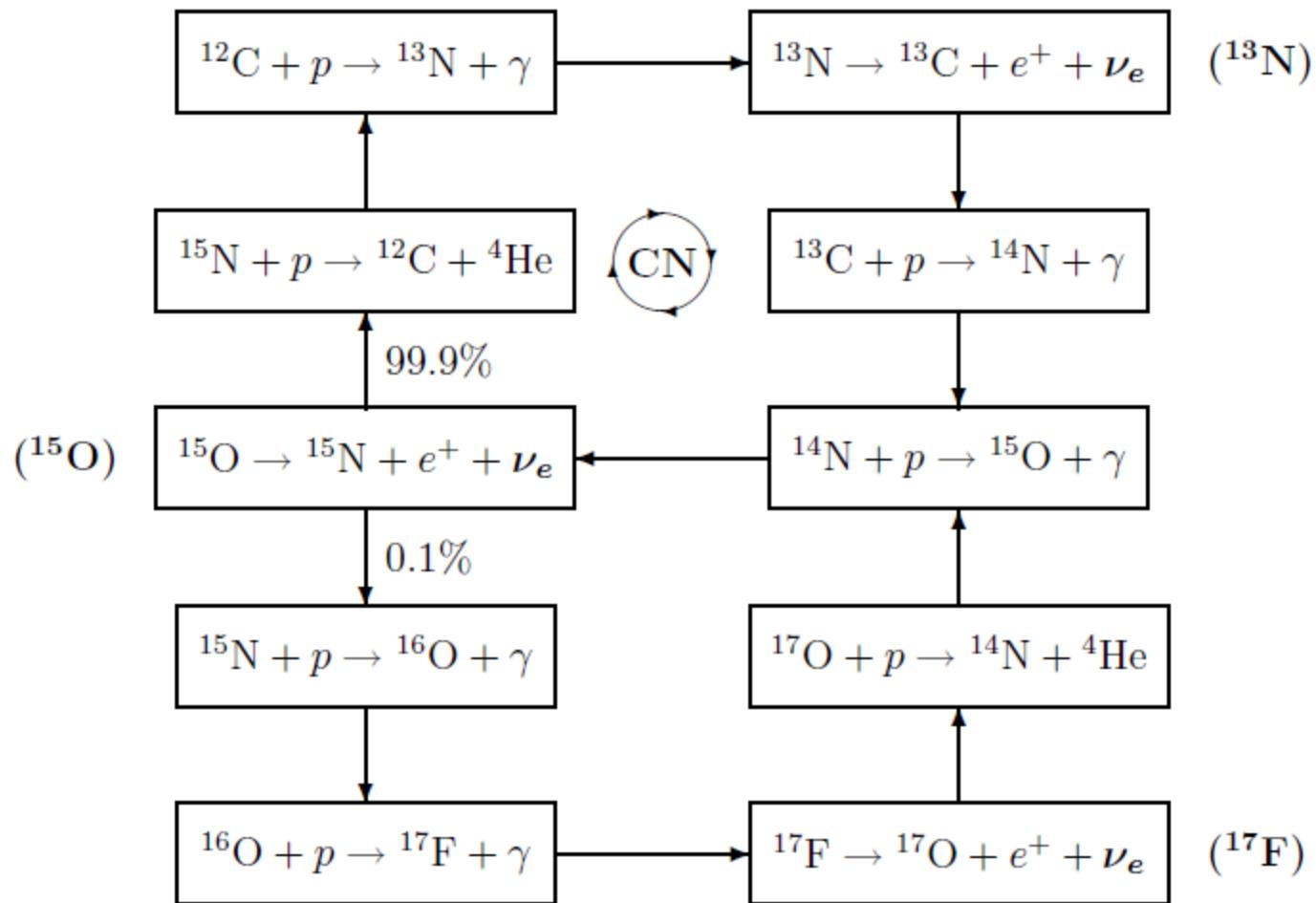
Solar Neutrinos

- Two type of thermonuclear reactions
 - pp chain
 - CNO cycle
- Standard Solar Model (SSM) Neutrinos

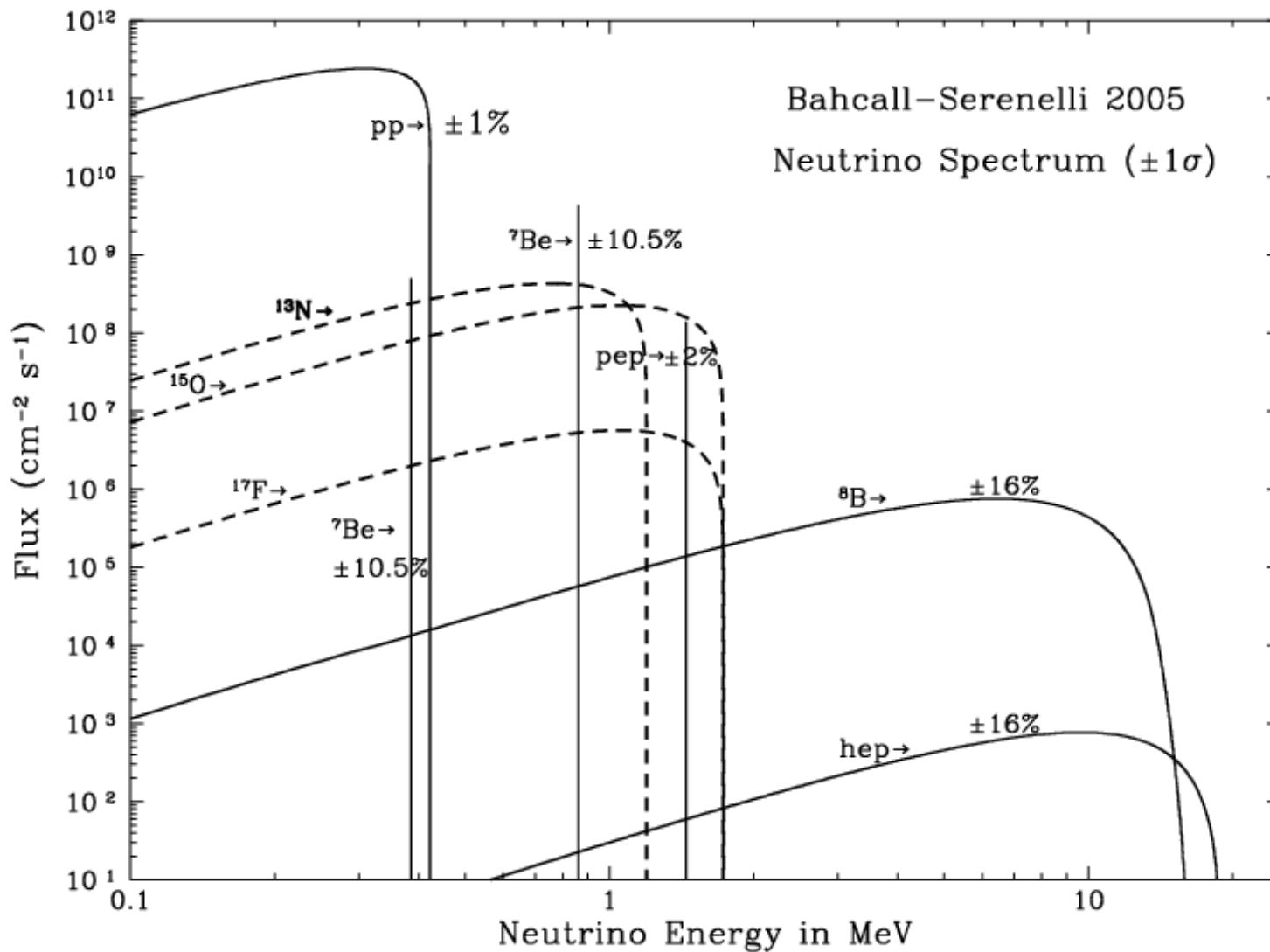
pp chain



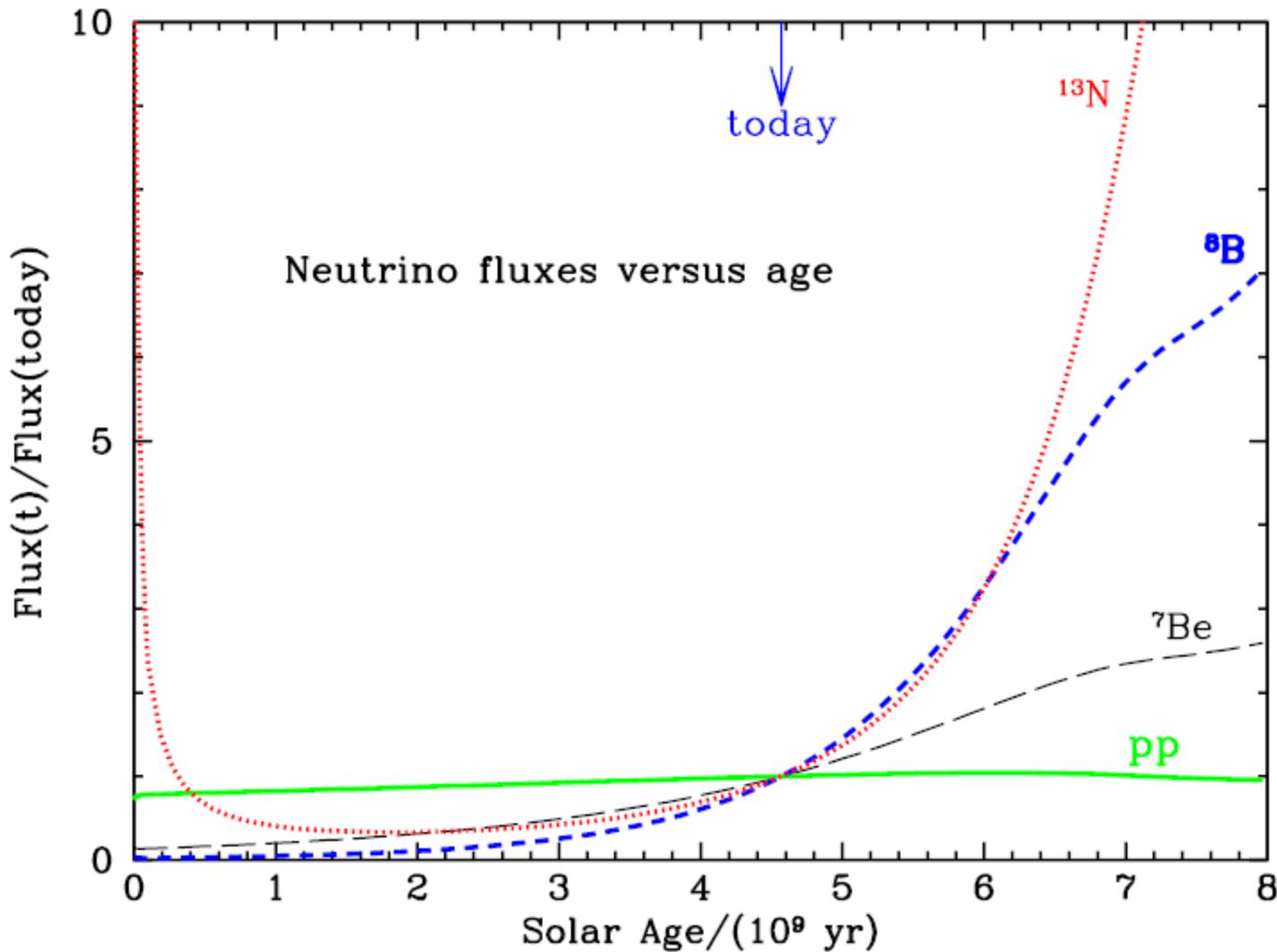
CNO cycle



SSM Neutrinos



SSM Neutrinos



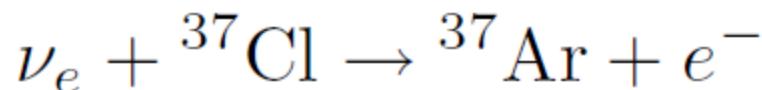
Solar Neutrino Experiments

Solar Neutrino Experiments

- Homestake experiment
- Gallium experiments
- KamiokaNDE
- Super-KamiokaNDE (SK)
- The Sudbury Neutrino Observatory (SNO)

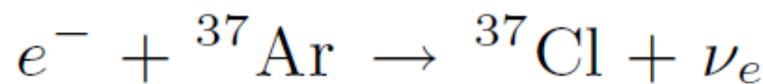
Homestake experiment

- Proposed in 1964

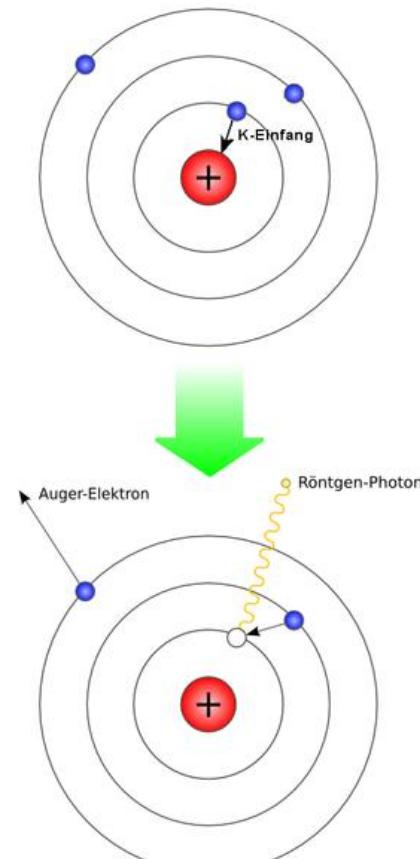


$$E_\nu^{\text{th}} = 0.814 \text{ MeV}$$

- Electron capture



- Auger electron



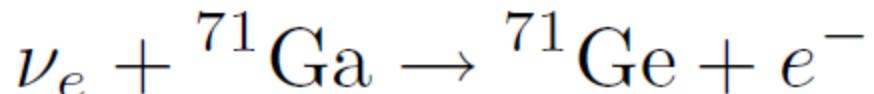
Homestake experiment

- Located 1478 m below the surface
- volume of 6×10^5 liters
- steel tank 6.1 m in diameter and 14.6 m long
- containing 2.16×10^{30} atoms of ^{37}Cl (133 ton)
- 615 ton of tetrachloroethylene C_2Cl_4

Homestake experiment

- first data indicated in 1968
- 108 extraction from March 1970 to February 1994
- Solar Neutrino Problem (SNP)
- Changes to the Solar Model

Gallium experiments



$$E_\nu^{\text{th}} = 0.233 \text{ MeV}$$

- GALLium EXperiment (GALLEX)
- Gallium Neutrino Observatory (GNO)
- The Soviet–American Gallium Experiment (SAGE)

KamiokaNDE

- Kamioka Nucleon Decay Experiment
- Kamioka Neutrino Detection Experiment
- Water Cherenkov detector
- 1000 m underground
- Kamiokande-I , II, III
- $E_{th} = 9.0, 7.2, 6.7 \text{ MeV}$

Kamiokande

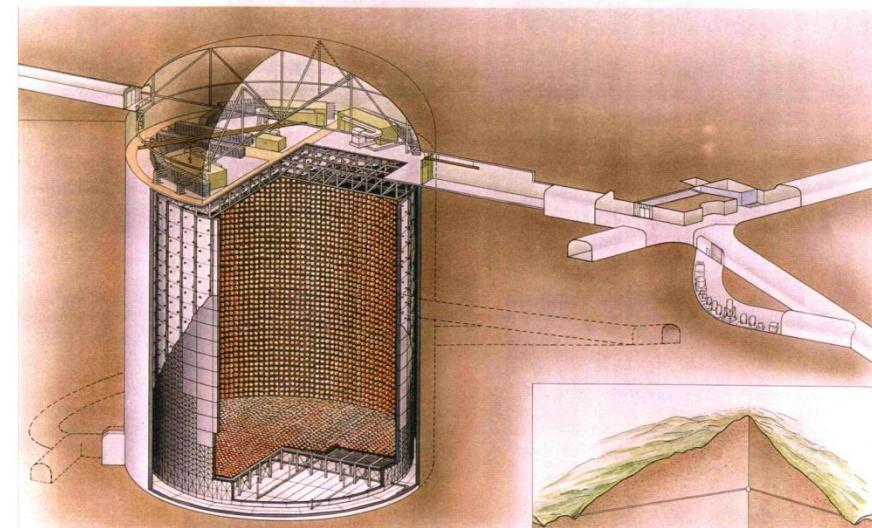
- 3 kton water, 1000 PMTs
- Elastic scattering

$$\nu_\alpha + e^- \rightarrow \nu_\alpha + e^-$$

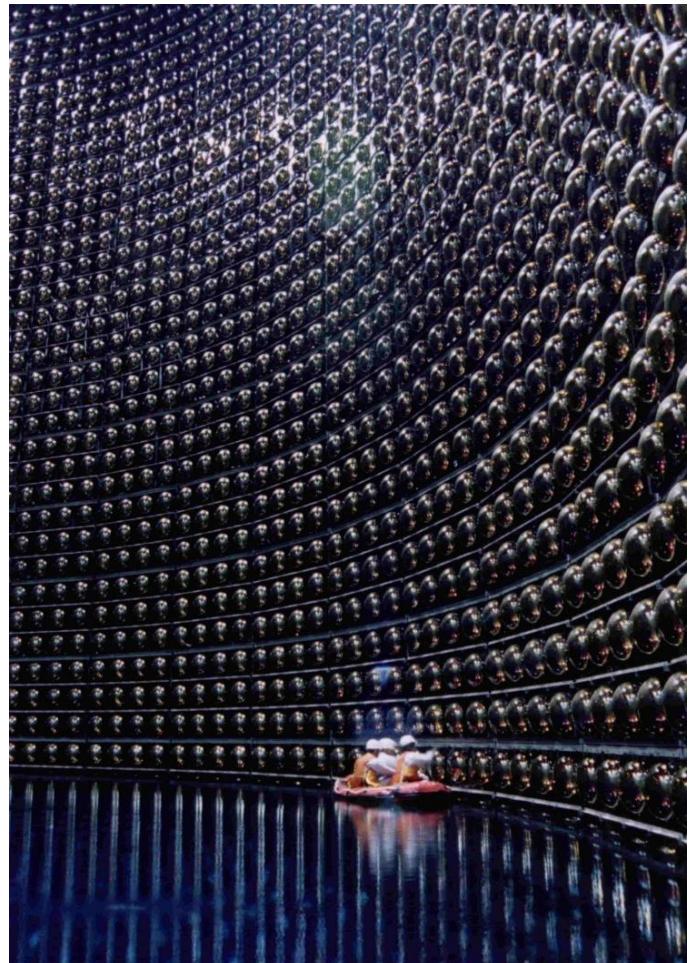
- Sensitive to electron
- ${}^8\text{B}$ solar ν_e 's measured by Kamiokande is about half of the SSM flux

Super-Kamiokande

- 50 kton water
- 11146 PMTs

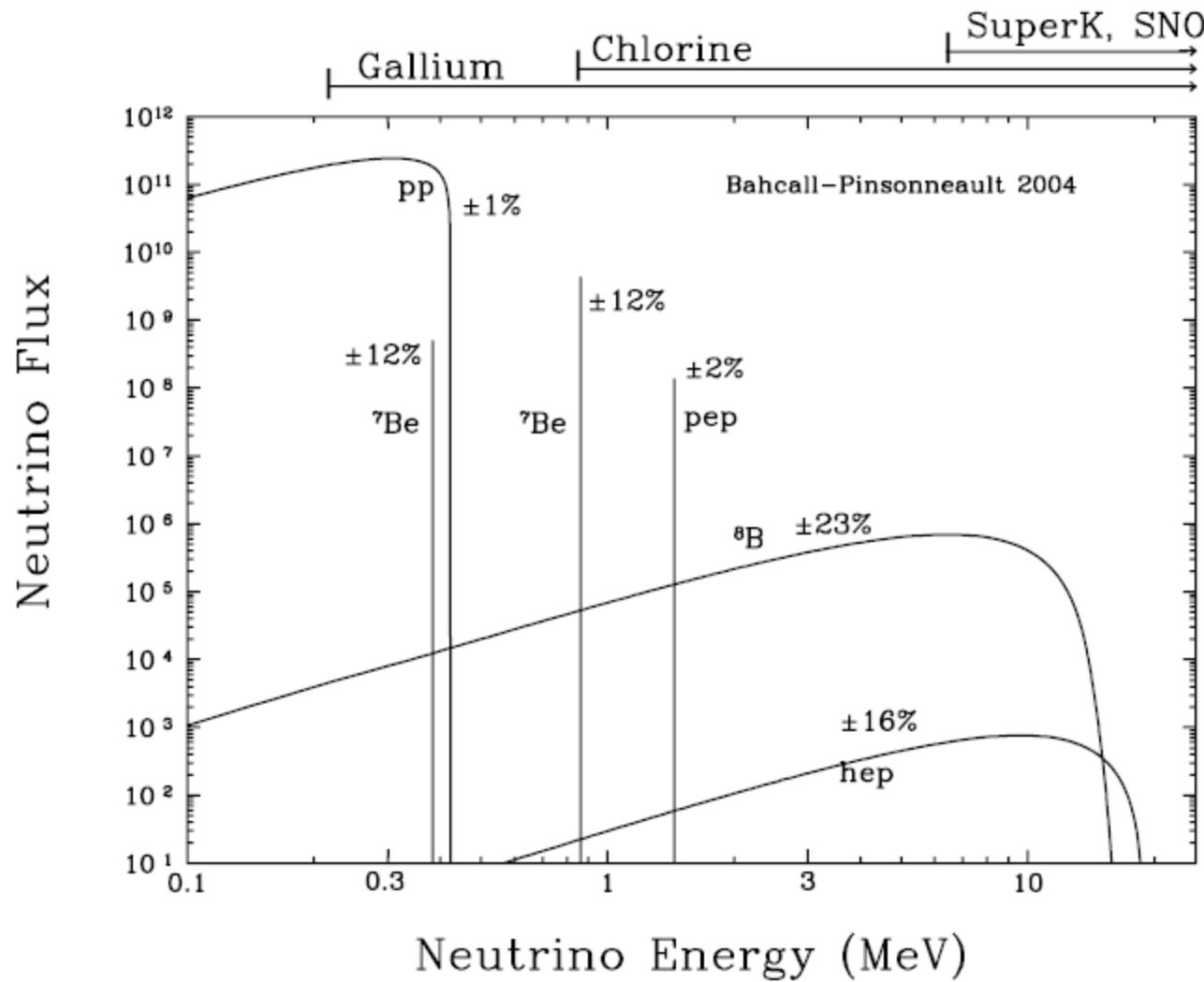


SUPERKAMIOKANDE INSTITUTE FOR COSMIC RAY RESEARCH UNIVERSITY OF TOKYO

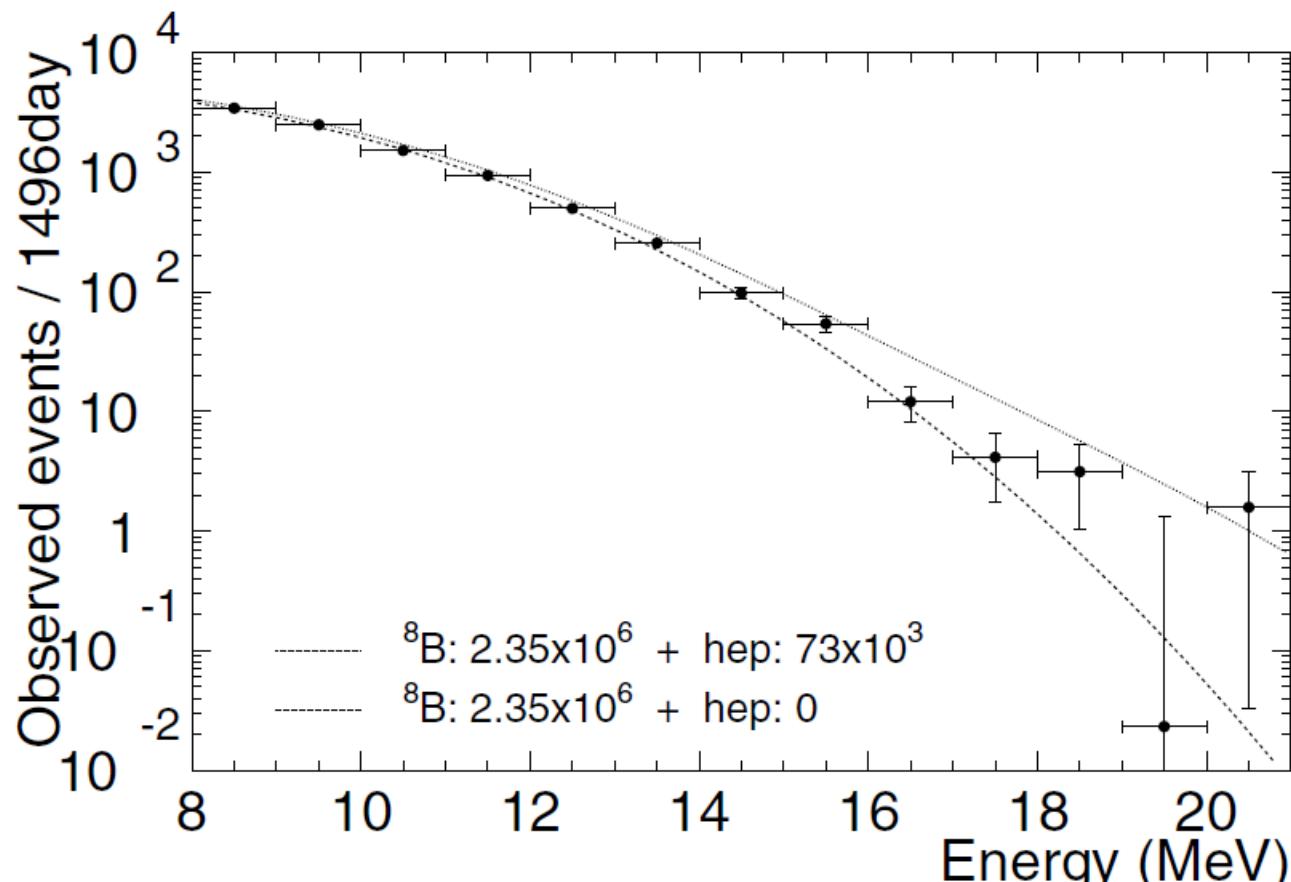


NIKONEN GOKKEI

Solar Neutrino Experiments



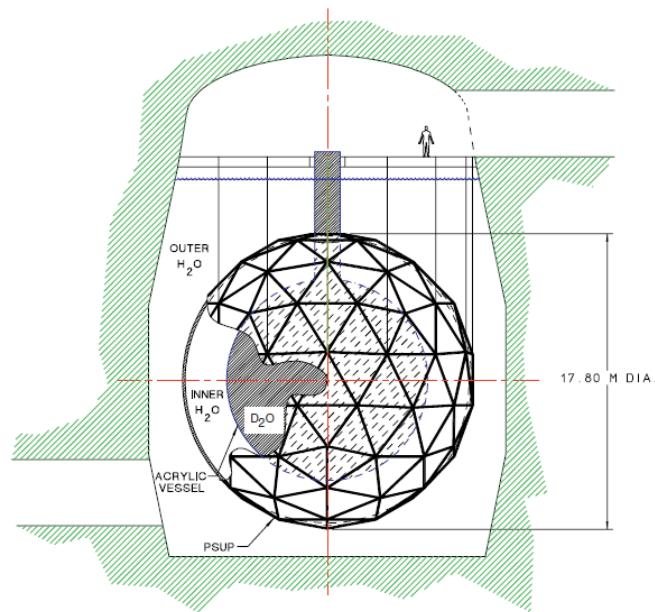
Super-Kamiokande



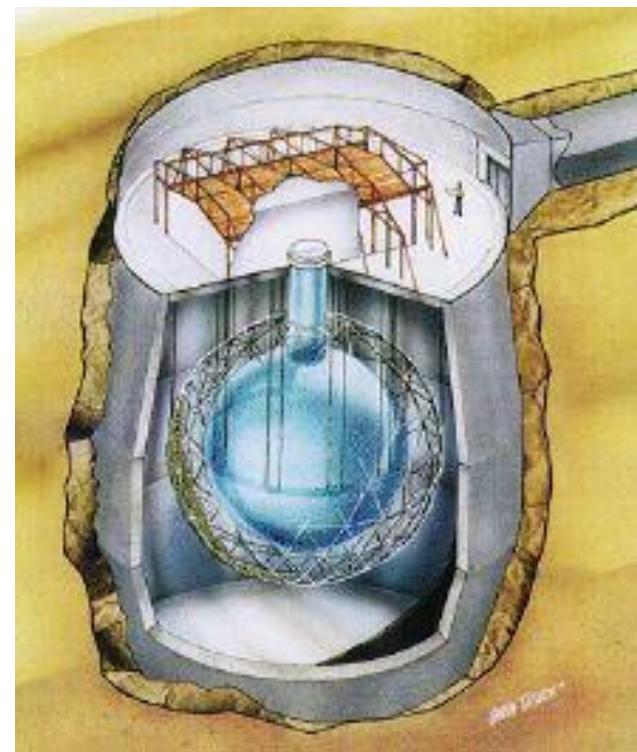
$$\Phi_{hep}^{SK} < 73 \times 10^3 \text{ cm}^{-2} \text{ s}^{-1}$$

SNO

- one kiloton of 99.92% isotopically pure D₂O
- 9456 PMTs



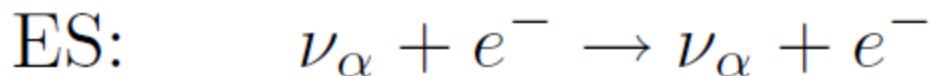
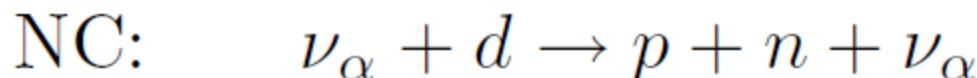
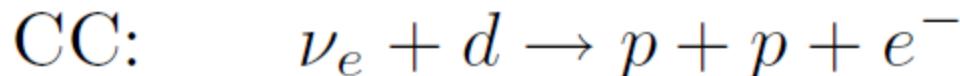
Fundamentals of Neutrino Physics and
Astrophysics, Carlo Giunti & Chung W. Kim.



Ryan Martin, Queen's University,
Kingston, ON, Canada, 8th January
2007- EPFL

SNO

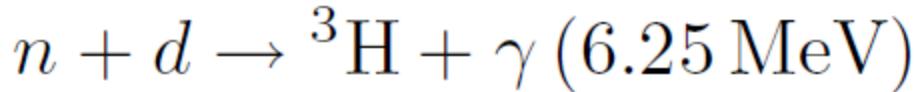
- detects through three reactions



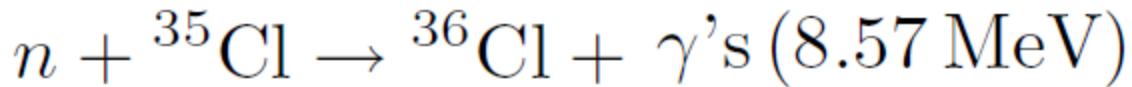
- NC reaction on deuterium is important for checking the neutrino oscillation solution of the SNP

SNO

- D₂O Phase



- NaCl Phase, 2 ton NaCl



- Third Phase

hundred ³He tubes

$$\sigma({}^{35}\text{Cl}) = 44 \text{ b}$$

$$\sigma(D) = 0.5 \text{ mb}$$

George Ewan, for the SNO Collaboration *Beyond the desert 2003*



SNO

- Salt phase

$$\Phi_{\text{CC}}^{\text{SNO}} = (1.68 \pm 0.06^{+0.08}_{-0.09}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

$$\Phi_{\text{NC}}^{\text{SNO}} = (4.94 \pm 0.21^{+0.38}_{-0.34}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

$$\Phi_{\text{ES}}^{\text{SNO}} = (2.35 \pm 0.22 \pm 0.15) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

$$\Phi_{\text{CC}}^{\text{SNO}} = \Phi_{\nu_e}^{\text{SNO}}$$

$$\Phi_{\nu_\mu, \nu_\tau}^{\text{SNO, NC}} = (3.26 \pm 0.25^{+0.40}_{-0.35}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

$$\Phi_{\nu_\mu, \nu_\tau}^{\text{SNO, ES}} = (4.36 \pm 1.52^{+0.90}_{-0.87}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

Conclusions

Conclusions

- Vacuum oscillation disfavored
 - no significant seasonal variation
- Resonance flavor transition
 - Small Mixing Angle (SMA)
 - Large Mixing Angle (LMA)
 - Quasi-Vacuum Oscillation (QVO)
 - LOW

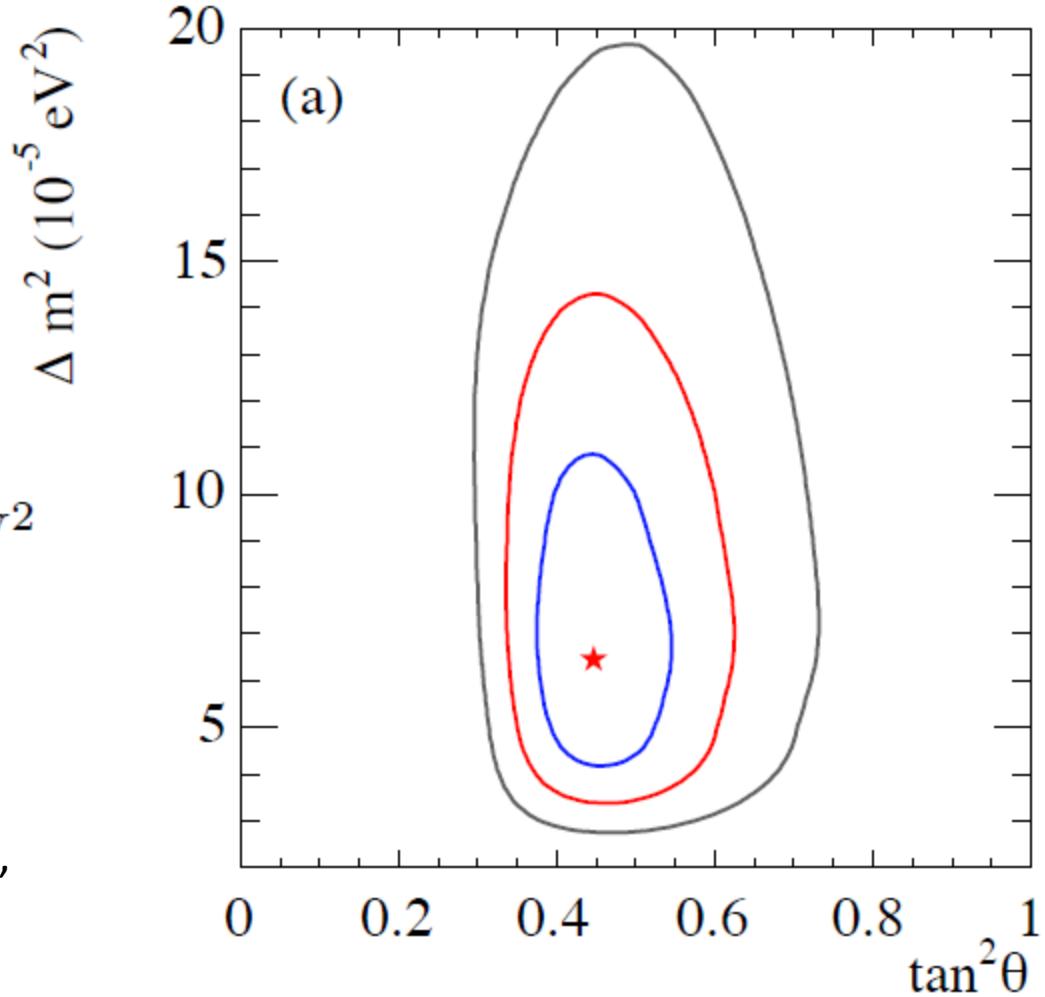
Conclusions

Allowed region in the
 $\tan^2 \theta$ - Δm^2 plane
(LMA) obtained from
a global analysis of
solar neutrino data

$$\Delta m^2 = (6.5^{+4.4}_{-2.3}) \times 10^{-5} \text{ eV}^2$$

$$\tan^2 \vartheta = 0.45^{+0.09}_{-0.08}$$

B. Aharmim et al., Phys. Rev., C72,
055502, 2005, nucl-ex/0502021



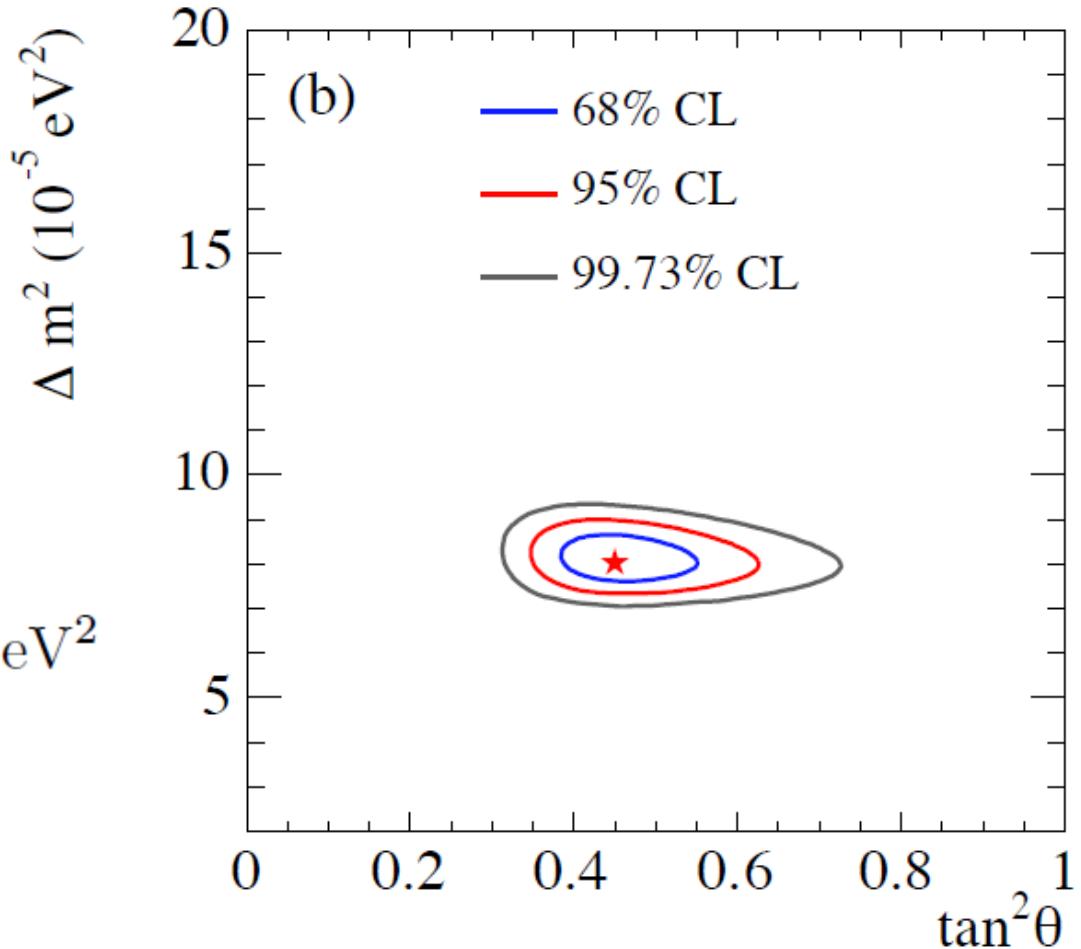
Conclusions

Reactor experiment
(KamLAND) +
global solar
neutrino data

$$\tan^2 \vartheta = 0.45^{+0.09}_{-0.07}$$

$$\Delta m^2 = (8.0^{+0.6}_{-0.4}) \times 10^{-5} \text{ eV}^2$$

T. Araki et al., Phys. Rev. Lett.,
94, 081801, 2005, hep-
ex/0406035



Summary

- Neutrinos
- Neutrino oscillation
- Solar neutrinos
- Solar neutrino experiments & SNP
- Conclusions



*Thanks for your
attention*